

# Package ‘dml’

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**Title** Distance Metric Learning in R

**Description** The state-of-the-art algorithms for distance metric learning, including global and local methods such as Relevant Component Analysis, Discriminative Component Analysis, Local Fisher Discriminant Analysis, etc. These distance metric learning methods are widely applied in feature extraction, dimensionality reduction, clustering, classification, information retrieval, and computer vision problems.

**Depends** MASS

**Imports** lfda

**Suggests** testthat

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**URL** <https://github.com/terrytangyuan/dml>

**BugReports** <https://github.com/terrytangyuan/dml/issues>

**NeedsCompilation** no

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dca

*Discriminative Component Analysis***Description**

Performs discriminative component analysis on the given data.

**Usage**

```
dca(data, chunks, neglinks, useD = NULL)
```

**Arguments**

data	n * d data matrix. n is the number of data points, d is the dimension of the data. Each data point is a row in the matrix.
chunks	length n vector describing the chunklets: -1 in the i th place means point i doesn't belong to any chunklet; integer j in place i means point i belongs to chunklet j. The chunklets indexes should be 1:(number of chunklets).
neglinks	s * s symmetric matrix describing the negative relationship between all the s chunklets. For the element $neglinks_{ij}$ : $neglinks_{ij} = 1$ means chunklet i and chunklet j have negative constraint(s); $neglinks_{ij} = 0$ means chunklet i and chunklet j don't have negative constraints or we don't have information about that.
useD	Integer. Optional. When not given, DCA is done in the original dimension and B is full rank. When useD is given, DCA is preceded by constraints based LDA which reduces the dimension to useD. B in this case is of rank useD.

**Details**

Put DCA function details here.

**Value**

list of the DCA results:

B	DCA suggested Mahalanobis matrix
DCA	DCA suggested transformation of the data. The dimension is (original data dimension) * (useD)
newData	DCA transformed data

For every two original data points (x1, x2) in newData (y1, y2):

$$(x2 - x1)' * B * (x2 - x1) = \|(x2 - x1) * A\|^2 = \|y2 - y1\|^2$$

**Note**

Put some note here.

**Author(s)**

Xiao Nan <<http://www.road2stat.com>>

**References**

Steven C.H. Hoi, W. Liu, M.R. Lyu and W.Y. Ma (2006). Learning Distance Metrics with Contextual Constraints for Image Retrieval. *Proceedings IEEE Conference on Computer Vision and Pattern Recognition (CVPR2006)*.

**Examples**

```
## Not run:
set.seed(123)
require(MASS) # generate synthetic Gaussian data
k = 100       # sample size of each class
n = 3        # specify how many class
N = k * n    # total sample number
x1 = mvrnorm(k, mu = c(-10, 6), matrix(c(10, 4, 4, 10), ncol = 2))
x2 = mvrnorm(k, mu = c(0, 0), matrix(c(10, 4, 4, 10), ncol = 2))
x3 = mvrnorm(k, mu = c(10, -6), matrix(c(10, 4, 4, 10), ncol = 2))
data = as.data.frame(rbind(x1, x2, x3))
# The fully labeled data set with 3 classes
plot(data$V1, data$V2, bg = c("#E41A1C", "#377EB8", "#4DAF4A")[gl(n, k)],
      pch = c(rep(22, k), rep(21, k), rep(25, k)))
Sys.sleep(3)
# Same data unlabeled; clearly the classes' structure is less evident
plot(x$V1, x$V2)
Sys.sleep(3)

chunk1 = sample(1:100, 5)
chunk2 = sample(setdiff(1:100, chunk1), 5)
chunk3 = sample(101:200, 5)
chunk4 = sample(setdiff(101:200, chunk3), 5)
chunk5 = sample(201:300, 5)
chks = list(chunk1, chunk2, chunk3, chunk4, chunk5)
chunks = rep(-1, 300)
# positive samples in the chunks
for (i in 1:5) {
  for (j in chks[[i]]) {
    chunks[j] = i
  }
}

# define the negative constrains between chunks
neglinks = matrix(c(
0, 0, 1, 1, 1,
0, 0, 1, 1, 1,
1, 1, 0, 0, 0,
1, 1, 0, 0, 1,
1, 1, 1, 1, 0),
ncol = 5, byrow = TRUE)
```

```
dcaData = dca(data = data, chunks = chunks, neglinks = neglinks)$newData
# plot DCA transformed data
plot(dcaData[, 1], dcaData[, 2], bg = c("#E41A1C", "#377EB8", "#4DAF4A")[gl(n, k)],
      pch = c(rep(22, k), rep(21, k), rep(25, k)),
      xlim = c(-15, 15), ylim = c(-15, 15))

## End(Not run)
```

