

Using `asremlPlus`, in conjunction with `asreml`, to do the analysis of a wheat experiment that includes choosing a local spatial variation model using AICs

Chris Brien

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This vignette shows how to use `asremlPlus` (Brien, 2024), in conjunction with `asreml` (Butler et al., 2023), to select the terms to be included in a mixed model for an experiment that involves spatial variation by comparing of information criteria . It also illustrates diagnostic checking and prediction production and presentation for this experiment. Here, `asremlPlus` and `asreml` are packages for the R Statistical Computing environment (R Core Team, 2024).

It is divided into the following main sections:

1. Set up the initial model for this experiment
2. Compare a series of information criteria to select a linear mixed model for the data
3. Diagnostic checking using residual plots and variofaces
4. Prediction production and presentation

1. Set up the initial model for this experiment

```
library(asreml, quietly=TRUE)
```

```
## Offline License checked out Sat Oct 26 18:57:03 2024
```

```
## Loading ASReML-R version 4.2
```

```
library(asremlPlus)
library(parallel)
library(doParallel)
```

```
## Loading required package: foreach
```

```
## Loading required package: iterators
```

```
library(foreach)
suppressMessages(library(qqplotr, quietly=TRUE))
options(width = 100)
```

Get data available in asremlPlus

The data are from a 1976 spring wheat experiment and are taken from Gilmour et al. (1995). An analysis is presented in the `asreml` manual by Butler et al. (2023, Section 7.6), although they suggest that it is a barley experiment.

```
data(Wheat.dat)
```

Add row and column covariates for the spatial modelling

```
tmp.dat <- within(Wheat.dat,
  {
    cColumn <- dae::as.numfac(Column)
    cColumn <- cColumn - mean(unique(cColumn))
    cRow <- dae::as.numfac(Row)
    cRow <- cRow - mean(unique(cRow))
  })
```

Fit an initial model - Row and column random

In the following, an initial model is fitted that has the terms that would be included for a balanced lattice. In addition, a term `WithinColPairs` has been included to allow for extraneous variation arising between pairs of adjacent lanes.

```
current.asr <- do.call(asreml,
  list(yield ~ Rep + WithinColPairs + Variety,
    random = ~ Row + Column,
    residual = ~ Row:Column,
    data = tmp.dat))
```

```
## ASReML Version 4.2 26/10/2024 18:57:04
##           LogLik      Sigma2      DF      wall
##  1      -702.7015    26232.20    119    18:57:04
##  2      -700.4838    24394.12    119    18:57:04
##  3      -698.4908    22487.75    119    18:57:04
##  4      -697.5842    21242.11    119    18:57:04
##  5      -697.3673    20590.05    119    18:57:04
##  6      -697.3595    20477.28    119    18:57:04
```

Intialize a model sequence by loading the current fit into an `asrtests` object

In creating the `asrtests` object, `IClikelihood` is set to `full` so that the full Restricted Maximum Likelihood (full REML) of Verbyla, 2019 is incorporated into the `tests.summary` of the `asrtests` object.

```
current.asrt <- as.asrtests(current.asr, NULL, NULL, IClikelihood = "full",
  label = "Initial model")
```

```
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, :
## Log-likelihood not converged
```

Check for and remove any boundary terms and print a summary of the fit in the `asrtests` object

```
current.asrt <- rmboundary(current.asrt)
print(current.asrt)

##
##
## ##### Summary of the fitted variance parameters
##
##           component std.error  z.ratio bound %ch
## Row           5943.898  3815.514  1.557824    P 0.0
## Column        12380.527  6323.542  1.957847    P 0.3
## Row:Column!R  20477.280  2896.642  7.069316    P 0.0
##
##
## ##### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
##           Df denDF  F.inc    Pr
## (Intercept)  1  14.9 1390.00 0.0000
## Rep          5  25.3   6.04 0.0008
## WithinColPairs  1  10.4   0.49 0.4998
## Variety      24 104.8   4.71 0.0000
##
##
## ##### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##           terms DF denDF  p      AIC      BIC      action
## 1 Initial model 31      3 NA 1720.891 1823.253 Starting model
```

The `test.summary` output shows that no changes have been made to the model loaded using `as.asrtests`. The pseudo-anova table shows that Varieties are highly significant ($p < 0.001$)

2. Compare a series of information criteria to select a linear mixed model for the data

In this section, models are compared using Akaike Information Criterion (AICs) based on the full REML.

Check the need for the term for within Column pairs (a post hoc factor)

```
current.asrt <- changeModelOnIC(current.asrt, dropFixed = "WithinColPairs",
                                label = "Try dropping withinColPairs", ICl likelihood = "full")
```

```
## ASReml Version 4.2 26/10/2024 18:57:06
##           LogLik           Sigma2           DF           wall
## 1      -697.3595          20472.09          119          18:57:06
```

```
## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, :
## Log-likelihood not converged
```

```
print(current.asrt)
```

```
##
##
## ##### Summary of the fitted variance parameters
##
##           component std.error  z.ratio bound %ch
## Row           5941.153  3813.586 1.557891    P    0
## Column        11165.335  5583.267 1.999785    P    0
## Row:Column!R  20472.402  2895.582 7.070219    P    0
##
##
## ##### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
##           Df denDF  F.inc  Pr
## (Intercept) 1  15.3 1466.00 0e+00
## Rep          5  26.7   6.11 7e-04
## Variety     24 105.3   4.73 0e+00
##
##
## ##### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##           terms DF denDF  p           AIC           BIC           action
## 1           Initial model 31      3 NA 1720.89134 1823.252944 Starting model
## 2 Try dropping withinColPairs -1      0 NA  -2.28193  -5.292565 Swapped
```

It is clear in the call to `changeModelOnIC` that the model is being changed by dropping the `withinColPairs` term, which could also be achieved using `update.asreml`. However, an `asremlPlus` model-changing function operates on an `asrtests` object, that includes an `asreml` object, and, except for `changeTerms.asrtests`, results in an `asrtests` object that may contain the changed model or the supplied model depending on the results of hypothesis tests or comparisons of information criteria. In addition, the result of the test or comparison will be added to a `test.summary` data.frame stored in the new `asrtests` object and, if the model was changed, the `wald.tab` in the new `asrtests` object will have been updated for the new model.

