

# Package ‘PrevMap’

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**Type** Package

**Title** Geostatistical Modelling of Spatially Referenced Prevalence Data

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**Imports** splancs, lme4, truncnorm, methods, numDeriv

**Depends** maxLik, raster, pdist, Matrix

**Description** Provides functions for both likelihood-based and Bayesian analysis of spatially referenced prevalence data. For a tutorial on the use of the R package, see Giorgi and Diggle (2017) <[doi:10.18637/jss.v078.i08](https://doi.org/10.18637/jss.v078.i08)>.

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<code>adjust.sigma2</code>	<i>Adjustment factor for the variance of the convolution of Gaussian noise</i>
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### Description

This function computes the multiplicative constant used to adjust the value of `sigma2` in the low-rank approximation of a Gaussian process.

### Usage

```
adjust.sigma2(knots.dist, phi, kappa)
```

### Arguments

<code>knots.dist</code>	a matrix of the distances between the observed coordinates and the spatial knots.
<code>phi</code>	scale parameter of the Matern covariance function.
<code>kappa</code>	shape parameter of the Matern covariance function.

### Details

Let  $U$  denote the  $n$  by  $m$  matrix of the distances between the  $n$  observed coordinates and  $m$  pre-defined spatial knots. This function computes the following quantity

$$\frac{1}{n} \sum_{i=1}^n \sum_{j=1}^m K(u_{ij}; \phi, \kappa)^2,$$

where  $K(\cdot; \phi, \kappa)$  is the Matern kernel (see [matern.kernel](#)) and  $u_{ij}$  is the distance between the  $i$ -th sampled location and the  $j$ -th spatial knot.

### Value

A value corresponding to the adjustment factor for `sigma2`.

### Author(s)

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### See Also

[matern.kernel](#), [pdist](#).

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autocor.plot

*Plot of the autocorrelgram for posterior samples*


---

**Description**

Plots the autocorrelogram for the posterior samples of the model parameters and spatial random effects.

**Usage**

```
autocor.plot(object, param, component.beta = NULL, component.S = NULL)
```

**Arguments**

object	an object of class 'Bayes.PrevMap'.
param	a character indicating for which component of the model the autocorrelation plot is required: param="beta" for the regression coefficients; param="sigma2" for the variance of the spatial random effect; param="phi" for the scale parameter of the Matern correlation function; param="tau2" for the variance of the nugget effect; param="S" for the spatial random effect.
component.beta	if param="beta", component.beta is a numeric value indicating the component of the regression coefficients; default is NULL.
component.S	if param="S", component.S can be a numeric value indicating the component of the spatial random effect, or set equal to "all" if the autocorrelgram should be plotted for all the components. Default is NULL.

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binary.probit.Bayes

*Bayesian estimation for the two-levels binary probit model*


---

**Description**

This function performs Bayesian estimation for a geostatistical binary probit model. It also allows to specify a two-levels model so as to include individual-level and household-level (or any other unit comprising a group of individuals, e.g. village, school, compound, etc...) variables.

**Usage**

```
binary.probit.Bayes(
  formula,
  coords,
  data,
  ID.coords,
  control.prior,
  control.mcmc,
  kappa,
  low.rank = FALSE,
  knots = NULL,
  messages = TRUE
)
```

**Arguments**

formula	an object of class <code>formula</code> (or one that can be coerced to that class): a symbolic description of the model to be fitted.
coords	an object of class <code>formula</code> indicating the geographic coordinates.
data	a data frame containing the variables in the model.
ID.coords	vector of ID values for the unique set of spatial coordinates obtained from <code>create.ID.coords</code> . These must be provided in order to specify spatial random effects at household-level. <b>Warning:</b> the household coordinates must all be distinct otherwise see <code>jitterDupCoords</code> . Default is NULL.
control.prior	output from <code>control.prior</code> .
control.mcmc	output from <code>control.mcmc.Bayes</code> .
kappa	value for the shape parameter of the Matern covariance function.
low.rank	logical; if <code>low.rank=TRUE</code> a low-rank approximation is required. Default is <code>low.rank=FALSE</code> .
knots	if <code>low.rank=TRUE</code> , <code>knots</code> is a matrix of spatial knots used in the low-rank approximation. Default is <code>knots=NULL</code> .
messages	logical; if <code>messages=TRUE</code> then status messages are printed on the screen (or output device) while the function is running. Default is <code>messages=TRUE</code> .

**Details**

This function performs Bayesian estimation for the parameters of the geostatistical binary probit model. Let  $i$  and  $j$  denote the indices of the  $i$ -th household and  $j$ -th individual within that household. The response variable  $Y_{ij}$  is a binary indicator taking value 1 if the individual has been tested positive for the disease of interest and 0 otherwise. Conditionally on a zero-mean stationary Gaussian process  $S(x_i)$ ,  $Y_{ij}$  are mutually independent Bernoulli variables with probit link function  $\Phi^{-1}(\cdot)$ , i.e.

$$\Phi^{-1}(p_{ij}) = d'_{ij}\beta + S(x_i),$$

where  $d_{ij}$  is a vector of covariates, both at individual- and household-level, with associated regression coefficients  $\beta$ . The Gaussian process  $S(x)$  has isotropic Matern covariance function (see `matern`) with variance `sigma2`, scale parameter `phi` and shape parameter `kappa`.

**Priors definition.** Priors can be defined through the function `control.prior`. The hierarchical structure of the priors is the following. Let  $\theta$  be the vector of the covariance parameters `c(sigma2, phi)`; each component of  $\theta$  has independent priors that can be freely defined by the user. However, in `control.prior` uniform and log-normal priors are also available as default priors for each of the covariance parameters. The vector of regression coefficients `beta` has a multivariate Gaussian prior with mean `beta.mean` and covariance matrix `beta.covar`.

**Updating regression coefficients and random effects using auxiliary variables.** To update  $\beta$  and  $S(x_i)$ , we use an auxiliary variable technique based on Rue and Held (2005). Let  $V_{ij}$  denote a set of random variables that conditionally on  $\beta$  and  $S(x_i)$ , are mutually independent Gaussian with mean  $d'_{ij}\beta + S(x_i)$  and unit variance. Then,  $Y_{ij} = 1$  if  $V_{ij} > 0$  and  $Y_{ij} = 0$  otherwise. Using this representation of the model, we use a Gibbs sampler to simulate from the full conditionals of  $\beta$ ,  $S(x_i)$  and  $V_{ij}$ . See Section 4.3 of Rue and Held (2005) for more details.

**Updating the covariance parameters with a Metropolis-Hastings algorithm.** In the MCMC algorithm implemented in `binary.probit.Bayes`, the transformed parameters

$$(\theta_1, \theta_2) = (\log(\sigma^2)/2, \log(\sigma^2/\phi^{2\kappa}))$$

are independently updated using a Metropolis Hastings algorithm. At the  $i$ -th iteration, a new value is proposed for each parameter from a univariate Gaussian distribution with variance  $h_i^2$ . This is tuned using the following adaptive scheme

$$h_i = h_{i-1} + c_1 i^{-c_2} (\alpha_i - 0.45),$$

where  $\alpha_i$  is the acceptance rate at the  $i$ -th iteration, 0.45 is the optimal acceptance rate for a univariate Gaussian distribution, whilst  $c_1 > 0$  and  $0 < c_2 < 1$  are pre-defined constants. The starting values  $h_1$  for each of the parameters  $\theta_1$  and  $\theta_2$  can be set using the function `control.mcmc.Bayes` through the arguments `h.theta1`, `h.theta2` and `h.theta3`. To define values for  $c_1$  and  $c_2$ , see the documentation of `control.mcmc.Bayes`.

**Low-rank approximation.** In the case of very large spatial data-sets, a low-rank approximation of the Gaussian spatial process  $S(x)$  might be computationally beneficial. Let  $(x_1, \dots, x_m)$  and  $(t_1, \dots, t_m)$  denote the set of sampling locations and a grid of spatial knots covering the area of interest, respectively. Then  $S(x)$  is approximated as  $\sum_{i=1}^m K(\|x - t_i\|; \phi, \kappa) U_i$ , where  $U_i$  are zero-mean mutually independent Gaussian variables with variance `sigma2` and  $K(\cdot; \phi, \kappa)$  is the isotropic Matern kernel (see `matern.kernel`). Since the resulting approximation is no longer a stationary process (but only approximately), `sigma2` may take very different values from the actual variance of the Gaussian process to approximate. The function `adjust.sigma2` can then be used to (approximately) explore the range for `sigma2`. For example if the variance of the Gaussian process is 0.5, then an approximate value for `sigma2` is `0.5/const.sigma2`, where `const.sigma2` is the value obtained with `adjust.sigma2`.

## Value

An object of class "Bayes.PrevMap". The function `summary.Bayes.PrevMap` is used to print a summary of the fitted model. The object is a list with the following components:

`estimate`: matrix of the posterior samples of the model parameters.

`S`: matrix of the posterior samples for each component of the random effect.

`const.sigma2`: vector of the values of the multiplicative factor used to adjust the values of `sigma2` in the low-rank approximation.

`y`: binary observations.  
`D`: matrix of covariates.  
`coords`: matrix of the observed sampling locations.  
`kappa`: shape parameter of the Matern function.  
`ID.coords`: set of ID values defined through the argument `ID.coords`.  
`knots`: matrix of spatial knots used in the low-rank approximation.  
`h1`: vector of values taken by the tuning parameter `h.theta1` at each iteration.  
`h2`: vector of values taken by the tuning parameter `h.theta2` at each iteration.  
`call`: the matched call.

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### References

Diggle, P.J., Giorgi, E. (2019). *Model-based Geostatistics for Global Public Health*. CRC/Chapman & Hall.

Giorgi, E., Diggle, P.J. (2017). *PrevMap: an R package for prevalence mapping*. Journal of Statistical Software. 78(8), 1-29. doi: 10.18637/jss.v078.i08

Rue, H., Held, L. (2005). *Gaussian Markov Random Fields: Theory and Applications*. Chapman & Hall, London.

Higdon, D. (1998). *A process-convolution approach to modeling temperatures in the North Atlantic Ocean*. Environmental and Ecological Statistics 5, 173-190.

### See Also

[control.mcmc.Bayes](#), [control.prior.summary.Bayes.PrevMap](#), [matern](#), [matern.kernel](#), [create.ID.coords](#).

---

`binomial.logistic.Bayes`

*Bayesian estimation for the binomial logistic model*

---

### Description

This function performs Bayesian estimation for a geostatistical binomial logistic model.

**Usage**

```

binomial.logistic.Bayes(
  formula,
  units.m,
  coords,
  data,
  ID.coords = NULL,
  control.prior,
  control.mcmc,
  kappa,
  low.rank = FALSE,
  knots = NULL,
  messages = TRUE,
  mesh = NULL,
  SPDE = FALSE
)

```

**Arguments**

formula	an object of class <a href="#">formula</a> (or one that can be coerced to that class): a symbolic description of the model to be fitted.
units.m	an object of class <a href="#">formula</a> indicating the binomial denominators.
coords	an object of class <a href="#">formula</a> indicating the geographic coordinates.
data	a data frame containing the variables in the model.
ID.coords	vector of ID values for the unique set of spatial coordinates obtained from <a href="#">create.ID.coords</a> . These must be provided if, for example, spatial random effects are defined at household level but some of the covariates are at individual level. <b>Warning:</b> the household coordinates must all be distinct otherwise see <a href="#">jitterDupCoords</a> . Default is NULL.
control.prior	output from <a href="#">control.prior</a> .
control.mcmc	output from <a href="#">control.mcmc.Bayes</a> .
kappa	value for the shape parameter of the Matern covariance function.
low.rank	logical; if low.rank=TRUE a low-rank approximation is required. Default is low.rank=FALSE.
knots	if low.rank=TRUE, knots is a matrix of spatial knots used in the low-rank approximation. Default is knots=NULL.
messages	logical; if messages=TRUE then status messages are printed on the screen (or output device) while the function is running. Default is messages=TRUE.
mesh	an object obtained as result of a call to the function <a href="#">inla.mesh.2d</a> .
SPDE	logical; if SPDE=TRUE the SPDE approximation for the Gaussian spatial model is used. Default is SPDE=FALSE.

## Details

This function performs Bayesian estimation for the parameters of the geostatistical binomial logistic model. Conditionally on a zero-mean stationary Gaussian process  $S(x)$  and mutually independent zero-mean Gaussian variables  $Z$  with variance `tau2`, the linear predictor assumes the form

$$\log(p/(1-p)) = d'\beta + S(x) + Z,$$

where  $d$  is a vector of covariates with associated regression coefficients  $\beta$ . The Gaussian process  $S(x)$  has isotropic Matern covariance function (see `matern`) with variance `sigma2`, scale parameter `phi` and shape parameter `kappa`.

**Priors definition.** Priors can be defined through the function `control.prior`. The hierarchical structure of the priors is the following. Let  $\theta$  be the vector of the covariance parameters `c(sigma2, phi, tau2)`; then each component of  $\theta$  has independent priors freely defined by the user. However, in `control.prior` uniform and log-normal priors are also available as default priors for each of the covariance parameters. To remove the nugget effect  $Z$ , no prior should be defined for `tau2`. Conditionally on `sigma2`, the vector of regression coefficients  $\beta$  has a multivariate Gaussian prior with mean `beta.mean` and covariance matrix `sigma2*beta.covar`, while in the low-rank approximation the covariance matrix is simply `beta.covar`.

**Updating the covariance parameters with a Metropolis-Hastings algorithm.** In the MCMC algorithm implemented in `binomial.logistic.Bayes`, the transformed parameters

$$(\theta_1, \theta_2, \theta_3) = (\log(\sigma^2)/2, \log(\sigma^2/\phi^{2\kappa}), \log(\tau^2))$$

are independently updated using a Metropolis Hastings algorithm. At the  $i$ -th iteration, a new value is proposed for each from a univariate Gaussian distribution with variance  $h_i^2$  that is tuned using the following adaptive scheme

$$h_i = h_{i-1} + c_1 i^{-c_2} (\alpha_i - 0.45),$$

where  $\alpha_i$  is the acceptance rate at the  $i$ -th iteration, 0.45 is the optimal acceptance rate for a univariate Gaussian distribution, whilst  $c_1 > 0$  and  $0 < c_2 < 1$  are pre-defined constants. The starting values  $h_1$  for each of the parameters  $\theta_1$ ,  $\theta_2$  and  $\theta_3$  can be set using the function `control.mcmc.Bayes` through the arguments `h.theta1`, `h.theta2` and `h.theta3`. To define values for  $c_1$  and  $c_2$ , see the documentation of `control.mcmc.Bayes`.

**Hamiltonian Monte Carlo.** The MCMC algorithm in `binomial.logistic.Bayes` uses a Hamiltonian Monte Carlo (HMC) procedure to update the random effect  $T = d'\beta + S(x) + Z$ ; see Neal (2011) for an introduction to HMC. HMC makes use of a position vector, say  $t$ , representing the random effect  $T$ , and a momentum vector, say  $q$ , of the same length of the position vector, say  $n$ . Hamiltonian dynamics also have a physical interpretation where the states of the system are described by the position of a puck and its momentum (its mass times its velocity). The Hamiltonian function is then defined as a function of  $t$  and  $q$ , having the form  $H(t, q) = -\log\{f(t|y, \beta, \theta)\} + q'q/2$ , where  $f(t|y, \beta, \theta)$  is the conditional distribution of  $T$  given the data  $y$ , the regression parameters  $\beta$  and covariance parameters  $\theta$ . The system of Hamiltonian equations then defines the evolution of the system in time, which can be used to implement an algorithm for simulation from the posterior distribution of  $T$ . In order to implement the Hamiltonian dynamic on a computer, the Hamiltonian equations must be discretised. The *leapfrog method* is then used for this purpose, where two tuning parameters should be defined: the stepsize  $\epsilon$  and the number of steps  $L$ . These respectively correspond to `epsilon.S.lim` and `L.S.lim` in the `control.mcmc.Bayes` function. However, it is advisable to let *epsilon* and  $L$  take different random values at each iteration of the HCM algorithm so as to account for the different variances amongst the components

of the posterior of  $T$ . This can be done in `control.mcmc.Bayes` by defining `epsilon.S.lim` and `L.S.lim` as vectors of two elements, each of which represents the lower and upper limit of a uniform distribution used to generate values for `epsilon.S.lim` and `L.S.lim`, respectively.