---

GdmDiag

*Global Distance Metric Learning*


---

### Description

Performs Global Distance Metric Learning (GDM) on the given data, learning a diagonal matrix.

### Usage

```
GdmDiag(data, simi, dism, C0 = 1, threshold = 0.001)
```

### Arguments

data	n * d data matrix. n is the number of data points, d is the dimension of the data. Each data point is a row in the matrix.
simi	n * 2 matrix describing the similar constrains. Each row of matrix is serial number of a similar pair in the original data. For example, pair(1, 3) represents the first observation is similar the 3th observation in the original data.
dism	n * 2 matrix describing the dissimilar constrains as simi. Each row of matrix is serial number of a dissimilar pair in the original data.
C0	numeric, the bound of similar constrains.
threshold	numeric, the threshold of stopping the learning iteration.

### Details

Put GdmDiag function details here.

### Value

list of the GdmDiag results:

newData	GdmDiag transformed data
diagonalA	suggested Mahalanobis matrix
dm1A	matrix to transform data, square root of diagonalA
error	the precision of obtained distance metric by Newton-Raphson optimization

For every two original data points (x1, x2) in newData (y1, y2):

$$(x2 - x1)' * A * (x2 - x1) = \|(x2 - x1) * B\|^2 = \|y2 - y1\|^2$$

**Note**

Be sure to check whether the dimension of original data and constrains' format are valid for the function.

**Author(s)**

Gao Tao <<http://www.gaotao.name>>

**References**

Steven C.H. Hoi, W. Liu, M.R. Lyu and W.Y. Ma (2003). Distance metric learning, with application to clustering with side-information.

**Examples**

```
## Not run:
set.seed(602)
library(MASS)
library(scatterplot3d)

# generate simulated Gaussian data
k = 100
m <- matrix(c(1, 0.5, 1, 0.5, 2, -1, 1, -1, 3), nrow = 3, byrow = T)
x1 <- mvrnorm(k, mu = c(1, 1, 1), Sigma = m)
x2 <- mvrnorm(k, mu = c(-1, 0, 0), Sigma = m)
data <- rbind(x1, x2)

# define similar constrains
simi <- rbind(t(combn(1:k, 2)), t(combn((k+1):(2*k), 2)))

temp <- as.data.frame(t(simi))
tol <- as.data.frame(combn(1:(2*k), 2))

# define dissimilar constrains
dism <- t(as.matrix(tol[!tol %in% simi]))

# transform data using GdmDiag
result <- GdmDiag(data, simi, dism)
newData <- result$newData

# plot original data
color <- gl(2, k, labels = c("red", "blue"))
par(mfrow = c(2, 1), mar = rep(0, 4) + 0.1)
scatterplot3d(data, color = color, cex.symbols = 0.6,
  xlim = range(data[, 1], newData[, 1]),
  ylim = range(data[, 2], newData[, 2]),
  zlim = range(data[, 3], newData[, 3]),
  main = "Original Data")

# plot GdmDiag transformed data
scatterplot3d(newData, color = color, cex.symbols = 0.6,
  xlim = range(data[, 1], newData[, 1]),
  ylim = range(data[, 2], newData[, 2]),
  zlim = range(data[, 3], newData[, 3]),
```

```

    main = "Transformed Data")
## End(Not run)

```

---

GdmFull

*Global Distance Metric Learning*


---

### Description

Performs Global Distance Metric Learning (GDM) on the given data, learning a full matrix.