In this case, as can be seen from the summary of `current.asrt` after the call, the model without `withinColPairs` had a smaller AIC and so now the model stored in `current.asrt` does not include `withinColPairs`. The `wald.tab` has been updated for the new model.

Choose a model for local spatial variation from several potential models

This example has been analyzed using a model for the local spatial variation based on a separable auto-correlation process of order one (Butler et al., 2023). The need for this model can be assessed using the function `addSpatialModelOnIC` from `asremlPlus` that uses a forward selection strategy for fitting a correlation model (see output below). For this function, the spatial model to be fitted, the centred covariates for the two dimensions of the grid, and the factors corresponding to the covariates must be specified. Also, `IClikelihood` is set to `full` so that the likelihood will be based on the full REML. Because the model that incorporates the spatial model has a smaller AIC, it is the model returned in `spatial.ar1.asrt`.

The print of `spatial.ar1.asrt` shows that an `ar1` model for Row was tried first and was found to reduce the AIC by 11.898 and so became the current model. Next a model that incorporates an `ar1` function for Column was similarly tried and became the current model. This model includes a nugget variance, unless either the variance for Row:Column term or the Residual is bound or fixed. The Residual is the nugget term and represents non-spatial variance, such as measurement error. An appraisal of the need for a nugget term was made by comparing the fits with the residual variance unfixed and fixed at one. The model with the unfixed residual variance was chosen and is the model to be returned. That is, this model includes a term for nugget variance.

```
spatial.ar1.asrt <- addSpatialModelOnIC(current.asrt, spatial.model = "corr",
                                       row.covar = "cRow", col.covar = "cColumn",
                                       row.factor = "Row", col.factor = "Column",
                                       IClikelihood = "full")
```

```
## WARN [2024-10-26 18:57:09] Warning : Oscillating parameter(s) reset to average value (iteration 7)

## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Warning :
## Oscillating parameter(s) reset to average value (iteration 7)

## WARN [2024-10-26 18:57:10] Warning : Oscillating parameter(s) reset to average value (iteration 12)

## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Warning :
## Oscillating parameter(s) reset to average value (iteration 12)

## WARN [2024-10-26 18:57:12] Some components changed by more than 1% on the last iteration

## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration

## WARN [2024-10-26 18:57:12] Some components changed by more than 1% on the last iteration

## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration

## WARN [2024-10-26 18:57:12] Some components changed by more than 1% on the last iteration

## Warning in (function (fixed = ~1, random = ~NULL, sparse = ~NULL, residual = ~NULL, : Some
## components changed by more than 1% on the last iteration

## WARN [2024-10-26 18:57:13] The following bound terms were discounted:
## Column
```

```

## Warning in infoCriteria.asreml(asreml.obj, ICLikelihood = ic.lik, bound.exclusions = bound.exclusion
## Column

## WARN [2024-10-26 18:57:13] The following bound terms were discounted:
## Column

## Warning in infoCriteria.asreml(asreml.obj, ICLikelihood = ic.lik): The following bound terms were di
## Column

## WARN [2024-10-26 18:57:14] In analysing yield, boundary terms removed

## Warning in changeTerms.asrtests(asrtests.obj, dropFixed = dropFixed, addFixed = addFixed, : In
## analysing yield, boundary terms removed

## WARN [2024-10-26 18:57:16] The following bound terms were discounted:
## Row:Column!R

## Warning in infoCriteria.asreml(asreml.obj, ICLikelihood = ic.lik, bound.exclusions = bound.exclusion
## Row:Column!R

## WARN [2024-10-26 18:57:17] The following bound terms were discounted:
## Row:Column!R

## Warning in infoCriteria.asreml(new.asrtests.obj$asreml.obj, ICLikelihood = ic.lik, : The following b
## Row:Column!R

```

```

spatial.ar1.asrt <- rmboundary(spatial.ar1.asrt)
infoCriteria(list(nonspatial = current.asrt$asreml.obj,
                 ar1 = spatial.ar1.asrt$asreml.obj))

```

```

##          fixedDF varDF NBound      AIC      BIC  loglik
## nonspatial      0     3      0 1409.023 1417.386 -701.5117
## ar1              0     5      0 1353.762 1367.700 -671.8811

```

```

print(spatial.ar1.asrt)

```

```

##
##
## ##### Summary of the fitted variance parameters
##
##          component      std.error  z.ratio bound %ch
## Row          2.191310e+03 8.216561e+03 0.2666943    P 0.7
## Row:Column    5.183862e+04 3.376288e+04 1.5353732    P 0.1
## Row:Column!Row!cor 7.121523e-01 9.571206e-02 7.4405706    U 0.0
## Row:Column!Column!cor 8.600849e-01 1.104747e-01 7.7853552    U 0.0
## Row:Column!R    4.820487e+03 1.717447e+03 2.8067739    P 0.0
##
##
## ##### Pseudo-anova table for fixed terms
##