**Using a two-level model to include household-level and individual-level information.** When analysing data from household surveys, some of the available information might be at household-level (e.g. material of house, temperature) and some at individual-level (e.g. age, gender). In this case, the Gaussian spatial process  $S(x)$  and the nugget effect  $Z$  are defined at household-level in order to account for extra-binomial variation between and within households, respectively.

**Low-rank approximation.** In the case of very large spatial data-sets, a low-rank approximation of the Gaussian spatial process  $S(x)$  might be computationally beneficial. Let  $(x_1, \dots, x_m)$  and  $(t_1, \dots, t_m)$  denote the set of sampling locations and a grid of spatial knots covering the area of interest, respectively. Then  $S(x)$  is approximated as  $\sum_{i=1}^m K(\|x - t_i\|; \phi, \kappa) U_i$ , where  $U_i$  are zero-mean mutually independent Gaussian variables with variance `sigma2` and  $K(\cdot; \phi, \kappa)$  is the isotropic Matern kernel (see `matern.kernel`). Since the resulting approximation is no longer a stationary process (but only approximately), `sigma2` may take very different values from the actual variance of the Gaussian process to approximate. The function `adjust.sigma2` can then be used to (approximately) explore the range for `sigma2`. For example if the variance of the Gaussian process is 0.5, then an approximate value for `sigma2` is `0.5/const.sigma2`, where `const.sigma2` is the value obtained with `adjust.sigma2`.

## Value

An object of class "Bayes.PrevMap". The function `summary.Bayes.PrevMap` is used to print a summary of the fitted model. The object is a list with the following components:

`estimate`: matrix of the posterior samples of the model parameters.

`S`: matrix of the posterior samples for each component of the random effect.

`const.sigma2`: vector of the values of the multiplicative factor used to adjust the values of `sigma2` in the low-rank approximation.

`y`: binomial observations.

`units.m`: binomial denominators.

`D`: matrix of covariates.

`coords`: matrix of the observed sampling locations.

`kappa`: shape parameter of the Matern function.

`ID.coords`: set of ID values defined through the argument `ID.coords`.

`knots`: matrix of spatial knots used in the low-rank approximation.

`h1`: vector of values taken by the tuning parameter `h.theta1` at each iteration.

`h2`: vector of values taken by the tuning parameter `h.theta2` at each iteration.

`h3`: vector of values taken by the tuning parameter `h.theta3` at each iteration.

`acc.beta.S`: empirical acceptance rate for the regression coefficients and random effects (only if `SPDE=TRUE`).

`mesh`: the mesh used in the SPDE approximation.

`call`: the matched call.

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**References**

Diggle, P.J., Giorgi, E. (2019). *Model-based Geostatistics for Global Public Health*. CRC/Chapman & Hall.

Giorgi, E., Diggle, P.J. (2017). *PrevMap: an R package for prevalence mapping*. Journal of Statistical Software. 78(8), 1-29. doi: 10.18637/jss.v078.i08

Neal, R. M. (2011) *MCMC using Hamiltonian Dynamics*, In: Handbook of Markov Chain Monte Carlo (Chapter 5), Edited by Steve Brooks, Andrew Gelman, Galin Jones, and Xiao-Li Meng Chapman & Hall / CRC Press.

Higdon, D. (1998). *A process-convolution approach to modeling temperatures in the North Atlantic Ocean*. Environmental and Ecological Statistics 5, 173-190.

**See Also**

[control.mcmc.Bayes](#), [control.prior.summary.Bayes.PrevMap](#), [matern](#), [matern.kernel](#), [create.ID.coords](#).

---

binomial.logistic.MCML

*Monte Carlo Maximum Likelihood estimation for the binomial logistic model*

---

**Description**

This function performs Monte Carlo maximum likelihood (MCML) estimation for the geostatistical binomial logistic model.

**Usage**

```
binomial.logistic.MCML(  
  formula,  
  units.m,  
  coords,  
  times = NULL,  
  data,  
  ID.coords = NULL,  
  par0,  
  control.mcmc,  
  kappa,  
  kappa.t = NULL,  
  sst.model = NULL,  
  fixed.rel.nugget = NULL,  
  start.cov.pars,
```

```

method = "BFGS",
low.rank = FALSE,
SPDE = FALSE,
knots = NULL,
mesh = NULL,
messages = TRUE,
plot.correlogram = TRUE
)

```

### Arguments

formula	an object of class <code>formula</code> (or one that can be coerced to that class): a symbolic description of the model to be fitted.
units.m	an object of class <code>formula</code> indicating the binomial denominators in the data.
coords	an object of class <code>formula</code> indicating the spatial coordinates in the data.
times	an object of class <code>formula</code> indicating the times in the data, used in the spatio-temporal model.
data	a data frame containing the variables in the model.
ID.coords	vector of ID values for the unique set of spatial coordinates obtained from <code>create.ID.coords</code> . These must be provided if, for example, spatial random effects are defined at household level but some of the covariates are at individual level. <b>Warning:</b> the household coordinates must all be distinct otherwise see <code>jitterDupCoords</code> . Default is <code>NULL</code> .
par0	parameters of the importance sampling distribution: these should be given in the following order <code>c(beta, sigma2, phi, tau2)</code> , where <code>beta</code> are the regression coefficients, <code>sigma2</code> is the variance of the Gaussian process, <code>phi</code> is the scale parameter of the spatial correlation and <code>tau2</code> is the variance of the nugget effect (if included in the model).
control.mcmc	output from <code>control.mcmc.MCML</code> .
kappa	fixed value for the shape parameter of the Matern covariance function.
kappa.t	fixed value for the shape parameter of the Matern covariance function in the separable double-Matern spatio-temporal model.
sst.model	a character value that specifies the spatio-temporal correlation function. <ul style="list-style-type: none"> <li>• <code>sst.model="DM"</code> separable double-Matern.</li> <li>• <code>sst.model="GN1"</code> separable correlation functions. Temporal correlation: <math>f(x) = 1/(1 + x/\psi)</math>; Spatial correlation: Matern function.</li> </ul> Default is <code>sst.model=NULL</code> , which is used when a purely spatial model is fitted.
fixed.rel.nugget	fixed value for the relative variance of the nugget effect; <code>fixed.rel.nugget=NULL</code> if this should be included in the estimation. Default is <code>fixed.rel.nugget=NULL</code> .
start.cov.pars	a vector of length two with elements corresponding to the starting values of <code>phi</code> and the relative variance of the nugget effect <code>nu2</code> , respectively, that are used in the optimization algorithm. If <code>nu2</code> is fixed through <code>fixed.rel.nugget</code> , then <code>start.cov.pars</code> represents the starting value for <code>phi</code> only.

method	method of optimization. If method="BFGS" then the <code>maxBFGS</code> function is used; otherwise method="nlminb" to use the <code>nlminb</code> function. Default is method="BFGS".
low.rank	logical; if low.rank=TRUE a low-rank approximation of the Gaussian spatial process is used when fitting the model. Default is low.rank=FALSE.
SPDE	logical; if SPDE=TRUE the SPDE approximation for the Gaussian spatial model is used. Default is SPDE=FALSE.
knots	if low.rank=TRUE, knots is a matrix of spatial knots that are used in the low-rank approximation. Default is knots=NULL.
mesh	an object obtained as result of a call to the function <code>inla.mesh.2d</code> .
messages	logical; if messages=TRUE then status messages are printed on the screen (or output device) while the function is running. Default is messages=TRUE.
plot.correlogram	logical; if plot.correlogram=TRUE the autocorrelation plot of the samples of the random effect is displayed after completion of conditional simulation. Default is plot.correlogram=TRUE.

## Details

This function performs parameter estimation for a geostatistical binomial logistic model. Conditionally on a zero-mean stationary Gaussian process  $S(x)$  and mutually independent zero-mean Gaussian variables  $Z$  with variance  $\tau^2$ , the observations  $y$  are generated from a binomial distribution with probability  $p$  and binomial denominators  $units.m$ . A canonical logistic link is used, thus the linear predictor assumes the form

$$\log(p/(1-p)) = d'\beta + S(x) + Z,$$

where  $d$  is a vector of covariates with associated regression coefficients  $\beta$ . The Gaussian process  $S(x)$  has isotropic Matern covariance function (see `matern`) with variance `sigma2`, scale parameter `phi` and shape parameter `kappa`. In the `binomial.logistic.MCML` function, the shape parameter is treated as fixed. The relative variance of the nugget effect,  $\nu^2 = \tau^2 / \sigma^2$ , can also be fixed through the argument `fixed.rel.nugget`; if `fixed.rel.nugget=NULL`, then the relative variance of the nugget effect is also included in the estimation.

**Monte Carlo Maximum likelihood.** The Monte Carlo maximum likelihood method uses conditional simulation from the distribution of the random effect  $T(x) = d(x)'\beta + S(x) + Z$  given the data  $y$ , in order to approximate the high-dimensional intractable integral given by the likelihood function. The resulting approximation of the likelihood is then maximized by a numerical optimization algorithm which uses analytic expression for computation of the gradient vector and Hessian matrix. The functions used for numerical optimization are `maxBFGS` (method="BFGS"), from the `maxLik` package, and `nlminb` (method="nlminb").

**Using a two-level model to include household-level and individual-level information.** When analysing data from household surveys, some of the available information might be at household-level (e.g. material of house, temperature) and some at individual-level (e.g. age, gender). In this case, the Gaussian spatial process  $S(x)$  and the nugget effect  $Z$  are defined at household-level in order to account for extra-binomial variation between and within households, respectively.

**Low-rank approximation.** In the case of very large spatial data-sets, a low-rank approximation of the Gaussian spatial process  $S(x)$  might be computationally beneficial. Let  $(x_1, \dots, x_m)$  and

$(t_1, \dots, t_m)$  denote the set of sampling locations and a grid of spatial knots covering the area of interest, respectively. Then  $S(x)$  is approximated as  $\sum_{i=1}^m K(\|x - t_i\|; \phi, \kappa) U_i$ , where  $U_i$  are zero-mean mutually independent Gaussian variables with variance `sigma2` and  $K(\cdot; \phi, \kappa)$  is the isotropic Matern kernel (see [matern.kernel](#)). Since the resulting approximation is no longer a stationary process (but only approximately), the parameter `sigma2` is then multiplied by a factor `constant.sigma2` so as to obtain a value that is closer to the actual variance of  $S(x)$ .

## Value

An object of class "PrevMap". The function [summary.PrevMap](#) is used to print a summary of the fitted model. The object is a list with the following components:

`estimate`: estimates of the model parameters; use the function [coef.PrevMap](#) to obtain estimates of covariance parameters on the original scale.

`covariance`: covariance matrix of the MCML estimates.

`log.lik`: maximum value of the log-likelihood.

`y`: binomial observations.

`units.m`: binomial denominators.

`D`: matrix of covariates.

`coords`: matrix of the observed sampling locations.

`method`: method of optimization used.

`ID.coords`: set of ID values defined through the argument `ID.coords`.

`kappa`: fixed value of the shape parameter of the Matern function.

`kappa.t`: fixed value for the shape parameter of the Matern covariance function in the separable double-Matern spatio-temporal model.

`knots`: matrix of the spatial knots used in the low-rank approximation.

`mesh`: the mesh used in the SPDE approximation.

`const.sigma2`: adjustment factor for `sigma2` in the low-rank approximation.

`h`: vector of the values of the tuning parameter at each iteration of the Langevin-Hastings MCMC algorithm; see [Laplace.sampling](#), or [Laplace.sampling.lr](#) if a low-rank approximation is used.

`samples`: matrix of the random effects samples from the importance sampling distribution used to approximate the likelihood function.

`fixed.rel.nugget`: fixed value for the relative variance of the nugget effect.

`call`: the matched call.

## Author(s)

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Peter J. Diggle <[p.diggle@lancaster.ac.uk](mailto:p.diggle@lancaster.ac.uk)>

## References

- Diggle, P.J., Giorgi, E. (2019). *Model-based Geostatistics for Global Public Health*. CRC/Chapman & Hall.
- Giorgi, E., Diggle, P.J. (2017). *PrevMap: an R package for prevalence mapping*. Journal of Statistical Software. 78(8), 1-29. doi: 10.18637/jss.v078.i08
- Christensen, O. F. (2004). *Monte carlo maximum likelihood in model-based geostatistics*. Journal of Computational and Graphical Statistics 13, 702-718.
- Higdon, D. (1998). *A process-convolution approach to modeling temperatures in the North Atlantic Ocean*. Environmental and Ecological Statistics 5, 173-190.

## See Also

[Laplace.sampling](#), [Laplace.sampling.lr](#), [summary.PrevMap](#), [coef.PrevMap](#), [matern](#), [matern.kernel](#), [control.mcmc.MCML](#), [create.ID.coords](#).

---

coef.PrevMap	<i>Extract model coefficients</i>
--------------	-----------------------------------

---

## Description

coef extracts parameters estimates from models fitted with the functions [linear.model.MLE](#) and [binomial.logistic.MCML](#).

## Usage

```
## S3 method for class 'PrevMap'
coef(object, ...)
```

## Arguments

object	an object of class "PrevMap".
...	other arguments.

## Value

coefficients extracted from the model object object.

## Author(s)

Emanuele Giorgi <[e.giorgi@lancaster.ac.uk](mailto:e.giorgi@lancaster.ac.uk)>  
 Peter J. Diggle <[p.diggle@lancaster.ac.uk](mailto:p.diggle@lancaster.ac.uk)>

---

coef.PrevMap.ps	<i>Extract model coefficients from geostatistical linear model with preferentially sampled locations</i>
-----------------	--

---

**Description**

coef extracts parameters estimates from models fitted with the functions [lm.ps.MCML](#).

**Usage**

```
## S3 method for class 'PrevMap.ps'
coef(object, ...)
```

**Arguments**

object	an object of class "PrevMap.ps".
...	other arguments.

**Value**

a list of coefficients extracted from the model in object.

**Author(s)**

Emanuele Giorgi <[e.giorgi@lancaster.ac.uk](mailto:e.giorgi@lancaster.ac.uk)>

---

continuous.sample	<i>Spatially continuous sampling</i>
-------------------	--------------------------------------

---

**Description**

Draws a sample of spatial locations within a spatially continuous polygonal sampling region.

**Usage**

```
continuous.sample(poly, n, delta, k = 0, rho = NULL)
```

**Arguments**

poly	boundary of a polygon.
n	number of events.
delta	minimum permissible distance between any two events in preliminary sample.
k	number of locations in preliminary sample to be replaced by near neighbours of other preliminary sample locations in final sample (must be between 0 and n/2)
rho	maximum distance between close pairs of locations in final sample.

## Details

To draw a sample of size  $n$  from a spatially continuous region  $A$ , with the property that the distance between any two sampled locations is at least  $\delta$ , the following algorithm is used.

- Step 1. Set  $i = 1$  and generate a point  $x_1$  uniformly distributed on  $A$ .
- Step 2. Increase  $i$  by 1, generate a point  $x_i$  uniformly distributed on  $A$  and calculate the minimum,  $d_{\min}$ , of the distances from  $x_i$  to all  $x_j : j < i$ .
- Step 3. If  $d_{\min} \geq \delta$ , increase  $i$  by 1 and return to step 2 if  $i \leq n$ , otherwise stop;
- Step 4. If  $d_{\min} < \delta$ , return to step 2 without increasing  $i$ .

**Sampling close pairs of points.** For some purposes, it is desirable that a spatial sampling scheme include pairs of closely spaced points. In this case, the above algorithm requires the following additional steps to be taken. Let  $k$  be the required number of close pairs. Choose a value  $\rho$  such that a close pair of points will be a pair of points separated by a distance of at most  $\rho$ .

- Step 5. Set  $j = 1$  and draw a random sample of size 2 from the integers  $1, 2, \dots, n$ , say  $(i_1; i_2)$ ;
- Step 6. Replace  $x_{i_1}$  by  $x_{i_2} + u$ , where  $u$  is uniformly distributed on the disc with centre  $x_{i_2}$  and radius  $\rho$ , increase  $i$  by 1 and return to step 5 if  $i \leq k$ , otherwise stop.