### Usage

```
GdmFull(data, simi, dism, maxiter = 100)
```

### Arguments

data	n * d data matrix. n is the number of data points, d is the dimension of the data. Each data point is a row in the matrix.
simi	n * 2 matrix describing the similar constrains. Each row of matrix is serial number of a similar pair in the original data. For example, pair(1, 3) represents the first observation is similar the 3th observation in the original data.
dism	n * 2 matrix describing the dissimilar constrains as simi. Each row of matrix is serial number of a dissimilar pair in the original data.
maxiter	numeric, the number of iteration.

### Details

Put GdmFull function details here.

### Value

list of the GdmDiag results:

newData	GdmDiag transformed data
fullA	suggested Mahalanobis matrix
dm1A	matrix to transform data, square root of diagonalA
converged	whether the iteration-projection optimization is converged or not

For every two original data points (x1, x2) in newData (y1, y2):

$$(x2 - x1)' * A * (x2 - x1) = \|(x2 - x1) * B\|^2 = \|y2 - y1\|^2$$

### Note

Be sure to check whether the dimension of original data and constrains' format are valid for the function.

**Author(s)**

Gao Tao <<http://www.gaotao.name>>

**References**

Steven C.H. Hoi, W. Liu, M.R. Lyu and W.Y. Ma (2003). Distance metric learning, with application to clustering with side-information.

**Examples**

```
## Not run:
set.seed(123)
library(MASS)
library(scatterplot3d)

# generate simulated Gaussian data
k = 100
m <- matrix(c(1, 0.5, 1, 0.5, 2, -1, 1, -1, 3), nrow = 3, byrow = T)
x1 <- mvrnorm(k, mu = c(1, 1, 1), Sigma = m)
x2 <- mvrnorm(k, mu = c(-1, 0, 0), Sigma = m)
data <- rbind(x1, x2)

# define similar constrains
simi <- rbind(t(combn(1:k, 2)), t(combn((k+1):(2*k), 2)))

temp <- as.data.frame(t(simi))
tol <- as.data.frame(combn(1:(2*k), 2))

# define dissimilar constrains
dism <- t(as.matrix(tol[!tol %in% simi]))

# transform data using GdmFull
result <- GdmFull(data, simi, dism)
newData <- result$newData
# plot original data
color <- gl(2, k, labels = c("red", "blue"))
par(mfrow = c(2, 1), mar = rep(0, 4) + 0.1)
scatterplot3d(data, color = color, cex.symbols = 0.6,
  xlim = range(data[, 1], newData[, 1]),
  ylim = range(data[, 2], newData[, 2]),
  zlim = range(data[, 3], newData[, 3]),
  main = "Original Data")
# plot GdmFull transformed data
scatterplot3d(newData, color = color, cex.symbols = 0.6,
  xlim = range(data[, 1], newData[, 1]),
  ylim = range(data[, 2], newData[, 2]),
  zlim = range(data[, 3], newData[, 3]),
  main = "Transformed Data")

## End(Not run)
```

---

rca *Relevant Component Analysis*

---

**Description**

Performs relevant component analysis on the given data.

**Usage**

rca(x, chunks)

**Arguments**

x	matrix or data frame of original data. Each row is a feature vector of a data instance.
chunks	list of k numerical vectors. Each vector represents a chunklet, the elements in the vectors indicate where the samples locate in x. See examples for more information.

**Details**

The RCA function takes a data set and a set of positive constraints as arguments and returns a linear transformation of the data space into better representation, alternatively, a Mahalanobis metric over the data space.

Relevant component analysis consists of three steps:

1. locate the test point
2. compute the distances between the test points
3. find  $k$  shortest distances and the bla

The new representation is known to be optimal in an information theoretic sense under a constraint of keeping equivalent data points close to each other.