```

```

##
## Wald tests for fixed effects.
## Response: yield
##
##           Df denDF   F.inc     Pr
## (Intercept) 1   1.8 194.700 0.0076
## Rep          5  21.8   0.559 0.7304
## Variety      24  74.3  10.560 0.0000
##
##
## ##### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##           terms DF denDF  p      AIC      BIC      action
## 1           Initial model 31     3 NA 1720.89134 1823.252944 Starting model
## 2           Try dropping withinColPairs -1     0 NA  -2.28193  -5.292565      Swapped
## 3           Try ar1(Row) 0     2 NA  -11.89789  -5.876622      Swapped
## 4           Try ar1(Column) 0     0 NA  -55.39721  -55.397212      Swapped
## 5           Column 1     NA NA 1651.31109 1756.683324      Boundary
## 6 Try fixed nugget (residual) variance 0    -1 NA   1.81043  -1.200206      Unswapped

```

However, the spatial models that are available in `asremlPlus` also include those based on two-dimensional tensor-product natural cubic smoothing splines (TPNCSS), as described by Verbyla et al. (2018), and on two-dimensional tensor-product P-splines (TPPS), as described by Rodriguez-Alvarez et al. (2018) and Piepho, Boer and Williams (2022). The P-splines have been implemented using functions from the R package `TPSbits` authored by Sue Welham (2022)

The `asremlPlus` function `chooseSpatialModelOnIC` allows one to select the best model from amongst these spatial correlation models using the AIC or the BIC, the AIC being the default. The four models from which it selects are (i) a separable autocorrelation model on both row and column dimensions (`corr`), (ii) a two-dimensional tensor-product natural cubic smoothing spline (TPNCSS), (iii) a two-dimensional tensor-product cubic P-spline with second-difference penalties (TPPSC2), and (iv) a tensor-product two-dimensional linear P-spline with first-difference penalties (TPPSL1). By default all four are fitted and compared, but the `trySpatial` argument can be used to specify a subset of them.

The call to `chooseSpatialModelOnIC`, in addition to the arguments specifying covariates and factors, has further arguments: (i) `dropFixed` and `dropRandom` that are relevant to fitting P-splines and are used here to remove the random, overall Row and Column terms that were included in the original model so that the fitted P-spline model will be compared to a model including them and because the code for fitting P-splines also automatically includes these terms so that they would be included twice in the model to be fitted resulting in model singularities, (ii) `rotateX` and `ngridangles` so that the angles in both row and column directions for rotating the eigenvectors of the penalty matrix for the linear component of the P-splines is optimized (setting `ngridangles` to `NULL` causes the R function `nloptr::bobyqa` to be invoked for finding the optimal angles), (iii) an `asreml.option` argument to specify that the `grp` method be used in fitting the P-spline terms, this being safer because the data.frame needed for any post-fitting computation is available in the `asreml` object, and (iv) `return.asrts` to specify which `asrtests` objects are to be returned. Here we specify `all` so that `asrtests` objects for the best fits between the model supplied in the `current.asrt` and each of the spatial models is returned for all four spatial models. In this case, neither the `checkboundaryonly` nor the `IClikelihood` arguments were set because their defaults for `chooseSpatialModelOnIC` are appropriate.

```

suppressWarnings(
  spatial.asrts <- chooseSpatialModelOnIC(current.asrt,
    row.covar = "cRow", col.covar = "cColumn",
    row.factor = "Row", col.factor = "Column",

```



```
##
## #### Optimal thetas: 20.2026842421406, 64.9729346095888 with criterion 1659.433
##
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .001400 have been merged
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## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .001400 have been merged
## WARN [2024-10-26 18:58:12] Log-likelihood not converged
##
##
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .001400 have been merged
## WARN [2024-10-26 18:58:12] Log-likelihood not converged
##
##
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .001400 have been merged
## WARN [2024-10-26 18:58:13] Log-likelihood not converged
##
##
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .000900 have been merged
## WARN [2024-10-26 18:58:14] Some components changed by more than 1% on the last iteration
##
##
## Notice : Spline design points closer than .000900 have been merged
## WARN [2024-10-26 18:58:15] Some components changed by more than 1% on the last iteration
##
##
## Notice : Spline design points closer than .000900 have been merged
## WARN [2024-10-26 18:58:15] Some components changed by more than 1% on the last iteration
##
##
## Notice : Spline design points closer than .000900 have been merged
## WARN [2024-10-26 18:58:15] Some components changed by more than 1% on the last iteration
```

```
##
##
## Notice : Spline design points closer than .000900 have been merged
## Notice : Spline design points closer than .000900 have been merged
## WARN [2024-10-26 18:58:17] Some components changed by more than 1% on the last iteration
##
##
## Notice : Spline design points closer than .000900 have been merged
## WARN [2024-10-26 18:58:17] Some components changed by more than 1% on the last iteration
```