## Value

A matrix of dimension  $n$  by 2 containing event locations.

## Author(s)

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

contour.pred.PrevMap *Contour plot of a predicted surface*

---

## Description

plot.pred.PrevMap displays contours of predictions obtained from [spatial.pred.linear.MLE](#), [spatial.pred.linear.Bayes](#), [spatial.pred.binomial.MCML](#) and [spatial.pred.binomial.Bayes](#).

## Usage

```
## S3 method for class 'pred.PrevMap'
contour(x, type = NULL, summary = "predictions", ...)
```

**Arguments**

x	an object of class "pred.PrevMap".
type	a character indicating the type of prediction to display: 'prevalence', 'odds', 'logit' or 'probit'.
summary	character indicating which summary to display: 'predictions', 'quantiles', 'standard.errors' or 'exceedance.prob'; default is 'predictions'. If summary="exceedance.prob", the argument type is ignored.
...	further arguments passed to <a href="#">contour</a> .

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

control.mcmc.Bayes      *Control settings for the MCMC algorithm used for Bayesian inference*

---

**Description**

This function defines the different tuning parameter that are used in the MCMC algorithm for Bayesian inference.

**Usage**

```
control.mcmc.Bayes(
  n.sim,
  burnin,
  thin,
  h.theta1 = 0.01,
  h.theta2 = 0.01,
  h.theta3 = 0.01,
  L.S.lim = NULL,
  epsilon.S.lim = NULL,
  start.beta = "prior mean",
  start.sigma2 = "prior mean",
  start.phi = "prior mean",
  start.S = "prior mean",
  start.nugget = "prior mean",
  c1.h.theta1 = 0.01,
  c2.h.theta1 = 1e-04,
  c1.h.theta2 = 0.01,
  c2.h.theta2 = 1e-04,
  c1.h.theta3 = 0.01,
  c2.h.theta3 = 1e-04,
  linear.model = FALSE,
  binary = FALSE
)
```

**Arguments**

n.sim	total number of simulations.
burnin	initial number of samples to be discarded.
thin	value used to retain only every thin-th sampled value.
h.theta1	starting value of the tuning parameter of the proposal distribution for $\theta_1 = \log(\sigma^2)/2$ . See 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
h.theta2	starting value of the tuning parameter of the proposal distribution for $\theta_2 = \log(\sigma^2/\phi^{2\kappa})$ . See 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
h.theta3	starting value of the tuning parameter of the proposal distribution for $\theta_3 = \log(\tau^2)$ . See 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
L.S.lim	an atomic value or a vector of length 2 that is used to define the number of steps used at each iteration in the Hamiltonian Monte Carlo algorithm to update the spatial random effect; if a single value is provided than the number of steps is kept fixed, otherwise if a vector of length 2 is provided the number of steps is simulated at each iteration as <code>floor(runif(1,L.S.lim[1],L.S.lim[2]+1))</code> .
epsilon.S.lim	an atomic value or a vector of length 2 that is used to define the stepsize used at each iteration in the Hamiltonian Monte Carlo algorithm to update the spatial random effect; if a single value is provided than the stepsize is kept fixed, otherwise if a vector of length 2 is provided the stepsize is simulated at each iteration as <code>runif(1,epsilon.S.lim[1],epsilon.S.lim[2])</code> .
start.beta	starting value for the regression coefficients beta.
start.sigma2	starting value for sigma2.
start.phi	starting value for phi.
start.S	starting value for the spatial random effect.
start.nugget	starting value for the variance of the nugget effect; default is NULL if the nugget effect is not present.
c1.h.theta1	value of $c_1$ used to adaptively tune the variance of the Gaussian proposal for the transformed parameter $\log(\text{sigma2})/2$ ; see 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
c2.h.theta1	value of $c_2$ used to adaptively tune the variance of the Gaussian proposal for the transformed parameter $\log(\text{sigma2})/2$ ; see 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
c1.h.theta2	value of $c_1$ used to adaptively tune the variance of the Gaussian proposal for the transformed parameter $\log(\text{sigma2.curr}/(\text{phi.curr}^{(2*\text{kappa}))})$ ; see 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
c2.h.theta2	value of $c_2$ used to adaptively tune the variance of the Gaussian proposal for the transformed parameter $\log(\text{sigma2.curr}/(\text{phi.curr}^{(2*\text{kappa}))})$ ; see 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
c1.h.theta3	value of $c_1$ used to adaptively tune the variance of the Gaussian proposal for the transformed parameter $\log(\text{tau2})$ ; see 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .

c2.h.theta3	value of $c_2$ used to adaptively tune the variance of the Gaussian proposal for the transformed parameter $\log(\tau_2)$ ; see 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
linear.model	logical; if linear.model=TRUE, the control parameters are set for the geostatistical linear model. Default is linear.model=FALSE.
binary	logical; if binary=TRUE, the control parameters are set the binary geostatistical model. Default is binary=FALSE.

**Value**

an object of class "mcmc.Bayes.PrevMap".

**Author(s)**

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Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

control.mcmc.Bayes.SPDE

*Control settings for the MCMC algorithm used for Bayesian inference using SPDE*

---

**Description**

This function defines the different tuning parameter that are used in the MCMC algorithm for Bayesian inference using a SPDE approximation for the spatial Gaussian process.

**Usage**

```
control.mcmc.Bayes.SPDE(
  n.sim,
  burnin,
  thin,
  h.theta1 = 0.01,
  h.theta2 = 0.01,
  start.beta = "prior mean",
  start.sigma2 = "prior mean",
  start.phi = "prior mean",
  start.S = "prior mean",
  n.iter = 1,
  h = 1,
  c1.h.theta1 = 0.01,
  c2.h.theta1 = 1e-04,
  c1.h.theta2 = 0.01,
  c2.h.theta2 = 1e-04
)
```

**Arguments**

n.sim	total number of simulations.
burnin	initial number of samples to be discarded.
thin	value used to retain only every thin-th sampled value.
h.theta1	starting value of the tuning parameter of the proposal distribution for $\theta_1 = \log(\sigma^2)/2$ . See 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
h.theta2	starting value of the tuning parameter of the proposal distribution for $\theta_2 = \log(\sigma^2/\phi^{2\kappa})$ . See 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
start.beta	starting value for the regression coefficients beta. If not provided the prior mean is used.
start.sigma2	starting value for sigma2. If not provided the prior mean is used.
start.phi	starting value for phi. If not provided the prior mean is used.
start.S	starting value for the spatial random effect. If not provided the prior mean is used.
n.iter	number of iteration of the Newton-Raphson procedure used to compute the mean and covariance matrix of the Gaussian proposal in the MCMC; default is n.iter=1.
h	tuning parameter for the covariance matrix of the Gaussian proposal. Default is h=1.
c1.h.theta1	value of $c_1$ used to adaptively tune the variance of the Gaussian proposal for the transformed parameter $\log(\text{sigma2})/2$ ; see 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
c2.h.theta1	value of $c_2$ used to adaptively tune the variance of the Gaussian proposal for the transformed parameter $\log(\text{sigma2})/2$ ; see 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
c1.h.theta2	value of $c_1$ used to adaptively tune the variance of the Gaussian proposal for the transformed parameter $\log(\text{sigma2.curr}/(\text{phi.curr}^{(2*\text{kappa}))})$ ; see 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .
c2.h.theta2	value of $c_2$ used to adaptively tune the variance of the Gaussian proposal for the transformed parameter $\log(\text{sigma2.curr}/(\text{phi.curr}^{(2*\text{kappa}))})$ ; see 'Details' in <a href="#">binomial.logistic.Bayes</a> or <a href="#">linear.model.Bayes</a> .

**Value**

an object of class "mcmc.Bayes.PrevMap".

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

control.mcmc.MCML	<i>Control settings for the MCMC algorithm used for classical inference on a binomial logistic model</i>
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---

## Description

This function defines the options for the MCMC algorithm used in the Monte Carlo maximum likelihood method.

## Usage

```
control.mcmc.MCML(n.sim, burnin, thin = 1, h = NULL, c1.h = 0.01, c2.h = 1e-04)
```

## Arguments

n.sim	number of simulations.
burnin	length of the burn-in period.
thin	only every thin iterations, a sample is stored; default is thin=1.
h	tuning parameter of the proposal distribution used in the Langevin-Hastings MCMC algorithm (see <a href="#">Laplace.sampling</a> and <a href="#">Laplace.sampling.lr</a> ); default is h=NULL and then set internally as $1.65/n^{(1/6)}$ , where $n$ is the dimension of the random effect.
c1.h	value of $c_1$ used in the adaptive scheme for h; default is c1.h=0.01. See also 'Details' in <a href="#">binomial.logistic.MCML</a>
c2.h	value of $c_2$ used in the adaptive scheme for h; default is c1.h=0.01. See also 'Details' in <a href="#">binomial.logistic.MCML</a>

## Value

A list with processed arguments to be passed to the main function.

## Author(s)

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Peter J. Diggle <[p.diggle@lancaster.ac.uk](mailto:p.diggle@lancaster.ac.uk)>

## Examples

```
control.mcmc <- control.mcmc.MCML(n.sim=1000,burnin=100,thin=1,h=0.05)
str(control.mcmc)
```

---

control.prior	<i>Priors specification</i>
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---

### Description

This function is used to define priors for the model parameters of a Bayesian geostatistical model.

### Usage

```
control.prior(
  beta.mean,
  beta.covar,
  log.prior.sigma2 = NULL,
  log.prior.phi = NULL,
  log.prior.nugget = NULL,
  uniform.sigma2 = NULL,
  log.normal.sigma2 = NULL,
  uniform.phi = NULL,
  log.normal.phi = NULL,
  uniform.nugget = NULL,
  log.normal.nugget = NULL
)
```

### Arguments

beta.mean	mean vector of the Gaussian prior for the regression coefficients.
beta.covar	covariance matrix of the Gaussian prior for the regression coefficients.
log.prior.sigma2	a function corresponding to the log-density of the prior distribution for the variance $\sigma^2$ of the Gaussian process. <b>Warning:</b> if a low-rank approximation is used, then $\sigma^2$ corresponds to the variance of the iid zero-mean Gaussian variables. Default is NULL.
log.prior.phi	a function corresponding to the log-density of the prior distribution for the scale parameter of the Matern correlation function; default is NULL.
log.prior.nugget	optional: a function corresponding to the log-density of the prior distribution for the variance of the nugget effect; default is NULL with no nugget incorporated in the model; default is NULL.
uniform.sigma2	a vector of length two, corresponding to the lower and upper limit of the uniform prior on $\sigma^2$ . Default is NULL.
log.normal.sigma2	a vector of length two, corresponding to the mean and standard deviation of the distribution on the log scale for the log-normal prior on $\sigma^2$ . Default is NULL.
uniform.phi	a vector of length two, corresponding to the lower and upper limit of the uniform prior on $\phi$ . Default is NULL.

- `log.normal.phi` a vector of length two, corresponding to the mean and standard deviation of the distribution on the log scale for the log-normal prior on `phi`. Default is `NULL`.
- `uniform.nugget` a vector of length two, corresponding to the lower and upper limit of the uniform prior on `tau2`. Default is `NULL`.
- `log.normal.nugget`  
a vector of length two, corresponding to the mean and standard deviation of the distribution on the log scale for the log-normal prior on `tau2`. Default is `NULL`.

**Value**

a list corresponding the prior distributions for each model parameter.

**Author(s)**

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Peter J. Diggle <[p.diggle@lancaster.ac.uk](mailto:p.diggle@lancaster.ac.uk)>

**See Also**

See "Priors definition" in the Details section of the [binomial.logistic.Bayes](#) function.

---

<code>control.profile</code>	<i>Auxiliary function for controlling profile log-likelihood in the linear Gaussian model</i>
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---

**Description**

Auxiliary function used by [loglik.linear.model](#). This function defines whether the profile-loglikelihood should be computed or evaluation of the likelihood is required by keeping the other parameters fixed.

**Usage**

```
control.profile(
  phi = NULL,
  rel.nugget = NULL,
  fixed.beta = NULL,
  fixed.sigma2 = NULL,
  fixed.phi = NULL,
  fixed.rel.nugget = NULL
)
```

**Arguments**

<code>phi</code>	a vector of the different values that should be used in the likelihood evaluation for the scale parameter <code>phi</code> , or NULL if a single value is provided either as first argument in <code>start.par</code> (for profile likelihood maximization) or as fixed value in <code>fixed.phi</code> ; default is NULL.
<code>rel.nugget</code>	a vector of the different values that should be used in the likelihood evaluation for the relative variance of the nugget effect <code>nu2</code> , or NULL if a single value is provided either in <code>start.par</code> (for profile likelihood maximization) or as fixed value in <code>fixed.nu2</code> ; default is NULL.
<code>fixed.beta</code>	a vector for the fixed values of the regression coefficients <code>beta</code> , or NULL if profile log-likelihood is to be performed; default is NULL.
<code>fixed.sigma2</code>	value for the fixed variance of the Gaussian process <code>sigma2</code> , or NULL if profile log-likelihood is to be performed; default is NULL.
<code>fixed.phi</code>	value for the fixed scale parameter <code>phi</code> in the Matern function, or NULL if profile log-likelihood is to be performed; default is NULL.
<code>fixed.rel.nugget</code>	value for the fixed relative variance of the nugget effect; <code>fixed.rel.nugget=NULL</code> if profile log-likelihood is to be performed; default is NULL.

**Value**

A list with components named as the arguments.

**Author(s)**

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Peter J. Diggle <[p.diggle@lancaster.ac.uk](mailto:p.diggle@lancaster.ac.uk)>

**See Also**

[loglik.linear.model](#)

---

<code>create.ID.coords</code>	<i>ID spatial coordinates</i>
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---

**Description**

Creates ID values for the unique set of coordinates.

**Usage**

```
create.ID.coords(data, coords)
```

**Arguments**

data            a data frame containing the spatial coordinates.  
coords         an object of class `formula` indicating the geographic coordinates.

**Value**

a vector of integers indicating the corresponding rows in `data` for each distinct coordinate obtained with the `unique` function.

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>  
Peter J. Diggle <p.diggle@lancaster.ac.uk>

**Examples**

```
x1 <- runif(5)
x2 <- runif(5)
data <- data.frame(x1=rep(x1,each=3),x2=rep(x2,each=3))
ID.coords <- create.ID.coords(data,coords=~x1+x2)
data[,c("x1","x2")]==unique(data[,c("x1","x2")])[ID.coords,]
```

---

`data_sim`*Simulated binomial data-set over the unit square*

---

**Description**

This binomial data-set was simulated by generating a zero-mean Gaussian process over a 30 by 30 grid covering the unit square. The parameters used in the simulation are  $\sigma^2=1$ ,  $\phi=0.15$  and  $\kappa=2$ . The nugget effect was not included, hence  $\tau^2=0$ . The variables are as follows:

- `y` binomial observations.
- `units.m` binomial denominators.
- `x1` horizontal coordinates.
- `x2` vertical coordinates.
- `S` simulated values of the Gaussian process.

**Usage**

```
data(data_sim)
```

**Format**

A data frame with 900 rows and 5 variables

---

dens.plot                      *Density plot for posterior samples*

---

### Description

Plots the autocorrelogram for the posterior samples of the model parameters and spatial random effects.

### Usage

```
dens.plot(  
  object,  
  param,  
  component.beta = NULL,  
  component.S = NULL,  
  hist = TRUE,  
  ...  
)
```

### Arguments

object	an object of class 'Bayes.PrevMap'.
param	a character indicating for which component of the model the density plot is required: param="beta" for the regression coefficients; param="sigma2" for the variance of the spatial random effect; param="phi" for the scale parameter of the Matern correlation function; param="tau2" for the variance of the nugget effect; param="S" for the spatial random effect.
component.beta	if param="beta", component.beta is a numeric value indicating the component of the regression coefficients; default is NULL.
component.S	if param="S", component.S can be a numeric value indicating the component of the spatial random effect. Default is NULL.
hist	logical; if TRUE a histogram is added to density plot.
...	additional parameters to pass to <a href="#">density</a> .