**Value**

list of the RCA results:

B	The RCA suggested Mahalanobis matrix. Distances between data points $x_1$ , $x_2$ should be computed by $(x_2 - x_1)' * B * (x_2 - x_1)$
A	The RCA suggested transformation of the data. The data should be transformed by $A * data$
newX	The data after the RCA transformation (A). $newData = A * data$

The three returned argument are just different forms of the same output. If one is interested in a Mahalanobis metric over the original data space, the first argument is all she/he needs. If a transformation into another space (where one can use the Euclidean metric) is preferred, the second returned argument is sufficient. Using A and B is equivalent in the following sense:

if  $y_1 = A * x_1$ ,  $y_2 = A * x_2$  then  $(x_2 - x_1)' * B * (x_2 - x_1) = (y_2 - y_1)' * (y_2 - y_1)$



**Note**

Note that any different sets of instances (chunklets), e.g. 1, 3, 7 and 4, 6, might belong to the same class and might belong to different classes.

**Author(s)**

Xiao Nan <<http://www.road2stat.com>>

**References**

Aharon Bar-Hillel, Tomer Hertz, Noam Shental, and Daphna Weinshall (2003). Learning Distance Functions using Equivalence Relations. *Proceedings of 20th International Conference on Machine Learning (ICML2003)*.

**See Also**

See [dca](#) for exploiting negative constrains.

**Examples**

```
## Not run:
set.seed(1234)
require(MASS) # generate synthetic Gaussian data
k = 100       # sample size of each class
n = 3        # specify how many class
N = k * n    # total sample number
x1 = mvrnorm(k, mu = c(-10, 6), matrix(c(10, 4, 4, 10), ncol = 2))
x2 = mvrnorm(k, mu = c(0, 0), matrix(c(10, 4, 4, 10), ncol = 2))
x3 = mvrnorm(k, mu = c(10, -6), matrix(c(10, 4, 4, 10), ncol = 2))
x = as.data.frame(rbind(x1, x2, x3))
x$V3 = gl(n, k)

# The fully labeled data set with 3 classes
plot(x$V1, x$V2, bg = c("#E41A1C", "#377EB8", "#4DAF4A")[x$V3],
      pch = c(rep(22, k), rep(21, k), rep(25, k)))
Sys.sleep(3)

# Same data unlabeled; clearly the classes' structure is less evident
plot(x$V1, x$V2)
Sys.sleep(3)

chunk1 = sample(1:100, 5)
chunk2 = sample(setdiff(1:100, chunk1), 5)
chunk3 = sample(101:200, 5)
chunk4 = sample(setdiff(101:200, chunk3), 5)
chunk5 = sample(201:300, 5)
chks = x[c(chunk1, chunk2, chunk3, chunk4, chunk5), ]
chunks = list(chunk1, chunk2, chunk3, chunk4, chunk5)

# The chunklets provided to the RCA algorithm
plot(chks$V1, chks$V2, col = rep(c("#E41A1C", "#377EB8",
```

```
"#4DAF4A", "#984EA3", "#FF7F00"), each = 5),  
  pch = rep(0:4, each = 5), ylim = c(-15, 15))  
Sys.sleep(3)  
  
# Whitening transformation applied to the chunklets  
chkTransformed = as.matrix(chks[ , 1:2]) %*% rca(x[ , 1:2], chunks)$A  
  
plot(chkTransformed[ , 1], chkTransformed[ , 2], col = rep(c(  
  "#E41A1C", "#377EB8", "#4DAF4A", "#984EA3", "#FF7F00"), each = 5),  
  pch = rep(0:4, each = 5), ylim = c(-15, 15))  
Sys.sleep(3)  
  
# The origin data after applying the RCA transformation  
plot(rca(x[ , 1:2], chunks)$newX[ , 1], rca(x[ , 1:2], chunks)$newX[ , 2],  
  bg = c("#E41A1C", "#377EB8", "#4DAF4A")[gl(n, k)],  
  pch = c(rep(22, k), rep(21, k), rep(25, k)))  
  
# The RCA suggested transformation of the data, dimensionality reduced  
rca(x[ , 1:2], chunks)$A  
  
# The RCA suggested Mahalanobis matrix  
rca(x[ , 1:2], chunks)$B  
  
## End(Not run)
```

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