Output the results

```
print(spatial.asrts$spatial.IC)
```

```
##           fixedDF varDF      AIC      BIC    loglik
## nonspatial      30     3 1718.609 1817.960 -826.3047
## corr            30     5 1651.314 1756.687 -790.6572
## TPNCSS          33     6 1639.489 1756.904 -780.7445
## TPPSC2          33     7 1642.838 1763.263 -781.4190
## TPPSL1          30     4 1652.122 1754.484 -792.0610
```

```
print(R2adj(spatial.asrts$asrts$TPNCSS$asreml.obj, include.which.random = ~ .))
```

```
## ASReml Version 4.2 26/10/2024 18:58:18
##           LogLik      Sigma2      DF      wall
## 1      -662.1988      7657.974      117      18:58:18
## 2      -662.1988      7657.974      117      18:58:18
## 3      -662.1988      7657.974      117      18:58:18
## 4      -662.1988      7657.974      117      18:58:18
## 5      -662.1988      7657.974      117      18:58:18
## 6      -662.1988      7657.974      117      18:58:18
## 7      -662.1988      7657.974      117      18:58:18
## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
## [1] 93.3036
## attr("fixed")
## ~.
## <environment: 0x000001cf6248cfb8>
## attr("random")
## ~.
```

```
print(spatial.asrts$best.spatial.mod)
```

```
## [1] "TPNCSS"
```

```
print(spatial.asrts$asrts$TPNCSS)
```

```
##
##
```

```

## ##### Summary of the fitted variance parameters
##
##
## component std.error z.ratio bound %ch
## spl(cRow):cColumn      523.1984  372.8005  1.403427    P    0
## dev(cRow)              7663.9934 4442.0575  1.725325    P    0
## spl(cColumn)          13338.6895 9236.0431  1.444200    P    0
## spl(cColumn):cRow      366.7696  322.7484  1.136395    P    0
## spl(cRow):spl(cColumn) 3630.2470 2186.2215  1.660512    P    0
## Row:Column!R          7657.9744 1312.1971  5.835994    P    0
##
##
## ##### Pseudo-anova table for fixed terms
##
##
## Wald tests for fixed effects.
## Response: yield
##
##      Df denDF  F.inc    Pr
## (Intercept)  1   6.8 2645.00 0.0000
## Rep          5  41.3  20.45 0.0000
## Variety     24  86.5  10.15 0.0000
## cRow        1   7.0   0.07 0.7954
## cColumn     1  30.1  20.30 0.0001
## cRow:cColumn 1  64.3  22.00 0.0000
##
##
## ##### Sequence of model investigations
##
## (If a row has NA for p but not denDF, DF and denDF relate to fixed and variance parameter numbers)
##
##      terms DF denDF  p      AIC      BIC      action
## 1      Initial model 31    3 NA 1720.89134 1823.252944 Starting model
## 2 Try dropping withinColPairs -1    0 NA  -2.28193  -5.292565      Swapped
## 3 Try tensor NCS splines 3    3 NA  -79.12051  -61.056702      Swapped
## 4      dev(cColumn) 1    NA NA 1639.48896 1756.903736      Boundary
## 5      spl(cRow) 1    NA NA 1639.48892 1756.903694      Boundary

printFormulae(spatial.asrts$asrts$TPNCSS$asreml.obj)

##
##
## ##### Formulae from asreml object
##
## fixed: yield ~ Rep + Variety + cRow + cColumn + cRow:cColumn
## random: ~ spl(cColumn) + dev(cRow) + spl(cRow):cColumn + spl(cColumn):cRow + spl(cRow):spl(cColumn)
## residual: ~ Row:Column

```

The output shows that the TPNCSS model has the lowest AIC and so is selected as the best model. The adjusted R^2 value shows that the fixed and random terms in the fitted model account for 93% of the total variation in the yield. The model fitted for the TPNCSS model has been printed using `printFormulae.asreml`. The fitted model includes the term `dev(cRow)` that is equivalent to a random Row term and measures the deviations of the Row trend from a linear trend, the `spl(cRow)` term having been dropped because it was estimated to be zero. The Wald F -statistic for Variety is now 10.15 with 86.5 denominator degrees of free-

dom, as compared to 10.56 and 74.3 for the correlation model and 4.71 and 105.3 for the initial nonspatial model.

3. Diagnosing checking using residual plots and variofaces

Get current fitted asreml object and update to include standardized residuals

```
current.asr <- spatial.asrts$asrts$TPNCSS$asreml.obj  
current.asr <- update(current.asr, aom=TRUE)
```

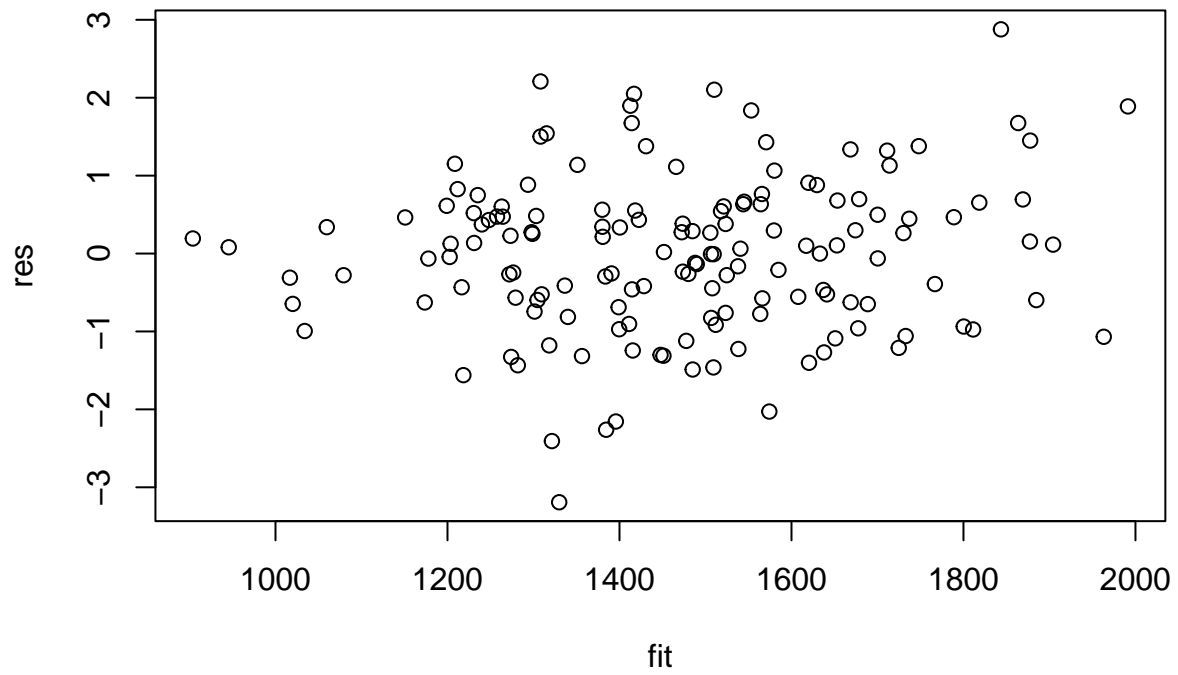
```
## ASReml Version 4.2 26/10/2024 18:58:19  
##           LogLik      Sigma2      DF      wall  
## 1      -662.1988      7657.974      117      18:58:20  
## 2      -662.1988      7657.974      117      18:58:20  
## 3      -662.1988      7657.974      117      18:58:20  
## 4      -662.1988      7657.974      117      18:58:20  
## 5      -662.1988      7657.974      117      18:58:20  
## 6      -662.1988      7657.974      117      18:58:20  
## 7      -662.1988      7657.974      117      18:58:20  
## Notice   : Spline design points closer than .001400 have been merged  
## Notice   : Spline design points closer than .000900 have been merged
```

```
Wheat.dat$res <- residuals(current.asr, type = "stdCond")  
Wheat.dat$fit <- fitted(current.asr)
```