### Author(s)

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

discrete.sample      *Spatially discrete sampling*

---

### Description

Draws a sub-sample from a set of units spatially located irregularly over some defined geographical region by imposing a minimum distance between any two sampled units.

### Usage

```
discrete.sample(xy.all, n, delta, k = 0)
```

### Arguments

xy.all	set of locations from which the sample will be drawn.
n	size of required sample.
delta	minimum distance between any two locations in preliminary sample.
k	number of locations in preliminary sample to be replaced by nearest neighbours of other preliminary sample locations in final sample (must be between 0 and $n/2$ ).

### Details

To draw a sample of size  $n$  from a population of spatial locations  $X_i : i = 1, \dots, N$ , with the property that the distance between any two sampled locations is at least `delta`, the function implements the following algorithm.

- Step 1. Draw an initial sample of size  $n$  completely at random and call this  $x_i : i = 1, \dots, n$ .
- Step 2. Set  $i = 1$  and calculate the minimum,  $d_{\min}$ , of the distances from  $x_i$  to all other  $x_j$  in the initial sample.
- Step 3. If  $d_{\min} \geq \delta$ , increase  $i$  by 1 and return to step 2 if  $i \leq n$ , otherwise stop.
- Step 4. If  $d_{\min} < \delta$ , draw an integer  $j$  at random from  $1, 2, \dots, N$ , set  $x_i = X_j$  and return to step 3.

Samples generated in this way will exhibit a more regular spatial arrangement than would a random sample of the same size. The degree of regularity achievable will be influenced by the spatial arrangement of the population  $X_i : i = 1, \dots, N$ , the specified value of `delta` and the sample size  $n$ . For any given population, if  $n$  and/or `delta` are too large, a sample of the required size with the distance between any two sampled locations at least `delta` will not be achievable; the suggested solution is then to run the algorithm with a smaller value of `delta`.

**Sampling close pairs of points.** For some purposes, it is desirable that a spatial sampling scheme include pairs of closely spaced points. In this case, the above algorithm requires the following additional steps to be taken. Let  $k$  be the required number of close pairs.

- Step 5. Set  $j = 1$  and draw a random sample of size 2 from the integers  $1, 2, \dots, n$ , say  $(i_1, i_2)$ .

- Step 6. Find the integer  $r$  such that the distances from  $x_{i_1}$  to  $X_r$  is the minimum of all  $N - 1$  distances from  $x_{i_1}$  to the  $X_j$ .
- Step 7. Replace  $x_{i_2}$  by  $X_r$ , increase  $i$  by 1 and return to step 5 if  $i \leq k$ , otherwise stop.

### Value

A matrix of dimension  $n$  by 2 containing the final sampled locations.

### Author(s)

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

### Examples

```
x<-0.015+0.03*(1:33)
xall<-rep(x,33)
yall<-c(t(matrix(xall,33,33)))
xy<-cbind(xall,yall)+matrix(-0.0075+0.015*runif(33*33*2),33*33,2)
par(pty="s",mfrow=c(1,2))
plot(xy[,1],xy[,2],pch=19,cex=0.25,xlab="Easting",ylab="Northing",
      cex.lab=1,cex.axis=1,cex.main=1)

set.seed(15892)
# Generate spatially random sample
xy.sample<-xy[sample(1:dim(xy)[1],50,replace=FALSE),]
points(xy.sample[,1],xy.sample[,2],pch=19,col="red")
points(xy[,1],xy[,2],pch=19,cex=0.25)
plot(xy[,1],xy[,2],pch=19,cex=0.25,xlab="Easting",ylab="Northing",
      cex.lab=1,cex.axis=1,cex.main=1)

set.seed(15892)
# Generate spatially regular sample
xy.sample<-discrete.sample(xy,50,0.08)
points(xy.sample[,1],xy.sample[,2],pch=19,col="red")
points(xy[,1],xy[,2],pch=19,cex=0.25)
```

---

galicia

*Heavy metal biomonitoring in Galicia*

---

### Description

This data-set relates to two studies on lead concentration in moss samples, in micrograms per gram dry weight, collected in Galicia, norther Spain. The data are from two surveys, one conducted in October 1997 and on in July 2000. The variables are as follows:

- $x$   $x$ -coordinate of the spatial locations.
- $y$   $y$ -coordinate of the spatial locations.

- lead lead concentration.
- survey year of the survey (either 1997 or 2000).

**Usage**

```
data(galicia)
```

**Format**

A data frame with 195 rows and 4 variables

**Source**

Diggle, P.J., Menezes, R. and Su, T.-L. (2010). Geostatistical analysis under preferential sampling (with Discussion). *Applied Statistics*, 59, 191-232.

---

galicia.boundary      *Boundary of Galicia*

---

**Description**

This data-set contains the geographical coordinates of the boundary of the Galicia region in northern Spain.

The variables are as follows:

- x x-coordinate of the spatial locations.
- y y-coordinate of the spatial locations.

**Usage**

```
data(galicia.boundary)
```

**Format**

A data frame with 42315 rows and 2 variables

---

glgm.LA	<i>Maximum Likelihood estimation for generalised linear geostatistical models via the Laplace approximation</i>
---------	---

---

## Description

This function performs the Laplace method for maximum likelihood estimation of a generalised linear geostatistical model.

## Usage

```
glgm.LA(
  formula,
  units.m = NULL,
  coords,
  times = NULL,
  data,
  ID.coords = NULL,
  kappa,
  kappa.t = 0.5,
  fixed.rel.nugget = NULL,
  start.cov.pars,
  method = "nlminb",
  messages = TRUE,
  family,
  return.covariance = TRUE
)
```

## Arguments

formula	an object of class <a href="#">formula</a> (or one that can be coerced to that class): a symbolic description of the model to be fitted.
units.m	an object of class <a href="#">formula</a> indicating the binomial denominators in the data.
coords	an object of class <a href="#">formula</a> indicating the spatial coordinates in the data.
times	an object of class <a href="#">formula</a> indicating the times in the data, used in the spatio-temporal model.
data	a data frame containing the variables in the model.
ID.coords	vector of ID values for the unique set of spatial coordinates obtained from <a href="#">create.ID.coords</a> . These must be provided if, for example, spatial random effects are defined at household level but some of the covariates are at individual level. <b>Warning:</b> the household coordinates must all be distinct otherwise see <a href="#">jitterDupCoords</a> . Default is NULL.
kappa	fixed value for the shape parameter of the Matern covariance function.
kappa.t	fixed value for the shape parameter of the Matern covariance function in the separable double-Matern spatio-temporal model.

<code>fixed.rel.nugget</code>	fixed value for the relative variance of the nugget effect; <code>fixed.rel.nugget=NULL</code> if this should be included in the estimation. Default is <code>fixed.rel.nugget=NULL</code> .
<code>start.cov.pars</code>	a vector of length two with elements corresponding to the starting values of <code>phi</code> and the relative variance of the nugget effect <code>nu2</code> , respectively, that are used in the optimization algorithm. If <code>nu2</code> is fixed through <code>fixed.rel.nugget</code> , then <code>start.cov.pars</code> represents the starting value for <code>phi</code> only.
<code>method</code>	method of optimization. If <code>method="BFGS"</code> then the <code>maxBFGS</code> function is used; otherwise <code>method="nlminb"</code> to use the <code>nlminb</code> function. Default is <code>method="BFGS"</code> .
<code>messages</code>	logical; if <code>messages=TRUE</code> then status messages are printed on the screen (or output device) while the function is running. Default is <code>messages=TRUE</code> .
<code>family</code>	character, indicating the conditional distribution of the outcome. This should be "Gaussian", "Binomial" or "Poisson".
<code>return.covariance</code>	logical; if <code>return.covariance=TRUE</code> then a numerical estimation of the covariance function for the model parameters is returned. Default is <code>return.covariance=TRUE</code> .

## Details

This function performs parameter estimation for a generalized linear geostatistical model. Conditionally on a zero-mean stationary Gaussian process  $S(x)$  and mutually independent zero-mean Gaussian variables  $Z$  with variance  $\tau^2$ , the observations  $y$  are generated from a GLM with link function  $g(\cdot)$  and linear predictor

$$\eta = d'\beta + S(x) + Z,$$

where  $d$  is a vector of covariates with associated regression coefficients  $\beta$ . The Gaussian process  $S(x)$  has isotropic Matern covariance function (see `matern`) with variance `sigma2`, scale parameter `phi` and shape parameter `kappa`. The shape parameter is treated as fixed. The relative variance of the nugget effect, `nu2=tau2/sigma2`, can also be fixed through the argument `fixed.rel.nugget`; if `fixed.rel.nugget=NULL`, then the relative variance of the nugget effect is also included in the estimation.

**Laplace Approximation** The Laplace approximation (LA) method uses a second-order Taylor expansion of the integrand expressing the likelihood function. The resulting approximation of the likelihood is then maximized by a numerical optimization as defined through the argument `method`.

**Using a two-level model to include household-level and individual-level information.** When analysing data from household surveys, some of the available information might be at household-level (e.g. material of house, temperature) and some at individual-level (e.g. age, gender). In this case, the Gaussian spatial process  $S(x)$  and the nugget effect  $Z$  are defined at household-level in order to account for extra-binomial variation between and within households, respectively.

## Value

An object of class "PrevMap". The function `summary.PrevMap` is used to print a summary of the fitted model. The object is a list with the following components:

`estimate`: estimates of the model parameters; use the function `coef.PrevMap` to obtain estimates of covariance parameters on the original scale.

covariance: covariance matrix of the MCML estimates.  
log.lik: maximum value of the log-likelihood.  
y: binomial observations.  
units.m: binomial denominators.  
D: matrix of covariates.  
coords: matrix of the observed sampling locations.  
times: vector of the time points used in a spatio-temporal model.  
method: method of optimization used.  
ID.coords: set of ID values defined through the argument ID.coords.  
kappa: fixed value of the shape parameter of the Matern function.  
kappa.t: fixed value for the shape parameter of the Matern covariance function in the separable double-Matern spatio-temporal model.  
fixed.rel.nugget: fixed value for the relative variance of the nugget effect.  
call: the matched call.

### Author(s)

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

### References

Diggle, P.J., Giorgi, E. (2019). *Model-based Geostatistics for Global Public Health*. CRC/Chapman & Hall.

Giorgi, E., Diggle, P.J. (2017). *PrevMap: an R package for prevalence mapping*. Journal of Statistical Software. 78(8), 1-29. doi: 10.18637/jss.v078.i08

Christensen, O. F. (2004). *Monte carlo maximum likelihood in model-based geostatistics*. Journal of Computational and Graphical Statistics 13, 702-718.

Higdon, D. (1998). *A process-convolution approach to modeling temperatures in the North Atlantic Ocean*. Environmental and Ecological Statistics 5, 173-190.

### See Also

[Laplace.sampling](#), [Laplace.sampling.lr](#), [summary.PrevMap](#), [coef.PrevMap](#), [matern](#), [matern.kernel](#), [control.mcmc.MCML](#), [create.ID.coords](#).

---

Laplace.sampling

*Langevin-Hastings MCMC for conditional simulation*


---

### Description

This function simulates from the conditional distribution of a Gaussian random effect, given binomial or Poisson observations  $y$ .

### Usage

```
Laplace.sampling(
  mu,
  Sigma,
  y,
  units.m,
  control.mcmc,
  ID.coords = NULL,
  messages = TRUE,
  plot.correlogram = TRUE,
  poisson.llik = FALSE
)
```

### Arguments

<code>mu</code>	mean vector of the marginal distribution of the random effect.
<code>Sigma</code>	covariance matrix of the marginal distribution of the random effect.
<code>y</code>	vector of binomial/Poisson observations.
<code>units.m</code>	vector of binomial denominators, or offset if the Poisson model is used.
<code>control.mcmc</code>	output from <code>control.mcmc.MCML</code> .
<code>ID.coords</code>	vector of ID values for the unique set of spatial coordinates obtained from <code>create.ID.coords</code> . These must be provided if, for example, spatial random effects are defined at household level but some of the covariates are at individual level. <b>Warning:</b> the household coordinates must all be distinct otherwise see <code>jitterDupCoords</code> . Default is <code>NULL</code> .
<code>messages</code>	logical; if <code>messages=TRUE</code> then status messages are printed on the screen (or output device) while the function is running. Default is <code>messages=TRUE</code> .
<code>plot.correlogram</code>	logical; if <code>plot.correlogram=TRUE</code> the autocorrelation plot of the conditional simulations is displayed.
<code>poisson.llik</code>	logical; if <code>poisson.llik=TRUE</code> a Poisson model is used or, if <code>poisson.llik=FALSE</code> , a binomial model is used.

## Details

**Binomial model.** Conditionally on the random effect  $S$ , the data  $y$  follow a binomial distribution with probability  $p$  and binomial denominators `units.m`. The logistic link function is used for the linear predictor, which assumes the form

$$\log(p/(1-p)) = S.$$

**Poisson model.** Conditionally on the random effect  $S$ , the data  $y$  follow a Poisson distribution with mean  $m\lambda$ , where  $m$  is an offset set through the argument `units.m`. The log link function is used for the linear predictor, which assumes the form

$$\log(\lambda) = S.$$

The random effect  $S$  has a multivariate Gaussian distribution with mean `mu` and covariance matrix `Sigma`.

**Laplace sampling.** This function generates samples from the distribution of  $S$  given the data  $y$ . Specifically a Langevin-Hastings algorithm is used to update  $\tilde{S} = \tilde{\Sigma}^{-1/2}(S - \tilde{s})$  where  $\tilde{\Sigma}$  and  $\tilde{s}$  are the inverse of the negative Hessian and the mode of the distribution of  $S$  given  $y$ , respectively. At each iteration a new value  $\tilde{s}_{prop}$  for  $\tilde{S}$  is proposed from a multivariate Gaussian distribution with mean

$$\tilde{s}_{curr} + (h/2)\nabla \log f(\tilde{S}|y),$$

where  $\tilde{s}_{curr}$  is the current value for  $\tilde{S}$ ,  $h$  is a tuning parameter and  $\nabla \log f(\tilde{S}|y)$  is the the gradient of the log-density of the distribution of  $\tilde{S}$  given  $y$ . The tuning parameter  $h$  is updated according to the following adaptive scheme: the value of  $h$  at the  $i$ -th iteration, say  $h_i$ , is given by

$$h_i = h_{i-1} + c_1 i^{-c_2} (\alpha_i - 0.547),$$

where  $c_1 > 0$  and  $0 < c_2 < 1$  are pre-defined constants, and  $\alpha_i$  is the acceptance rate at the  $i$ -th iteration (0.547 is the optimal acceptance rate for a multivariate standard Gaussian distribution). The starting value for  $h$ , and the values for  $c_1$  and  $c_2$  can be set through the function `control.mcmc.MCML`.

**Random effects at household-level.** When the data consist of two nested levels, such as households and individuals within households, the argument `ID.coords` must be used to define the household IDs for each individual. Let  $i$  and  $j$  denote the  $i$ -th household and the  $j$ -th person within that household; the logistic link function then assumes the form

$$\log(p_{ij}/(1-p_{ij})) = \mu_{ij} + S_i$$

where the random effects  $S_i$  are now defined at household level and have mean zero. **Warning:** this modelling option is available only for the binomial model.

## Value

A list with the following components

`samples`: a matrix, each row of which corresponds to a sample from the predictive distribution.

`h`: vector of the values of the tuning parameter at each iteration of the Langevin-Hastings MCMC algorithm.

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

**See Also**

[control.mcmc.MCML](#), [create.ID.coords](#).

---

Laplace.sampling.lr     *Langevin-Hastings MCMC for conditional simulation (low-rank approximation)*

---

**Description**

This function simulates from the conditional distribution of the random effects of binomial and Poisson models.