Do diagnostic checking

Do residuals-versus-fitted values plot

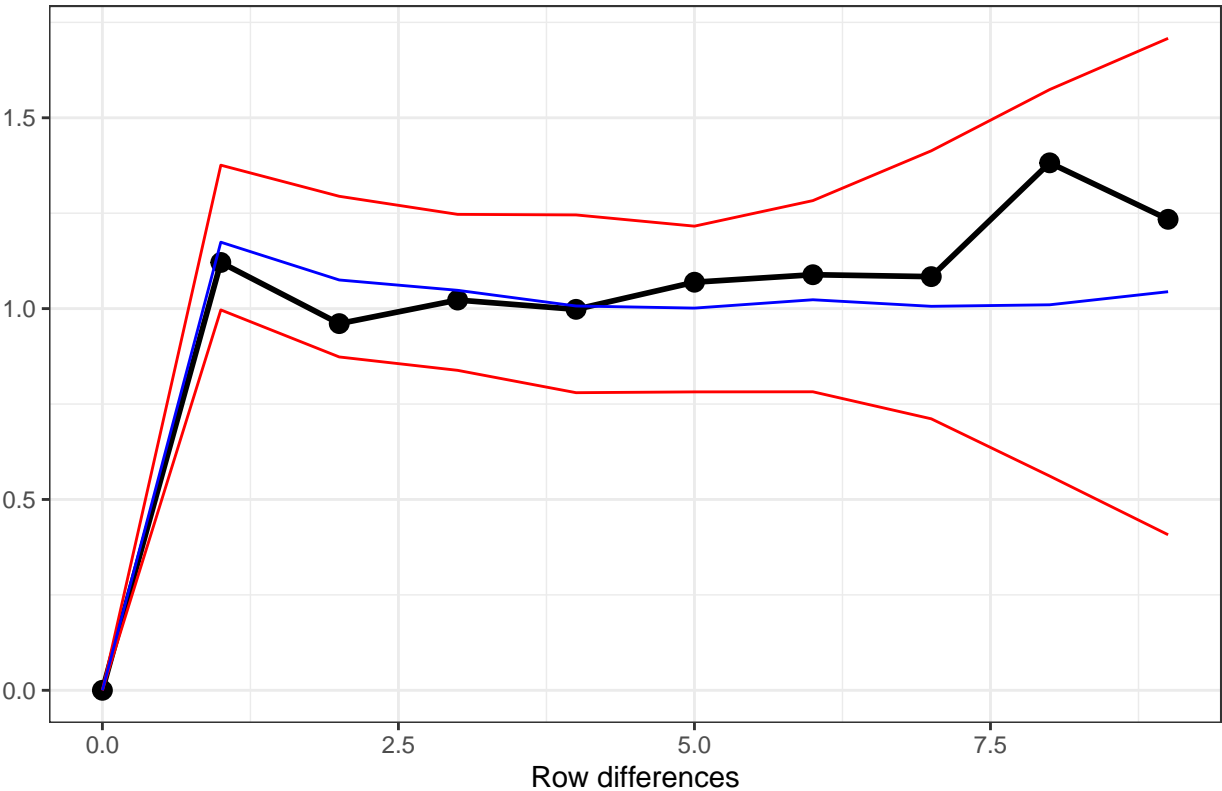
```
with(Wheat.dat, plot(fit, res))
```



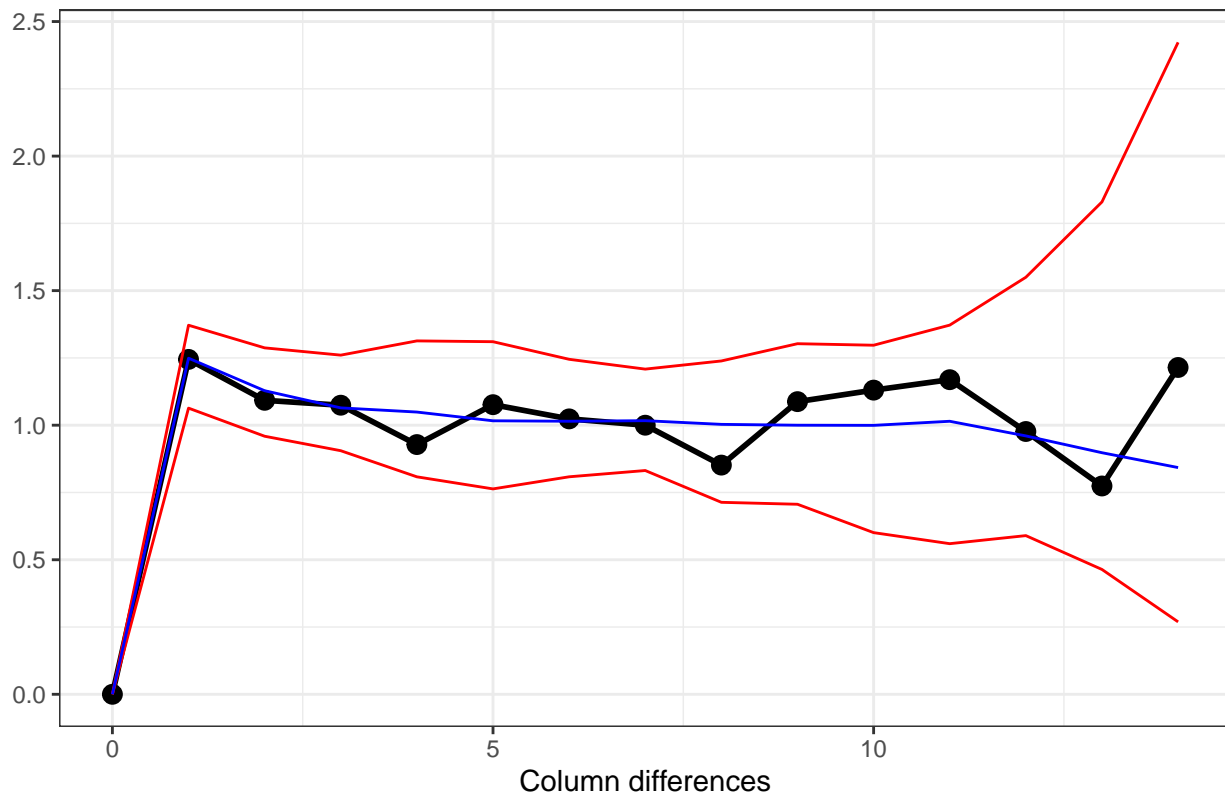
Plot variofaces

```
variofaces(current.asr, V=NULL, units="addtores",  
            maxiter=50, update = FALSE,  