**Usage**

```
Laplace.sampling.lr(
  mu,
  sigma2,
  K,
  y,
  units.m,
  control.mcmc,
  messages = TRUE,
  plot.correlogram = TRUE,
  poisson.llik = FALSE
)
```

**Arguments**

mu	mean vector of the linear predictor.
sigma2	variance of the random effect.
K	random effect design matrix, or kernel matrix for the low-rank approximation.
y	vector of binomial/Poisson observations.
units.m	vector of binomial denominators, or offset if the Poisson model is used.
control.mcmc	output from <a href="#">control.mcmc.MCML</a> .
messages	logical; if messages=TRUE then status messages are printed on the screen (or output device) while the function is running. Default is messages=TRUE.
plot.correlogram	logical; if plot.correlogram=TRUE the autocorrelation plot of the conditional simulations is displayed.
poisson.llik	logical; if poisson.llik=TRUE a Poisson model is used or, if poisson.llik=FALSE, a binomial model is used.

**Details**

**Binomial model.** Conditionally on  $Z$ , the data  $y$  follow a binomial distribution with probability  $p$  and binomial denominators `units.m`. Let  $K$  denote the random effects design matrix; a logistic link function is used, thus the linear predictor assumes the form

$$\log(p/(1-p)) = \mu + KZ$$

where  $\mu$  is the mean vector component defined through `mu`. **Poisson model.** Conditionally on  $Z$ , the data  $y$  follow a Poisson distribution with mean  $m\lambda$ , where  $m$  is an offset set through the argument `units.m`. Let  $K$  denote the random effects design matrix; a log link function is used, thus the linear predictor assumes the form

$$\log(\lambda) = \mu + KZ$$

where  $\mu$  is the mean vector component defined through `mu`. The random effect  $Z$  has iid components distributed as zero-mean Gaussian variables with variance `sigma2`.

**Laplace sampling.** This function generates samples from the distribution of  $Z$  given the data  $y$ . Specifically, a Langevin-Hastings algorithm is used to update  $\tilde{Z} = \tilde{\Sigma}^{-1/2}(Z - \tilde{z})$  where  $\tilde{\Sigma}$  and  $\tilde{z}$  are the inverse of the negative Hessian and the mode of the distribution of  $Z$  given  $y$ , respectively. At each iteration a new value  $\tilde{z}_{prop}$  for  $\tilde{Z}$  is proposed from a multivariate Gaussian distribution with mean

$$\tilde{z}_{curr} + (h/2)\nabla \log f(\tilde{Z}|y),$$

where  $\tilde{z}_{curr}$  is the current value for  $\tilde{Z}$ ,  $h$  is a tuning parameter and  $\nabla \log f(\tilde{Z}|y)$  is the the gradient of the log-density of the distribution of  $\tilde{Z}$  given  $y$ . The tuning parameter  $h$  is updated according to the following adaptive scheme: the value of  $h$  at the  $i$ -th iteration, say  $h_i$ , is given by

$$h_i = h_{i-1} + c_1 i^{-c_2} (\alpha_i - 0.547),$$

where  $c_1 > 0$  and  $0 < c_2 < 1$  are pre-defined constants, and  $\alpha_i$  is the acceptance rate at the  $i$ -th iteration (0.547 is the optimal acceptance rate for a multivariate standard Gaussian distribution). The starting value for  $h$ , and the values for  $c_1$  and  $c_2$  can be set through the function [control.mcmc.MCML](#).

**Value**

A list with the following components

`samples`: a matrix, each row of which corresponds to a sample from the predictive distribution.

`h`: vector of the values of the tuning parameter at each iteration of the Langevin-Hastings MCMC algorithm.

**Author(s)**

Emanuele Giorgi <[e.giorgi@lancaster.ac.uk](mailto:e.giorgi@lancaster.ac.uk)>

Peter J. Diggle <[p.diggle@lancaster.ac.uk](mailto:p.diggle@lancaster.ac.uk)>

**See Also**

[control.mcmc.MCML](#).

---

Laplace.sampling.SPDE *Independence sampler for conditional simulation of a Gaussian process using SPDE*

---

### Description

This function simulates from the conditional distribution of a Gaussian process given binomial  $y$ . The Gaussian process is also approximated using SPDE.

### Usage

```
Laplace.sampling.SPDE(
  mu,
  sigma2,
  phi,
  kappa,
  y,
  units.m,
  coords,
  mesh,
  control.mcmc,
  messages = TRUE,
  plot.correlogram = TRUE,
  poisson.llik
)
```

### Arguments

<code>mu</code>	mean vector of the Gaussian process to approximate.
<code>sigma2</code>	variance of the Gaussian process to approximate.
<code>phi</code>	scale parameter of the Matern function for the Gaussian process to approximate.
<code>kappa</code>	smoothness parameter of the Matern function for the Gaussian process to approximate.
<code>y</code>	vector of binomial observations.
<code>units.m</code>	vector of binomial denominators.
<code>coords</code>	matrix of two columns corresponding to the spatial coordinates.
<code>mesh</code>	mesh object set through <code>inla.mesh.2d</code> .
<code>control.mcmc</code>	control parameters of the Independence sampler set through <code>control.mcmc.MCML</code> .
<code>messages</code>	logical; if <code>messages=TRUE</code> then status messages are printed on the screen (or output device) while the function is running. Default is <code>messages=TRUE</code> .
<code>plot.correlogram</code>	logical; if <code>plot.correlogram=TRUE</code> the autocorrelation plot of the conditional simulations is displayed.
<code>poisson.llik</code>	logical: if <code>poisson.llik=TRUE</code> then conditional conditional distribution of the data is Poisson; <code>poisson.llik=FALSE</code> then conditional conditional distribution of the data is Binomial.

**Details**

**Binomial model.** Conditionally on the random effect  $S$ , the data  $y$  follow a binomial distribution with probability  $p$  and binomial denominators `units.m`. The logistic link function is used for the linear predictor, which assumes the form

$$\log(p/(1-p)) = S.$$

The random effect  $S$  has a multivariate Gaussian distribution with mean `mu` and covariance matrix `Sigma`.

**Value**

A list with the following components

`samples`: a matrix, each row of which corresponds to a sample from the predictive distribution.

**Author(s)**

Emanuele Giorgi <[e.giorgi@lancaster.ac.uk](mailto:e.giorgi@lancaster.ac.uk)>

Peter J. Diggle <[p.diggle@lancaster.ac.uk](mailto:p.diggle@lancaster.ac.uk)>

**See Also**

[control.mcmc.MCML](#).

---

`linear.model.Bayes`      *Bayesian estimation for the geostatistical linear Gaussian model*

---

**Description**

This function performs Bayesian estimation for the geostatistical linear Gaussian model.

**Usage**

```
linear.model.Bayes(  
  formula,  
  coords,  
  data,  
  kappa,  
  control.mcmc,  
  control.prior,  
  low.rank = FALSE,  
  knots = NULL,  
  messages = TRUE  
)
```

**Arguments**

formula	an object of class "formula" (or one that can be coerced to that class): a symbolic description of the model to be fitted.
coords	an object of class formula indicating the geographic coordinates.
data	a data frame containing the variables in the model.
kappa	shape parameter of the Matern covariance function.
control.mcmc	output from <code>control.mcmc.Bayes</code> .
control.prior	output from <code>control.prior</code> .
low.rank	logical; if low.rank=TRUE a low-rank approximation is fitted.
knots	if low.rank=TRUE, knots is a matrix of spatial knots used in the low-rank approximation. Default is knots=NULL.
messages	logical; if messages=TRUE then status messages are printed on the screen (or output device) while the function is running. Default is messages=TRUE.

**Details**

This function performs Bayesian estimation for the geostatistical linear Gaussian model, specified as

$$Y = d'\beta + S(x) + Z,$$

where  $Y$  is the measured outcome,  $d$  is a vector of covariates,  $\beta$  is a vector of regression coefficients,  $S(x)$  is a stationary Gaussian spatial process and  $Z$  are independent zero-mean Gaussian variables with variance tau2. More specifically,  $S(x)$  has an isotropic Matern covariance function with variance sigma2, scale parameter phi and shape parameter kappa. The shape parameter kappa is treated as fixed.

**Priors definition.** Priors can be defined through the function `control.prior`. The hierarchical structure of the priors is the following. Let  $\theta$  be the vector of the covariance parameters  $(\sigma^2, \phi, \tau^2)$ ; then each component of  $\theta$  can have independent priors freely defined by the user. However, uniform and log-normal priors are also available as default priors for each of the covariance parameters. To remove the nugget effect  $Z$ , no prior should be defined for tau2. Conditionally on sigma2, the vector of regression coefficients beta has a multivariate Gaussian prior with mean beta.mean and covariance matrix sigma2\*beta.covar, while in the low-rank approximation the covariance matrix is simply beta.covar.

**Updating the covariance parameters using a Metropolis-Hastings algorithm.** In the MCMC algorithm implemented in `linear.model.Bayes`, the transformed parameters

$$(\theta_1, \theta_2, \theta_3) = (\log(\sigma^2)/2, \log(\sigma^2/\phi^{2\kappa}), \log(\tau^2))$$

are independently updated using a Metropolis Hastings algorithm. At the  $i$ -th iteration, a new value is proposed for each from a univariate Gaussian distribution with variance, say  $h_i^2$ , tuned according the following adaptive scheme

$$h_i = h_{i-1} + c_1 i^{-c_2} (\alpha_i - 0.45),$$

where  $\alpha_i$  is the acceptance rate at the  $i$ -th iteration (0.45 is the optimal acceptance rate for a univariate Gaussian distribution) whilst  $c_1 > 0$  and  $0 < c_2 < 1$  are pre-defined constants. The starting values  $h_1$  for each of the parameters  $\theta_1$ ,  $\theta_2$  and  $\theta_3$  can be set using the function `control.mcmc.Bayes`

through the arguments `h.theta1`, `h.theta2` and `h.theta3`. To define values for  $c_1$  and  $c_2$ , see the documentation of `control.mcmc.Bayes`.

**Low-rank approximation.** In the case of very large spatial data-sets, a low-rank approximation of the Gaussian spatial process  $S(x)$  might be computationally beneficial. Let  $(x_1, \dots, x_m)$  and  $(t_1, \dots, t_m)$  denote the set of sampling locations and a grid of spatial knots covering the area of interest, respectively. Then  $S(x)$  is approximated as  $\sum_{i=1}^m K(\|x - t_i\|; \phi, \kappa) U_i$ , where  $U_i$  are zero-mean mutually independent Gaussian variables with variance `sigma2` and  $K(\cdot; \phi, \kappa)$  is the isotropic Matern kernel (see `matern.kernel`). Since the resulting approximation is no longer a stationary process (but only approximately), `sigma2` may take very different values from the actual variance of the Gaussian process to approximate. The function `adjust.sigma2` can then be used to (approximately) explore the range for `sigma2`. For example if the variance of the Gaussian process is 0.5, then an approximate value for `sigma2` is `0.5/const.sigma2`, where `const.sigma2` is the value obtained with `adjust.sigma2`.

## Value

An object of class "Bayes.PrevMap". The function `summary.Bayes.PrevMap` is used to print a summary of the fitted model. The object is a list with the following components:

`estimate`: matrix of the posterior samples for each of the model parameters.

`S`: matrix of the posterior samples for each component of the random effect. This is only returned for the low-rank approximation.

`y`: response variable.

`D`: matrix of covariates.

`coords`: matrix of the observed sampling locations.

`kappa`: values of the shape parameter of the Matern function.

`knots`: matrix of spatial knots used in the low-rank approximation.

`const.sigma2`: vector of the values of the multiplicative factor used to adjust the `sigma2` in the low-rank approximation.

`h1`: vector of values taken by the tuning parameter `h.theta1` at each iteration.

`h2`: vector of values taken by the tuning parameter `h.theta2` at each iteration.

`h3`: vector of values taken by the tuning parameter `h.theta3` at each iteration.

`call`: the matched call.

## Author(s)

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

## References

Diggle, P.J., Giorgi, E. (2019). *Model-based Geostatistics for Global Public Health*. CRC/Chapman & Hall.

Giorgi, E., Diggle, P.J. (2017). *PrevMap: an R package for prevalence mapping*. Journal of Statistical Software. 78(8), 1-29. doi: 10.18637/jss.v078.i08

Higdon, D. (1998). *A process-convolution approach to modeling temperatures in the North Atlantic Ocean*. Environmental and Ecological Statistics 5, 173-190.

### See Also

[control.prior](#), [control.mcmc.Bayes](#), [shape.matern](#), [summary.Bayes.PrevMap](#), [autocor.plot](#), [trace.plot](#), [dens.plot](#), [matern](#), [matern.kernel](#), [adjust.sigma2](#).

---

linear.model.MLE	<i>Maximum Likelihood estimation for the geostatistical linear Gaussian model</i>
------------------	---

---

### Description

This function performs maximum likelihood estimation for the geostatistical linear Gaussian Model.

### Usage

```
linear.model.MLE(
  formula,
  coords = NULL,
  data,
  ID.coords = NULL,
  kappa,
  fixed.rel.nugget = NULL,
  start.cov.pars,
  method = "BFGS",
  low.rank = FALSE,
  knots = NULL,
  messages = TRUE,
  profile.llik = FALSE,
  SPDE = FALSE,
  mesh = NULL,
  SPDE.analytic.hessian = FALSE
)
```

### Arguments

formula	an object of class " <a href="#">formula</a> " (or one that can be coerced to that class): a symbolic description of the model to be fitted.
coords	an object of class <a href="#">formula</a> indicating the geographic coordinates.
data	a data frame containing the variables in the model.
ID.coords	vector of ID values for the unique set of spatial coordinates obtained from <a href="#">create.ID.coords</a> . These must be provided in order to define a geostatistical model where locations have multiple observations. Default is ID.coords=NULL. See the <b>Details</b> section for more information.

<code>kappa</code>	shape parameter of the Matern covariance function.
<code>fixed.rel.nugget</code>	fixed value for the relative variance of the nugget effect; default is <code>fixed.rel.nugget=NULL</code> if this should be included in the estimation.
<code>start.cov.pars</code>	if <code>ID.coords=NULL</code> , a vector of length two with elements corresponding to the starting values of <code>phi</code> and the relative variance of the nugget effect <code>nu2</code> , respectively, that are used in the optimization algorithm; if <code>ID.coords</code> is provided, a third starting value for the relative variance of the individual unexplained variation <code>nu2.star = omega2/sigma2</code> must be provided. If <code>nu2</code> is fixed through <code>fixed.rel.nugget</code> , then <code>start.cov.pars</code> represents the starting value for <code>phi</code> only, if <code>ID.coords=NULL</code> , or for <code>phi</code> and <code>nu2.star</code> , otherwise.
<code>method</code>	method of optimization. If <code>method="BFGS"</code> then the <code>maxBFGS</code> function is used; otherwise <code>method="nlminb"</code> to use the <code>nlminb</code> function. Default is <code>method="BFGS"</code> .
<code>low.rank</code>	logical; if <code>low.rank=TRUE</code> a low-rank approximation of the Gaussian spatial process is used when fitting the model. Default is <code>low.rank=FALSE</code> .
<code>knots</code>	if <code>low.rank=TRUE</code> , <code>knots</code> is a matrix of spatial knots that are used in the low-rank approximation. Default is <code>knots=NULL</code> .
<code>messages</code>	logical; if <code>messages=TRUE</code> then status messages are printed on the screen (or output device) while the function is running. Default is <code>messages=TRUE</code> .
<code>profile.lik</code>	logical; if <code>profile.lik=TRUE</code> the maximization of the profile likelihood is carried out. If <code>profile.lik=FALSE</code> the full-likelihood is used. Default is <code>profile.lik=FALSE</code> .
<code>SPDE</code>	logical; if <code>SPDE=TRUE</code> the SPDE approximation for the Gaussian spatial model is used. Default is <code>SPDE=FALSE</code> .
<code>mesh</code>	an object obtained as result of a call to the function <code>inla.mesh.2d</code> .
<code>SPDE.analytic.hessian</code>	logical; if <code>SPDE.analytic.hessian=TRUE</code> computation of the hessian matrix using the SPDE approximation is carried out using analytical expressions, otherwise a numerical approximation is used. Defaults is <code>SPDE.analytic.hessian=FALSE</code> .