            ncores = parallel::detectCores())
```

Variogram face of Standardized conditional residuals for Row



Variogram face of Standardized conditional residuals for Column



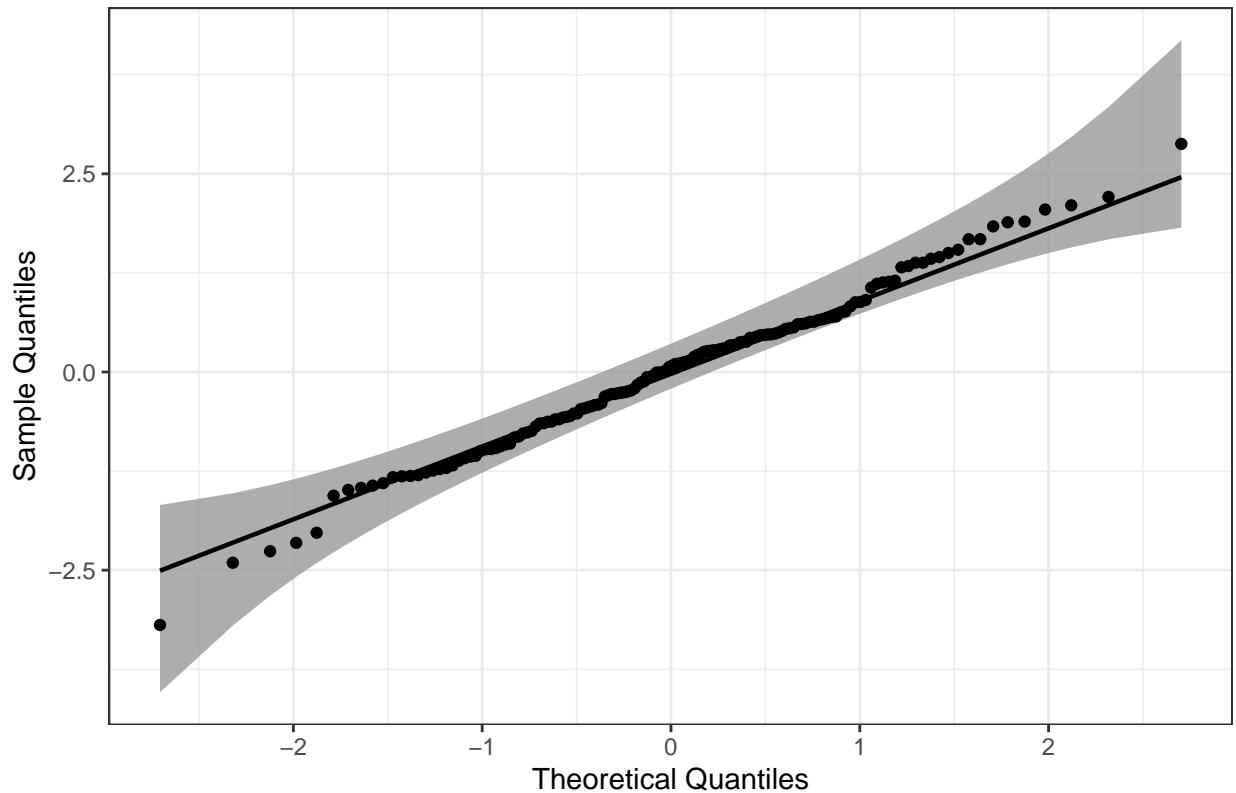
The variofaces are the lag 1 plots of the sample semivariogram with simulated confidence envelopes (Stefanova et al., 2009).