## Details

This function estimates the parameters of a geostatistical linear Gaussian model, specified as

$$Y = d'\beta + S(x) + Z,$$

where  $Y$  is the measured outcome,  $d$  is a vector of covariates,  $\beta$  is a vector of regression coefficients,  $S(x)$  is a stationary Gaussian spatial process and  $Z$  are independent zero-mean Gaussian variables with variance  $\tau^2$ . More specifically,  $S(x)$  has an isotropic Matern covariance function with variance  $\sigma^2$ , scale parameter  $\phi$  and shape parameter  $\kappa$ . In the estimation, the shape parameter  $\kappa$  is treated as fixed. The relative variance of the nugget effect,  $\text{nu2}=\tau^2/\sigma^2$ , can be fixed through the argument `fixed.rel.nugget`; if `fixed.rel.nugget=NULL`, then the variance of the nugget effect is also included in the estimation.

**Locations with multiple observations.** If multiple observations are available at any of the sampled locations the above model is modified as follows. Let  $Y_{ij}$  denote the random variable associated to

the measured outcome for the  $j$ -th individual at location  $x_i$ . The linear geostatistical model assumes the form

$$Y_{ij} = d'_{ij}\beta + S(x_i) + Zi + U_{ij},$$

where  $S(x_i)$  and  $Z_i$  are specified as mentioned above, and  $U_{ij}$  are i.i.d. zero-mean Gaussian variable with variance  $\omega^2$ . This model can be fitted by specifying a vector of ID for the unique set locations through the argument `ID.coords` (see also `create.ID.coords`).

**Low-rank approximation.** In the case of very large spatial data-sets, a low-rank approximation of the Gaussian spatial process  $S(x)$  can be computationally beneficial. Let  $(x_1, \dots, x_m)$  and  $(t_1, \dots, t_m)$  denote the set of sampling locations and a grid of spatial knots covering the area of interest, respectively. Then  $S(x)$  is approximated as  $\sum_{i=1}^m K(\|x - t_i\|; \phi, \kappa)U_i$ , where  $U_i$  are zero-mean mutually independent Gaussian variables with variance `sigma2` and  $K(\cdot; \phi, \kappa)$  is the isotropic Matern kernel (see `matern.kernel`). Since the resulting approximation is no longer a stationary process, the parameter `sigma2` is adjusted by a factor `constant.sigma2`. See `adjust.sigma2` for more details on the computation of the adjustment factor `constant.sigma2` in the low-rank approximation.

## Value

An object of class "PrevMap". The function `summary.PrevMap` is used to print a summary of the fitted model. The object is a list with the following components:

`estimate`: estimates of the model parameters; use the function `coef.PrevMap` to obtain estimates of covariance parameters on the original scale.

`covariance`: covariance matrix of the ML estimates.

`log.lik`: maximum value of the log-likelihood.

`y`: response variable.

`D`: matrix of covariates.

`coords`: matrix of the observed sampling locations.

`ID.coords`: set of ID values defined through the argument `ID.coords`.

`method`: method of optimization used.

`kappa`: fixed value of the shape parameter of the Matern function.

`knots`: matrix of the spatial knots used in the low-rank approximation.

`const.sigma2`: adjustment factor for `sigma2` in the low-rank approximation.

`fixed.rel.nugget`: fixed value for the relative variance of the nugget effect.

`mesh`: the mesh used in the SPDE approximation.

`call`: the matched call.

## Author(s)

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## References

- Diggle, P.J., Giorgi, E. (2019). *Model-based Geostatistics for Global Public Health*. CRC/Chapman & Hall.
- Giorgi, E., Diggle, P.J. (2017). *PrevMap: an R package for prevalence mapping*. Journal of Statistical Software. 78(8), 1-29. doi: 10.18637/jss.v078.i08
- Higdon, D. (1998). *A process-convolution approach to modeling temperatures in the North Atlantic Ocean*. Environmental and Ecological Statistics 5, 173-190.

## See Also

[shape.matern](#), [summary.PrevMap](#), [coef.PrevMap](#), [matern](#), [matern.kernel](#), [maxBFGS](#), [nlminb](#).

---

Im.ps.MCML

*Monte Carlo Maximum Likelihood estimation of the geostatistical linear model with preferentially sampled locations*

---

## Description

This function performs Monte Carlo maximum likelihood (MCML) estimation for a geostatistical linear model with preferentially sampled locations. For more details on the model, see below.

## Usage

```
Im.ps.MCML(  
  formula.response,  
  formula.log.intensity = ~1,  
  coords,  
  which.is.preferential = NULL,  
  data.response,  
  data.intensity = NULL,  
  par0,  
  control.mcmc,  
  kappa1,  
  kappa2,  
  mesh,  
  grid.intensity,  
  start.par = NULL,  
  method = "nlminb",  
  messages = TRUE,  
  plot.correlogram = TRUE  
)
```

**Arguments**

<code>formula.response</code>	an object of class <code>formula</code> (or one that can be coerced to that class): a symbolic description of the sub-model for the response variable.
<code>formula.log.intensity</code>	an object of class <code>formula</code> (or one that can be coerced to that class): a symbolic description of the log-Gaussian Cox process sub-model.
<code>coords</code>	an object of class <code>formula</code> indicating the spatial coordinates in the data.
<code>which.is.preferential</code>	a vector of 0 and 1, where 1 indicates a location in the data from a preferential sampling scheme and 0 from a non-preferential. This option is used to fit a model with a mix of preferentially and non-preferentially sampled locations. For more, details on the model structure see the 'Details' section.
<code>data.response</code>	a data frame containing the variables in the sub-model of the response variable.
<code>data.intensity</code>	a data frame containing the variables in the log-Gaussian Cox process sub-model. This data frame must be provided only when explanatory variables are used in the log-Gaussian Cox process model. Each row in the data frame must correspond to a point in the grid provided through the argument ' <code>grid.intensity</code> '. Default is <code>data.intensity=NULL</code> , which corresponds to a model with only the intercept.
<code>par0</code>	an object of class ' <code>coef.PrevMap.ps</code> '. This argument is used to define the parameters of the importance sampling distribution used in the MCML algorithm. The input of this argument must be defined using the <code>set.par.ps</code> function.
<code>control.mcmc</code>	output from <code>control.mcmc.MCML</code> which defined the control parameters of the Monte Carlo Markov chain algorithm.
<code>kappa1</code>	fixed value for the shape parameter of the Matern covariance function of the spatial process of the sampling intensity (currently only <code>kappa1=1</code> is implemented).
<code>kappa2</code>	fixed value for the shape parameter of the Matern covariance function of the spatial process of the response variable.
<code>mesh</code>	an object obtained as result of a call to the function <code>inla.mesh.2d</code> .
<code>grid.intensity</code>	a regular grid covering the geographical region of interest, used to approximate the density function of the log-Gaussian Cox process.
<code>start.par</code>	starting value of the optimization algorithm. This is an object of class ' <code>coef.PrevMap.ps</code> ' and must be defined using the function <code>set.par.ps</code> . Default is <code>start.cov.pars=NULL</code> , so that the starting values are set automatically.
<code>method</code>	method of optimization. If <code>method="BFGS"</code> then the <code>maxBFGS</code> function is used; otherwise <code>method="nlminb"</code> to use the <code>nlminb</code> function. Default is <code>method="BFGS"</code> .
<code>messages</code>	logical; if <code>messages=TRUE</code> then status messages are printed on the screen (or output device) while the function is running. Default is <code>messages=TRUE</code> .
<code>plot.correlogram</code>	logical; if <code>plot.correlogram=TRUE</code> the autocorrelation plot of the samples of the random effect is displayed after completion of conditional simulation. Default is <code>plot.correlogram=TRUE</code> .

## Details

This function performs parameter estimation for a geostatistical linear model with preferentially sampled locations. Let  $S_1$  and  $S_2$  denote two independent, stationary and isotropic Gaussian processes. The overall model consists of two sub-models: the log-Gaussian Cox process model for the preferentially sampled locations, say  $X$ ; the model for the response variable, say  $Y$ . The model assumes that

$$[X, Y, S_1, S_2] = [S_1][S_2][X|S_1][Y|X, S_1, S_2],$$

where  $[\cdot]$  denotes 'the distribution of  $\cdot$ '. Each of the two submodels has an associated linear predictor. Let  $\Lambda(x)$  denote the intensity of the Poisson process  $X$ , continionally on  $S_1$ . Then

$$\log\{\Lambda(x)\} = d(x)'\alpha + S_1$$

, where  $d(x)$  is vector of explanatory variables with regression coefficient  $\alpha$ . This linear predictor is defined through the argument `formula.log.intensity`. The density of  $[X|S_1]$  is given by

$$\frac{\Lambda(x)}{\int_A \Lambda(u) du}$$

, where  $A$  is the region of interest. The integral at the denominator is intractable and is then approximated using a quadrature procedure. The regular grid covering  $A$ , used for the quadrature, must be provided through the argument `grid.intensity`. Conditionally on  $X$ ,  $S_1$  and  $S_2$ , the response variable model is given by

$$Y = d(x)'\beta + S_2 + \gamma S_1,$$

where  $\beta$  is another vector of regression coefficients and  $\gamma$  is the preferentiality parameter. If  $\gamma = 0$  then we recover the standard geostatistical model. More details on the fitting procedure can be found in Diggle and Giorgi (2016).

**When the data have a mix of preferentially and non-preferentially sampled locations.** In some cases the set of locations may consist of a sub-set which is preferentially sampled,  $X$ , and a standard non-preferential sample,  $X^*$ . Let  $Y$  and  $Y^*$  denote the measurements at locations  $X$  and  $X^*$ . In the current implementation, the model has the following form

$$[X, X^*, Y, Y^*, S_1, S_2, S_2^*] = [S_1][S_2][S_2^*][X|S_1][Y|X, S_1, S_2][X^*][Y^*|X^*, S_2^*],$$

where  $S_2$  and  $S_2^*$  are two independent Gaussian process but with shared parameters, associated with  $Y$  and  $Y^*$ , respectively. The linear predictor for  $Y$  is the same as above. The measurements  $Y^*$ , instead, have linear predicotr

$$Y^* = d(x)'\beta + S_2^*,$$

where  $\beta^*$  is vector of regression coefficients, different from  $\beta$ . The linear predictor for  $Y$  and  $Y^*$  is specified though `formula.response`. For example, `response ~ x | x + z` defines a linear predictor for  $Y$  with one explanatory variable  $x$  and a linear predictor for  $Y^*$  with two explanatory variables  $x$  and  $z$ . An example on the application of this model is given in Diggle and Giorgi (2016).

## Value

An object of class "PrevMap.ps". The function `summary.PrevMap.ps` is used to print a summary of the fitted model. The object is a list with the following components:

`estimate`: estimates of the model parameters; use the function `coef.PrevMap.ps` to obtain estimates of covariance parameters on the original scale.

covariance: covariance matrix of the MCML estimates.

log.lik: maximum value of the approximated log-likelihood.

y: observed values of the response variable. If `which.is.preferential` has been provided, then `y` is a list with components `y$preferential`, for the data with preferentially sampled locations, and `y$non.preferential`, for the remaining.

D.response: matrix of covariates used to model the mean component of the response variable. If `which.is.preferential` has been provided, then `D.response` is a list with components `D.response$preferential`, for the data with preferentially sampled locations, and `D.response$non.preferential`, for the remaining.

D.intensity: matrix of covariates used to model the mean component of log-intensity of the log-Gaussian Cox process.

grid.intensity: grid of locations used to approximate the intractable integral of the log-Gaussian Cox process model.

coords: matrix of the observed sampling locations. If `which.is.preferential` has been provided, then `coords` is a list with components `y$preferential`, for the data with preferentially sampled locations, and `y$non.preferential`, for the remaining.

method: method of optimization used.

ID.coords: set of ID values defined through the argument `ID.coords`.

kappa.response: fixed value of the shape parameter of the Matern covariance function used to model the spatial process associated with the response variable.

mesh: the mesh used in the SPDE approximation.

samples: matrix of the random effects samples from the importance sampling distribution used to approximate the likelihood function.

call: the matched call.

## Author(s)

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## References

- Diggle, P.J., Giorgi, E. (2019). *Model-based Geostatistics for Global Public Health*. CRC/Chapman & Hall.
- Giorgi, E., Diggle, P.J. (2017). *PrevMap: an R package for prevalence mapping*. Journal of Statistical Software. 78(8), 1-29. doi: 10.18637/jss.v078.i08
- Diggle, P.J., Giorgi, E. (2017). *Preferential sampling of exposures levels*. In: Handbook of Environmental and Ecological Statistics. Chapman & Hall.
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- Lindgren, F., Havard, R., Lindstrom, J. (2011). *An explicit link between Gaussian fields and Gaussian Markov random fields: the stochastic partial differential equation approach (with discussion)*. Journal of the Royal Statistical Society, Series B, 73, 423-498.
- Pati, D., Reich, B. J., and Dunson, D. B. (2011). *Bayesian geostatistical modelling with informative sampling locations*. Biometrika, 98, 35-48.

---

`loaloa`*Loa loa prevalence data from 197 village surveys*

---

## Description

This data-set relates to a study of the prevalence of *Loa loa* (eyeworm) in a series of surveys undertaken in 197 villages in west Africa (Cameroon and southern Nigeria). The variables are as follows:

- ROW row id: 1 to 197.
- VILLCODE village id.
- LONGITUDE Longitude in degrees.
- LATITUDE Latitude in degrees.
- NO\_EXAM Number of people tested.
- NO\_INF Number of positive test results.
- ELEVATION Height above sea-level in metres.
- MEAN9901 Mean of all NDVI values recorded at village location, 1999-2001
- MAX9901 Maximum of all NDVI values recorded at village location, 1999-2001
- MIN9901 Minimum of all NDVI values recorded at village location, 1999-2001
- MIN9901 Minimum of all NDVI values recorded at village location, 1999-2001
- STDEV9901 standard deviation of all NDVI values recorded at village location, 1999-2001

## Usage

```
data(loaloa)
```

## Format

A data frame with 197 rows and 11 variables

## References

Diggle, P.J., Thomson, M.C., Christensen, O.F., Rowlingson, B., Obsomer, V., Gardon, J., Wanji, S., Takougang, I., Enyong, P., Kamgno, J., Remme, H., Boussinesq, M. and Molyneux, D.H. (2007). Spatial modelling and prediction of *Loa loa* risk: decision making under uncertainty. *Annals of Tropical Medicine and Parasitology*, 101, 499-509.

---

loglik.ci	<i>Profile likelihood confidence intervals</i>
-----------	--

---

### Description

Computes confidence intervals based on the interpolated profile likelihood computed for a single covariance parameter.

### Usage

```
loglik.ci(object, coverage = 0.95, plot.spline.profile = TRUE)
```

### Arguments

object	object of class "profile.PrevMap" obtained from <a href="#">loglik.linear.model</a> .
coverage	a value between 0 and 1 indicating the coverage of the confidence interval based on the interpolated profile likelihood. Default is coverage=0.95.
plot.spline.profile	logical; if TRUE an interpolating spline of the profile-likelihood of for a univariate parameter is plotted. Default is FALSE.

### Value

A list with elements lower and upper for the upper and lower limits of the confidence interval, respectively.

### Author(s)

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---

loglik.linear.model	<i>Profile log-likelihood or fixed parameters likelihood evaluation for the covariance parameters in the geostatistical linear model</i>
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---

### Description

Computes profile log-likelihood, or evaluates likelihood keeping the other parameters fixed, for the scale parameter  $\phi$  of the Matern function and the relative variance of the nugget effect  $\nu^2$  in the linear Gaussian model.

**Usage**

```
loglik.linear.model(
  object,
  control.profile,
  plot.profile = TRUE,
  messages = TRUE
)
```

**Arguments**

`object` an object of class 'PrevMap', which is the fitted linear model obtained with the function `linear.model.MLE`.

`control.profile` control parameters obtained with `control.profile`.

`plot.profile` logical; if TRUE a plot of the computed profile likelihood is displayed.

`messages` logical; if messages=TRUE then status messages are printed on the screen (or output device) while the function is running. Default is messages=TRUE.

**Value**

an object of class "profile.PrevMap" which is a list with the following values

`eval.points.phi`: vector of the values used for phi in the evaluation of the likelihood.

`eval.points.rel.nugget`: vector of the values used for nu2 in the evaluation of the likelihood.

`profile.phi`: vector of the values of the likelihood function evaluated at `eval.points.phi`.

`profile.rel.nugget`: vector of the values of the likelihood function evaluated at `eval.points.rel.nugget`.

`profile.phi.rel.nugget`: matrix of the values of the likelihood function evaluated at `eval.points.phi` and `eval.points.rel.nugget`.

`fixed.par`: logical value; TRUE is the evaluation if the likelihood is carried out by fixing the other parameters, and FALSE if the computation of the profile-likelihood was performed instead.

**Author(s)**

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 Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

 matern.kernel

*Matern kernel*


---

**Description**

This function computes values of the Matern kernel for given distances and parameters.

**Usage**

```
matern.kernel(u, rho, kappa)
```

**Arguments**

u	a vector, matrix or array with values of the distances between pairs of data locations.
rho	value of the (re-parametrized) scale parameter; this corresponds to the re-parametrization $\text{rho} = 2 * \text{sqrt}(\text{kappa}) * \text{phi}$ .
kappa	value of the shape parameter.

**Details**

The Matern kernel is defined as:

$$K(u; \phi, \kappa) = \frac{\Gamma(\kappa + 1)^{1/2} \kappa^{(\kappa+1)/4} u^{(\kappa-1)/2}}{\pi^{1/2} \Gamma((\kappa + 1)/2) \Gamma(\kappa)^{1/2} (2\kappa^{1/2} \phi)^{(\kappa+1)/2}} \mathcal{K}_{\kappa}(u/\phi), u > 0,$$

where  $\phi$  and  $\kappa$  are the scale and shape parameters, respectively, and  $\mathcal{K}_{\kappa}(\cdot)$  is the modified Bessel function of the third kind of order  $\kappa$ . The family is valid for  $\phi > 0$  and  $\kappa > 0$ .

**Value**

A vector matrix or array, according to the argument u, with the values of the Matern kernel function for the given distances.

**Author(s)**

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Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

plot.pred.PrevMap      *Plot of a predicted surface*

---

**Description**

plot.pred.PrevMap displays predictions obtained from [spatial.pred.linear.MLE](#), [spatial.pred.linear.Bayes](#), [spatial.pred.binomial.Bayes](#) and [spatial.pred.poisson.MCML](#).

**Usage**

```
## S3 method for class 'pred.PrevMap'
plot(x, type = NULL, summary = "predictions", ...)
```

**Arguments**

x	an object of class "PrevMap".
type	a character indicating the type of prediction to display: 'prevalence', 'odds', 'logit' or 'probit' for binomial models; "log" or "exponential" for Poisson models. Default is NULL.
summary	character indicating which summary to display: 'predictions', 'quantiles', 'standard.errors' or 'exceedance.prob'; default is 'predictions'. If summary="exceedance.prob", the argument type is ignored.
...	further arguments passed to <code>plot</code> of the 'raster' package.

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

plot.pred.PrevMap.ps *Plot of a predicted surface of geostatistical linear fits with preferentially sampled locations*

---

**Description**

plot.pred.PrevMap.ps displays predictions obtained from `lm.ps.MCML`.

**Usage**

```
## S3 method for class 'pred.PrevMap.ps'
plot(x, target = NULL, summary = "predictions", ...)
```

**Arguments**

x	an object of class "PrevMap".
target	a integer value indicating the predictive target: target=1 to visualize summaries of the surface associated with the response variable; target=2 to visualize summaries of the surface associated with the sampling intensity. If only one target has been predicted, this argument is ignored.
summary	character indicating which summary to display: 'predictions', 'quantiles' or 'standard.errors'. Default is summary='predictions'. If summary="exceedance.prob", the argument type is ignored.
...	further arguments passed to <code>plot</code> of the 'raster' package.

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

---

`plot.PrevMap.diagnostic`*Plot of the variogram-based diagnostics*

---

**Description**

Displays the results from a call to `variog.diagnostic.lm` and `variog.diagnostic.glm`.

**Usage**

```
## S3 method for class 'PrevMap.diagnostic'  
plot(x, ...)
```

**Arguments**

`x` an object of class "PrevMap.diagnostic".  
`...` further arguments passed to `plot` of the 'raster' package.

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>  
Peter J. Diggle <p.diggle@lancaster.ac.uk>

**See Also**

`variog.diagnostic.lm`, `variog.diagnostic.glm`

---

`plot.profile.PrevMap` *Plot of the profile log-likelihood for the covariance parameters of the Matern function*

---

**Description**

This function displays a plot of the profile log-likelihood that is computed by the function `loglik.linear.model`.

**Usage**

```
## S3 method for class 'profile.PrevMap'  
plot(x, log.scale = FALSE, plot.spline.profile = FALSE, ...)
```

**Arguments**

x	object of class "profile.PrevMap" obtained as output from <a href="#">loglik.linear.model</a> .
log.scale	logical; if log.scale=TRUE, the profile likelihood is plotted on the log-scale of the parameter values.
plot.spline.profile	logical; if TRUE an interpolating spline of the profile-likelihood of for a univariate parameter is plotted. Default is FALSE.
...	further arguments passed to <a href="#">plot</a> if the profile log-likelihood is for only one parameter, or to <a href="#">contour</a> for the bi-variate profile-likelihood.

**Value**

A plot is returned. No value is returned.

**Author(s)**

Emanuele Giorgi <[e.giorgi@lancaster.ac.uk](mailto:e.giorgi@lancaster.ac.uk)>

Peter J. Diggle <[p.diggle@lancaster.ac.uk](mailto:p.diggle@lancaster.ac.uk)>

---

plot.shape.matern	<i>Plot of the profile likelihood for the shape parameter of the Matern covariance function</i>
-------------------	---

---

**Description**

This function plots the profile likelihood for the shape parameter of the Matern covariance function using the output from [shape.matern](#) function.

**Usage**

```
## S3 method for class 'shape.matern'
plot(x, plot.spline = TRUE, ...)
```

**Arguments**

x	an object of class 'shape.matern' obtained as result of a call to <a href="#">shape.matern</a>
plot.spline	logical; if TRUE an interpolating spline of the profile likelihood is added to the plot.
...	further arguments passed to <a href="#">plot</a> .

**Value**

The function does not return any value.

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

**See Also**

[shape.matern](#)

---

point.map

*Point map*

---

**Description**

This function produces a plot with points indicating the data locations. Arguments can control the points sizes, patterns and colors. These can be set to be proportional to data values, ranks or quantiles. Alternatively, points can be added to the current plot.

**Usage**

```
point.map(data, var.name, coords, ...)
```

**Arguments**

data	an object of class "data.frame" containing the data.
var.name	a <a href="#">formula</a> object indicating the variable to display.
coords	a <a href="#">formula</a> object indicating the geographical coordinates.
...	additional arguments to be passed to <code>points.geodata</code> .

---

poisson.log.MCML

*Monte Carlo Maximum Likelihood estimation for the Poisson model*

---

**Description**

This function performs Monte Carlo maximum likelihood (MCML) estimation for the geostatistical Poisson model with log link function.

**Usage**

```

poisson.log.MCML(
  formula,
  units.m = NULL,
  coords,
  data,
  ID.coords = NULL,
  par0,
  control.mcmc,
  kappa,
  fixed.rel.nugget = NULL,
  start.cov.pars,
  method = "BFGS",
  low.rank = FALSE,
  knots = NULL,
  messages = TRUE,
  plot.correlogram = TRUE
)

```

**Arguments**

formula	an object of class <code>formula</code> (or one that can be coerced to that class): a symbolic description of the model to be fitted.
units.m	an object of class <code>formula</code> indicating the multiplicative offset for the mean of the Poisson model; if not specified this is then internally set as 1.
coords	an object of class <code>formula</code> indicating the geographic coordinates.
data	a data frame containing the variables in the model.
ID.coords	vector of ID values for the unique set of spatial coordinates obtained from <code>create.ID.coords</code> . These must be provided if, for example, spatial random effects are defined at location-level but some of the covariates are at individual level. <b>Warning:</b> the spatial coordinates must all be distinct otherwise see <code>jitterDupCoords</code> . Default is <code>NULL</code> .
par0	parameters of the importance sampling distribution: these should be given in the following order <code>c(beta, sigma2, phi, tau2)</code> , where <code>beta</code> are the regression coefficients, <code>sigma2</code> is the variance of the Gaussian process, <code>phi</code> is the scale parameter of the spatial correlation and <code>tau2</code> is the variance of the nugget effect (if included in the model).
control.mcmc	output from <code>control.mcmc.MCML</code> .
kappa	fixed value for the shape parameter of the Matern covariance function.
fixed.rel.nugget	fixed value for the relative variance of the nugget effect; <code>fixed.rel.nugget=NULL</code> if this should be included in the estimation. Default is <code>fixed.rel.nugget=NULL</code> .
start.cov.pars	a vector of length two with elements corresponding to the starting values of <code>phi</code> and the relative variance of the nugget effect <code>nu2</code> , respectively, that are used in the optimization algorithm. If <code>nu2</code> is fixed through <code>fixed.rel.nugget</code> , then <code>start.cov.pars</code> represents the starting value for <code>phi</code> only.

method	method of optimization. If method="BFGS" then the <code>maxBFGS</code> function is used; otherwise method="nlminb" to use the <code>nlminb</code> function. Default is method="BFGS".
low.rank	logical; if low.rank=TRUE a low-rank approximation of the Gaussian spatial process is used when fitting the model. Default is low.rank=FALSE.
knots	if low.rank=TRUE, knots is a matrix of spatial knots that are used in the low-rank approximation. Default is knots=NULL.
messages	logical; if messages=TRUE then status messages are printed on the screen (or output device) while the function is running. Default is messages=TRUE.
plot.correlogram	logical; if plot.correlogram=TRUE the autocorrelation plot of the samples of the random effect is displayed after completion of conditional simulation. Default is plot.correlogram=TRUE.

## Details

This function performs parameter estimation for a geostatistical Poisson model with log link function. Conditionally on a zero-mean stationary Gaussian process  $S(x)$  and mutually independent zero-mean Gaussian variables  $Z$  with variance  $\tau^2$ , the observations  $y$  are generated from a Poisson distribution with mean  $m\lambda$ , where  $m$  is an offset defined through the argument `units.m`. A canonical log link is used, thus the linear predictor assumes the form

$$\log(\lambda) = d'\beta + S(x) + Z,$$

where  $d$  is a vector of covariates with associated regression coefficients  $\beta$ . The Gaussian process  $S(x)$  has isotropic Matern covariance function (see `matern`) with variance `sigma2`, scale parameter `phi` and shape parameter `kappa`. In the `poisson.log.MCML` function, the shape parameter is treated as fixed. The relative variance of the nugget effect, `nu2=tau2/sigma2`, can also be fixed through the argument `fixed.rel.nugget`; if `fixed.rel.nugget=NULL`, then the relative variance of the nugget effect is also included in the estimation.

**Monte Carlo Maximum likelihood.** The Monte Carlo maximum likelihood method uses conditional simulation from the distribution of the random effect  $T(x) = d(x)'\beta + S(x) + Z$  given the data  $y$ , in order to approximate the high-dimensional intractable integral given by the likelihood function. The resulting approximation of the likelihood is then maximized by a numerical optimization algorithm which uses analytic expression for computation of the gradient vector and Hessian matrix. The functions used for numerical optimization are `maxBFGS` (method="BFGS"), from the `maxLik` package, and `nlminb` (method="nlminb").

**Low-rank approximation.** In the case of very large spatial data-sets, a low-rank approximation of the Gaussian spatial process  $S(x)$  might be computationally beneficial. Let  $(x_1, \dots, x_m)$  and  $(t_1, \dots, t_m)$  denote the set of sampling locations and a grid of spatial knots covering the area of interest, respectively. Then  $S(x)$  is approximated as  $\sum_{i=1}^m K(\|x - t_i\|; \phi, \kappa) U_i$ , where  $U_i$  are zero-mean mutually independent Gaussian variables with variance `sigma2` and  $K(\cdot; \phi, \kappa)$  is the isotropic Matern kernel (see `matern.kernel`). Since the resulting approximation is no longer a stationary process (but only approximately), the parameter `sigma2` is then multiplied by a factor `constant.sigma2` so as to obtain a value that is closer to the actual variance of  $S(x)$ .

## Value

An object of class "PrevMap". The function `summary.PrevMap` is used to print a summary of the fitted model. The object is a list with the following components:

`estimate`: estimates of the model parameters; use the function `coef.PrevMap` to obtain estimates of covariance parameters on the original scale.

`covariance`: covariance matrix of the MCML estimates.

`log.lik`: maximum value of the log-likelihood.

`y`: observations.

`units.m`: offset.

`D`: matrix of covariates.

`ID.coords`: set of ID values defined through the argument `ID.coords`.

`coords`: matrix of the observed sampling locations.

`method`: method of optimization used.

`kappa`: fixed value of the shape parameter of the Matern function.

`knots`: matrix of the spatial knots used in the low-rank approximation.

`const.sigma2`: adjustment factor for `sigma2` in the low-rank approximation.

`h`: vector of the values of the tuning parameter at each iteration of the Langevin-Hastings MCMC algorithm; see `Laplace.sampling`, or `Laplace.sampling.lr` if a low-rank approximation is used.

`samples`: matrix of the random effects samples from the importance sampling distribution used to approximate the likelihood function.

`fixed.rel.nugget`: fixed value for the relative variance of the nugget effect.

`call`: the matched call.

### Author(s)

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

### References

Diggle, P.J., Giorgi, E. (2019). *Model-based Geostatistics for Global Public Health*. CRC/Chapman & Hall.

Giorgi, E., Diggle, P.J. (2017). *PrevMap: an R package for prevalence mapping*. Journal of Statistical Software. 78(8), 1-29. doi: 10.18637/jss.v078.i08

Christensen, O. F. (2004). *Monte carlo maximum likelihood in model-based geostatistics*. Journal of Computational and Graphical Statistics 13, 702-718.

Higdon, D. (1998). *A process-convolution approach to modeling temperatures in the North Atlantic Ocean*. Environmental and Ecological Statistics 5, 173-190.

### See Also

`Laplace.sampling`, `Laplace.sampling.lr`, `summary.PrevMap`, `coef.PrevMap`, `matern`, `matern.kernel`, `control.mcmc.MCML`.

---

set.par.ps	<i>Define the model coefficients of a geostatistical linear model with preferentially sampled locations</i>
------------	---

---

### Description

set.par.ps defines the model coefficients of a geostatistical linear model with preferentially sampled locations. The output of this function can be used to: 1) define the parameters of the importance sampling distribution in `lm.ps.MCML`; 2) the starting values of the optimization algorithm in `lm.ps.MCML`.

### Usage

```
set.par.ps(p = 1, q = 1, intensity, response, preferentiality.par)
```

### Arguments

p	number of covariates used in the response variable model, including the intercept. Default is p=1.
q	number of covariates used in the log-Gaussian Cox process model, including the intercept. Default is q=1.
intensity	a vector of parameters of the log-Gaussian Cox process model. These must be provided in the following order: regression coefficients of the explanatory variables; variance and scale of the spatial correlation for the isotropic Gaussian process. In the case of a model with a mix of preferentially and non-preferentially sampled locations, the order of the regression coefficients should be the following: regression coefficients for the linear predictor with preferential sampling; regression coefficients for the linear predictor with non-preferential samples.
response	a vector of parameters of the response variable model. These must be provided in the following order: regression coefficients of the explanatory variables; variance and scale of the spatial correlation for the isotropic Gaussian process; and variance of the nugget effect.
preferentiality.par	value of the preferentiality paramter.

### Value

a list of coefficients of class `coef.PrevMap.ps`.

### Author(s)

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

---

shape.matern	<i>Profile likelihood for the shape parameter of the Matern covariance function</i>
--------------	---

---

### Description

This function plots the profile likelihood for the shape parameter of the Matern covariance function used in the linear Gaussian model. It also computes confidence intervals of coverage coverage by interpolating the profile likelihood with a spline and using the asymptotic distribution of a chi-squared with one degree of freedom.