Plot normal quantile plot

The plot is obtained using the `ggplot` function with extensions available from the `qqplotr` package (Almeida et al., 2023).

```
ggplot(data = Wheat.dat, mapping = aes(sample = res)) +  
  stat_qq_band(bandType = "ts") + stat_qq_line() + stat_qq_point() +  
  labs(x = "Theoretical Quantiles", y = "Sample Quantiles",  
       title = "Normal probability plot") +  
  theme(plot.title = element_text(size = 12, face = "bold")) + theme_bw()
```

Normal probability plot



4. Prediction production and presentation

Get Variety predictions and all pairwise prediction differences and p-values

```
Var.diffs <- predictPlus(classify = "Variety",
                        asreml.obj=current.asr,
                        error.intervals="halfLeast",
                        wald.tab=current.asrt$wald.tab,
                        sortFactor = "Variety",
                        tables = "predictions")
```

```
## Notice : Spline design points closer than .001400 have been merged
## Notice : Spline design points closer than .000900 have been merged
##
##
## #### Predictions for yield from Variety
##
##
## Notes:
## - The predictions are obtained by averaging across the hypertable
##   calculated from model terms constructed solely from factors in
##   the averaging and classify sets.
```



```

## - Use 'average' to move ignored factors into the averaging set.
## - spl(cRow) evaluated at average value of 0.00000
## - spl(cColumn) evaluated at average value of 0.00000
## - The simple averaging set: Rep
##
##   Variety predicted.value standard.error upper.halfLeastSignificant.limit
## 1      10      1196.214      64.11316      1255.028
## 2       9      1266.442      69.62176      1325.255
## 3      16      1268.206      74.01873      1327.020
## 4       1      1273.794      69.30592      1332.608
## 5      14      1310.806      70.75661      1369.620
## 6      23      1329.114      73.70238      1387.928
## 7      11      1340.668      75.07426      1399.481
## 8       4      1406.408      76.83336      1465.222
## 9       3      1408.543      71.85868      1467.356
## 10      7      1414.471      72.23082      1473.284
## 11     12      1423.303      71.18629      1482.117
## 12      8      1445.533      75.37805      1504.347
## 13      5      1480.687      70.31499      1539.500
## 14     15      1485.249      74.28025      1544.063
## 15     17      1495.212      71.09930      1554.026
## 16     21      1512.767      72.53109      1571.580
## 17      6      1520.841      72.50721      1579.654
## 18     24      1563.649      65.33308      1622.463
## 19     18      1568.887      71.06200      1627.700
## 20     25      1579.929      70.52509      1638.743
## 21      2      1585.398      74.96623      1644.211
## 22     22      1633.080      71.38265      1691.894
## 23     13      1637.119      66.24775      1695.932
## 24     19      1651.533      74.93686      1710.347
## 25     20      1657.612      68.65452      1716.426
##   lower.halfLeastSignificant.limit est.status
## 1      1137.400 Estimable
## 2      1207.628 Estimable
## 3      1209.393 Estimable
## 4      1214.980 Estimable
## 5      1251.993 Estimable
## 6      1270.300 Estimable
## 7      1281.854 Estimable
## 8      1347.594 Estimable
## 9      1349.729 Estimable
## 10     1355.657 Estimable
## 11     1364.490 Estimable
## 12     1386.720 Estimable
## 13     1421.873 Estimable
## 14     1426.435 Estimable
## 15     1436.399 Estimable
## 16     1453.953 Estimable
## 17     1462.027 Estimable
## 18     1504.836 Estimable
## 19     1510.073 Estimable
## 20     1521.115 Estimable
## 21     1526.584 Estimable
## 22     1574.266 Estimable

```

```
## 23                1578.305  Estimable
## 24                1592.719  Estimable
## 25                1598.798  Estimable
##
##
## LSD values
##
## minimum LSD =  109.6008
##
## mean LSD =  117.6273
##
## maximum LSD =  126.3422
##
## (sed range / mean sed =  0.142 )
```

We have set `error.intervals` to `halfLeast` so that the limits for each prediction $\pm(0.5 \text{ LSD})$ are calculated. When these are plotted overlapping error bars indicate predictions that are not significant, while those that do not overlap are significantly different (Snee, 1981).

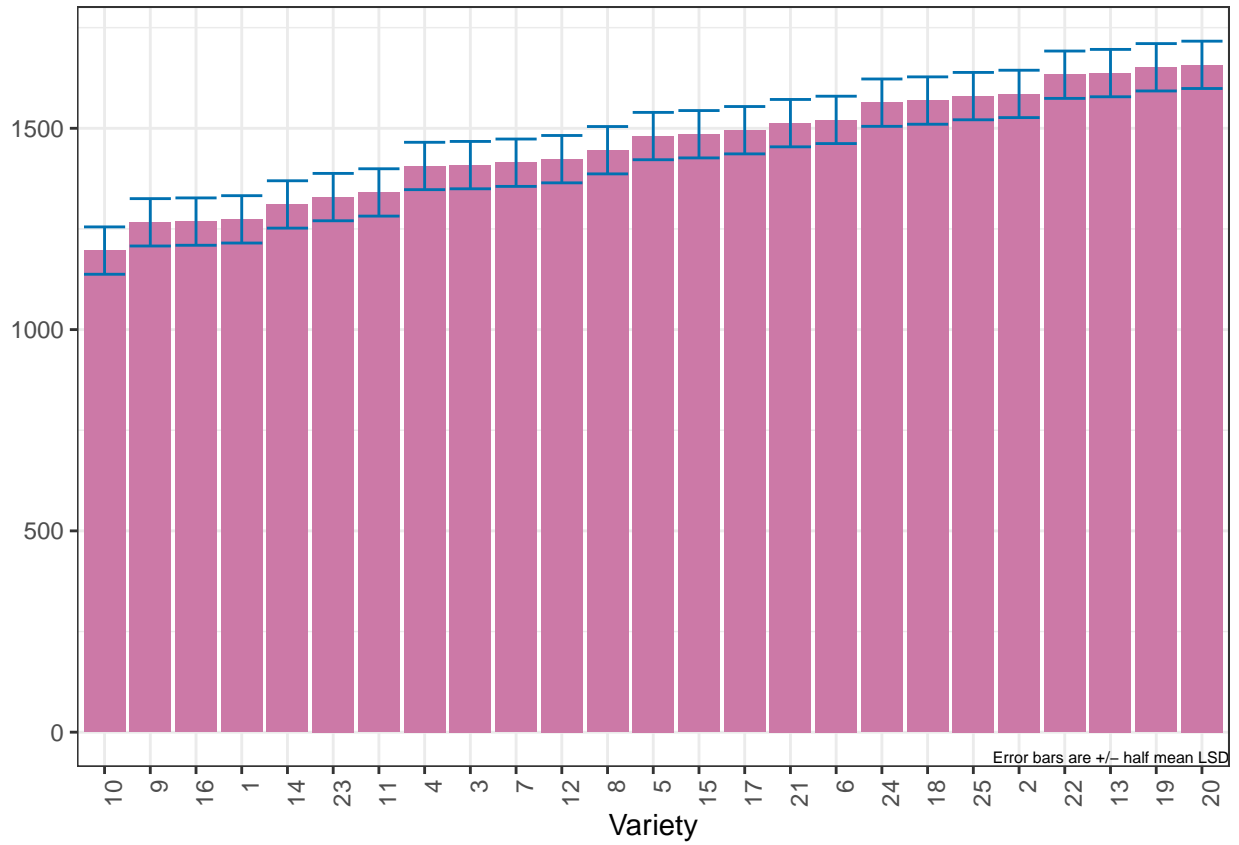
Also set was `sortFactor`, so that the results would be ordered for the values of the predictions for Variety.

The function `predictPlus` returns an `alldiffs` object, a list consisting of the following components:

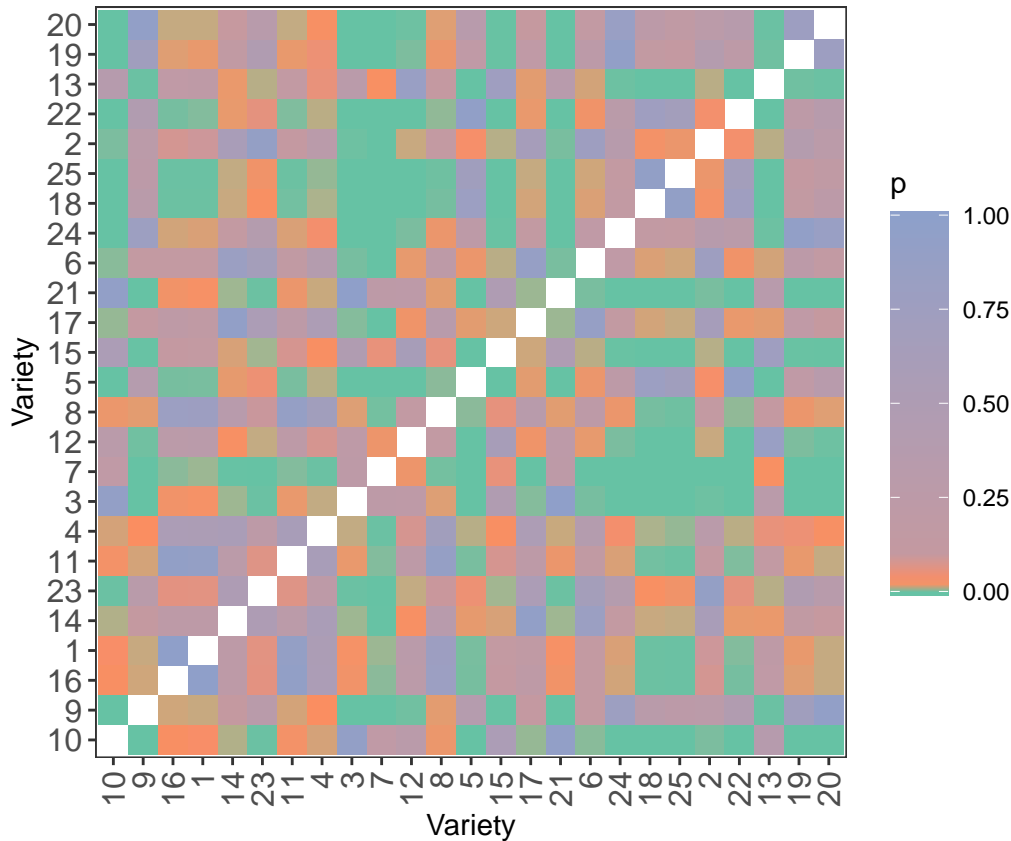
- `predictions`: the predictions, their standard errors and error intervals;
- `vcov`: the variance matrix of the predictions;
- `differences`: all pairwise differences between the predictions,
- `p.differences`: p-values for all pairwise differences between the predictions;
- `sed`: the standard errors of all pairwise differences between the predictions;
- `LSD`: the mean, minimum and maximum of the LSDs.

Plot the Variety predictions, with halfLSD intervals, and the p-values

```
plotPredictions(Var.diffs$predictions,
  classify = "Variety", y = "predicted.value",
  error.intervals = "half")
```



```
plotPvalues(Var.diffs)
```



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