### Usage

```
shape.matern(
  formula,
  coords,
  data,
  set.kappa,
  fixed.rel.nugget = NULL,
  start.par,
  coverage = NULL,
  plot.profile = TRUE,
  messages = TRUE
)
```

### Arguments

formula	an object of class <code>formula</code> (or one that can be coerced to that class): a symbolic description of the model to be fitted.
coords	an object of class <code>formula</code> indicating the geographic coordinates.
data	a data frame containing the variables in the model.
set.kappa	a vector indicating the set values for evaluation of the profile likelihood.
fixed.rel.nugget	a value for the relative variance $\nu^2$ of the nugget effect, that is then treated as fixed. Default is <code>NULL</code> .
start.par	starting values for the scale parameter $\phi$ and the relative variance of the nugget effect $\nu^2$ ; if <code>fixed.rel.nugget</code> is provided, then a starting value for $\phi$ only should be provided.
coverage	a value between 0 and 1 indicating the coverage of the confidence interval based on the interpolated profile likelihood for the shape parameter. Default is <code>coverage=NULL</code> and no confidence interval is then computed.
plot.profile	logical; if <code>TRUE</code> the computed profile-likelihood is plotted together with the interpolating spline.
messages	logical; if <code>messages=TRUE</code> then status messages are printed on the screen (or output device) while the function is running. Default is <code>messages=TRUE</code> .

**Value**

The function returns an object of class 'shape.matern' that is a list with the following components

- `set.kappa` set of values of the shape parameter used to evaluate the profile-likelihood.

- `val.kappa` values of the profile likelihood.

If a value for coverage is specified, the list also contains `lower`, `upper` and `kappa.hat` that correspond to the lower and upper limits of the confidence interval, and the maximum likelihood estimate for the shape parameter, respectively.

**Author(s)**

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---

spat.corr.diagnostic *Diagnostics for residual spatial correlation*

---

**Description**

This function performs two variogram-based tests for residual spatial correlation in real-valued and count (Binomial and Poisson) data.

**Usage**

```
spat.corr.diagnostic(
  formula,
  units.m = NULL,
  coords,
  data,
  likelihood,
  ID.coords = NULL,
  n.sim = 200,
  nAGQ = 1,
  uvec = NULL,
  plot.results = TRUE,
  lse.variogram = FALSE,
  kappa = 0.5,
  which.test = "both"
)
```

**Arguments**

<code>formula</code>	an object of class <code>formula</code> (or one that can be coerced to that class): a symbolic description of the model to be fitted.
<code>units.m</code>	vector of binomial denominators, or offset if the Poisson model is used.
<code>coords</code>	an object of class <code>formula</code> indicating the geographic coordinates.

<code>data</code>	an object of class "data.frame" containing the data.
<code>likelihood</code>	a character that can be set to "Gaussian", "Binomial" or "Poisson"
<code>ID.coords</code>	vector of ID values for the unique set of spatial coordinates obtained from <code>create.ID.coords</code> . These must be provided if, for example, spatial random effects are defined at household level but some of the covariates are at individual level. <b>Warning:</b> the household coordinates must all be distinct otherwise see <code>jitterDupCoords</code> . Default is NULL.
<code>n.sim</code>	number of simulations used to perform the selected test(s) for spatial correlation.
<code>nAGQ</code>	integer scalar (passed to <code>glmer</code> ) - the number of points per axis for evaluating the adaptive Gauss-Hermite approximation to the log-likelihood. Defaults to 1, corresponding to the Laplace approximation. Values greater than 1 produce greater accuracy in the evaluation of the log-likelihood at the expense of speed. A value of zero uses a faster but less exact form of parameter estimation for GLMMs by optimizing the random effects and the fixed-effects coefficients in the penalized iteratively reweighted least squares step.
<code>uvec</code>	a vector with values used to define the variogram binning. If <code>uvec=NULL</code> , then <code>uvec</code> is then set to <code>seq(MIN_DIST, (MAX_DIST-MIN_DIST)/2, length=15)</code> where <code>MIN_DIST</code> and <code>MAX_DIST</code> are the minimum and maximum observed distances.
<code>plot.results</code>	if <code>plot.results=TRUE</code> , a plot is returned showing the results for the selected test(s) for spatial correlation. By default <code>plot.results=TRUE</code> .
<code>lse.variogram</code>	if <code>lse.variogram=TRUE</code> , a weighted least square fit of a Matern function (with fixed kappa) to the empirical variogram is performed. If <code>plot.results=TRUE</code> and <code>lse.variogram=TRUE</code> , the fitted weighted least square fit is displayed as a dashed line in the returned plot.
<code>kappa</code>	smoothness parameter of the Matern function for the Gaussian process to approximate. The default is <code>kappa=0.5</code> .
<code>which.test</code>	a character specifying which test for residual spatial correlation is to be performed: "variogram", "test statistic" or "both". The default is <code>which.test="both"</code> . See 'Details'.

## Details

The function first fits a generalized linear mixed model using the for an outcome  $Y_i$  which, conditionally on i.i.d. random effects  $Z_i$ , are mutually independent GLMs with linear predictor

$$g^{-1}(\eta_i) = d_i' \beta + Z_i$$

where  $d_i$  is a vector of covariates which are specified through formula. Finally, the  $Z_i$  are assumed to be zero-mean Gaussian variables with variance  $\sigma^2$

### Variogram-based graphical diagnostic

This graphical diagnostic is performed by setting `which.test="both"` or `which.test="variogram"`. The output are 95 (see below `lower.lim` and `upper.lim`) that are generated under the assumption of spatial independence through the following steps

1. Fit a generalized linear mixed model as indicated by the equation above.
2. Obtain the mode, say  $\hat{Z}_i$ , of the  $Z_i$  conditioned on the data  $Y_i$ .

3. Compute the empirical variogram using  $\hat{Z}_i$
4. Permute the locations specified in `coords`, `n.sim` time while holding the  $\hat{Z}_i$  fixed.
5. For each of the permuted data-sets compute the empirical variogram based on the  $\hat{Z}_i$ .
6. From the `n.sim` variograms obtained in the previous step, compute the 95

If the observed variogram (`obs.variogram` below), based on the un-permuted  $\hat{Z}_i$ , falls within the 95 residual spatial correlation; if, instead, that partly falls outside the 95

### Test for spatial independence

This diagnostic test is performed if `which.test="both"` or `which.test="test statistic"`. Let  $\hat{v}(B)$  denote the empirical variogram based on  $\hat{Z}_i$  for the distance bin  $B$ . The test statistic used for testing residual spatial correlation is

$$T = \sum_B N(B) \{v(B) - \hat{\sigma}^2\}$$

where  $N(B)$  is the number of pairs of data-points falling within the distance bin  $B$  (`n.bins` below) and  $\hat{\sigma}^2$  is the estimate of  $\sigma^2$ .

To obtain the distribution of the test statistic  $T$  under the null hypothesis of spatial independence, we use the simulated empirical variograms as obtained in step 5 of the iterative procedure described in "Variogram-based graphical diagnostic." The p-value for the test of spatial independence is then computed by taking the proportion of simulated values for  $T$  under the null the hypothesis that are larger than the value of  $T$  based on the original (un-permuted)  $\hat{Z}_i$

### Value

An object of class "PrevMap.diagnostic" which is a list containing the following components:

`obs.variogram`: a vector of length `length(uvec)-1` containing the values of the variogram for each of the distance bins defined through `uvec`.

`distance.bins`: a vector of length `length(uvec)-1` containing the average distance within each of the distance bins defined through `uvec`.

`n.bins`: a vector of length `length(uvec)-1` containing the number of pairs of data-points falling within each distance bin.

`lower.lim`: (available only if `which.test="both"` or `which.test="variogram"`) a vector of length `length(uvec)-1` containing the lower limits of the 95 generated under the assumption of absence of spatial correlation at each fo the distance bins defined through `uvec`.

`upper.lim`: (available only if `which.test="both"` or `which.test="variogram"`) a vector of length `length(uvec)-1` containing the upper limits of the 95 generated under the assumption of absence of spatial correlation at each fo the distance bins defined through `uvec`.

`mode.rand.effects`: the predictive mode of the random effects from the fitted non-spatial generalized linear mixed model.

`p.value`: (available only if `which.test="both"` or `which.test="test statistic"`) p-value of the test for residual spatial correlation.

`lse.variogram`: (available only if `lse.variogram=TRUE`) a vector of length `length(uvec)-1` containing the values of the estimated Matern variogram via a weighted least square fit.

---

 spatial.pred.binomial.Bayes

*Bayesian spatial prediction for the binomial logistic and binary probit models*

---

## Description

This function performs Bayesian spatial prediction for the binomial logistic and binary probit models.

## Usage

```
spatial.pred.binomial.Bayes(
  object,
  grid.pred,
  predictors = NULL,
  type = "marginal",
  scale.predictions = "prevalence",
  quantiles = c(0.025, 0.975),
  standard.errors = FALSE,
  thresholds = NULL,
  scale.thresholds = NULL,
  messages = TRUE
)
```

## Arguments

object	an object of class "Bayes.PrevMap" obtained as result of a call to <a href="#">binomial.logistic.Bayes</a> or <a href="#">binary.probit.Bayes</a> .
grid.pred	a matrix of prediction locations.
predictors	a data frame of the values of the explanatory variables at each of the locations in grid.pred; each column correspond to a variable and each row to a location. <b>Warning:</b> the names of the columns in the data frame must match those in the data used to fit the model. Default is predictors=NULL for models with only an intercept.
type	a character indicating the type of spatial predictions: type="marginal" for marginal predictions or type="joint" for joint predictions. Default is type="marginal". In the case of a low-rank approximation only joint predictions are available.
scale.predictions	a character vector of maximum length 3, indicating the required scale on which spatial prediction is carried out: "logit", "prevalence", "odds" and "probit". Default is scale.predictions="prevalence".
quantiles	a vector of quantiles used to summarise the spatial predictions.
standard.errors	logical; if standard.errors=TRUE, then standard errors for each scale.predictions are returned. Default is standard.errors=FALSE.

thresholds	a vector of exceedance thresholds; default is NULL.
scale.thresholds	a character value ("logit", "prevalence", "odds" or "probit") indicating the scale on which exceedance thresholds are provided.
messages	logical; if messages=TRUE then status messages are printed on the screen (or output device) while the function is running. Default is messages=TRUE.

### Value

A "pred.PrevMap" object list with the following components: `logit`; `prevalence`; `odds`; `probit`; `exceedance.prob`, corresponding to a matrix of the exceedance probabilities where each column corresponds to a specified value in `thresholds`; `samples`, corresponding to a matrix of the posterior samples at each prediction locations for the linear predictor; `grid.pred` prediction locations. Each of the three components `logit`, `prevalence`, `odds` and `probit` is also a list with the following components:

`predictions`: a vector of the predictive mean for the associated quantity (`logit`, `odds` or `prevalence`).

`standard.errors`: a vector of prediction standard errors (if `standard.errors=TRUE`).

`quantiles`: a matrix of quantiles of the resulting predictions with each column corresponding to a quantile specified through the argument `quantiles`.

### Author(s)

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 Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

spatial.pred.binomial.MCML

*Spatial predictions for the binomial logistic model using plug-in of MCML estimates*

---

### Description

This function performs spatial prediction, fixing the model parameters at the Monte Carlo maximum likelihood estimates of a geostatistical binomial logistic model.

### Usage

```
spatial.pred.binomial.MCML(
  object,
  grid.pred,
  predictors = NULL,
  control.mcmc,
  type = "marginal",
  scale.predictions = c("logit", "prevalence", "odds"),
  quantiles = c(0.025, 0.975),
  standard.errors = FALSE,
  thresholds = NULL,
```

```

    scale.thresholds = NULL,
    plot.correlogram = FALSE,
    messages = TRUE
  )

```

## Arguments

object	an object of class "PrevMap" obtained as result of a call to <code>binomial.logistic.MCML</code> .
grid.pred	a matrix of prediction locations.
predictors	a data frame of the values of the explanatory variables at each of the locations in <code>grid.pred</code> ; each column correspond to a variable and each row to a location. <b>Warning:</b> the names of the columns in the data frame must match those in the data used to fit the model. Default is <code>predictors=NULL</code> for models with only an intercept.
control.mcmc	output from <code>control.mcmc.MCML</code> .
type	a character indicating the type of spatial predictions: <code>type="marginal"</code> for marginal predictions or <code>type="joint"</code> for joint predictions. Default is <code>type="marginal"</code> . In the case of a low-rank approximation only joint predictions are available.
scale.predictions	a character vector of maximum length 3, indicating the required scale on which spatial prediction is carried out: "logit", "prevalence" and "odds". Default is <code>scale.predictions=c("logit", "prevalence", "odds")</code> .
quantiles	a vector of quantiles used to summarise the spatial predictions.
standard.errors	logical; if <code>standard.errors=TRUE</code> , then standard errors for each <code>scale.predictions</code> are returned. Default is <code>standard.errors=FALSE</code> .
thresholds	a vector of exceedance thresholds; default is <code>thresholds=NULL</code> .
scale.thresholds	a character value indicating the scale on which exceedance thresholds are provided; "logit", "prevalence" or "odds". Default is <code>scale.thresholds=NULL</code> .
plot.correlogram	logical; if <code>plot.correlogram=TRUE</code> the autocorrelation plot of the conditional simulations is displayed.
messages	logical; if <code>messages=TRUE</code> then status messages are printed on the screen (or output device) while the function is running. Default is <code>messages=TRUE</code> .

## Value

A "pred.PrevMap" object list with the following components: `logit`; `prevalence`; `odds`; `exceedance.prob`, corresponding to a matrix of the exceedance probabilities where each column corresponds to a specified value in `thresholds`; `samples`, corresponding to a matrix of the predictive samples at each prediction locations for the linear predictor of the binomial logistic model (if `scale.predictions="logit"` and neither the SPDE nor the low-rank approximations have been used, this component is `NULL`); `grid.pred` prediction locations. Each of the three components `logit`, `prevalence` and `odds` is also a list with the following components:

`predictions`: a vector of the predictive mean for the associated quantity (logit, odds or prevalence).

standard.errors: a vector of prediction standard errors (if standard.errors=TRUE).

quantiles: a matrix of quantiles of the resulting predictions with each column corresponding to a quantile specified through the argument quantiles.

### Author(s)

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

spatial.pred.linear.Bayes

*Bayesian spatial predictions for the geostatistical Linear Gaussian model*

---

### Description

This function performs Bayesian prediction for a geostatistical linear Gaussian model.

### Usage

```
spatial.pred.linear.Bayes(
  object,
  grid.pred,
  predictors = NULL,
  type = "marginal",
  scale.predictions = c("logit", "prevalence", "odds"),
  quantiles = c(0.025, 0.975),
  standard.errors = FALSE,
  thresholds = NULL,
  scale.thresholds = NULL,
  messages = TRUE
)
```

### Arguments

object	an object of class "Bayes.PrevMap" obtained as result of a call to <a href="#">linear.model.Bayes</a> .
grid.pred	a matrix of prediction locations.
predictors	a data frame of the values of the explanatory variables at each of the locations in grid.pred; each column correspond to a variable and each row to a location. <b>Warning:</b> the names of the columns in the data frame must match those in the data used to fit the model. Default is predictors=NULL for models with only an intercept.
type	a character indicating the type of spatial predictions: type="marginal" for marginal predictions or type="joint" for joint predictions. Default is type="marginal". In the case of a low-rank approximation only joint predictions are available.

scale.predictions	a character vector of maximum length 3, indicating the required scale on which spatial prediction is carried out: "logit", "prevalence" and "odds". Default is <code>scale.predictions=c("logit", "prevalence", "odds")</code> .
quantiles	a vector of quantiles used to summarise the spatial predictions.
standard.errors	logical; if <code>standard.errors=TRUE</code> , then standard errors for each <code>scale.predictions</code> are returned. Default is <code>standard.errors=FALSE</code> .
thresholds	a vector of exceedance thresholds; default is <code>thresholds=NULL</code> .
scale.thresholds	a character value indicating the scale on which exceedance thresholds are provided: "logit", "prevalence" or "odds". Default is <code>scale.thresholds=NULL</code> .
messages	logical; if <code>messages=TRUE</code> then status messages are printed on the screen (or output device) while the function is running. Default is <code>messages=TRUE</code> .

### Value

A "pred.PrevMap" object list with the following components: `logit`; `prevalence`; `odds`; `exceedance.prob`, corresponding to a matrix of the exceedance probabilities where each column corresponds to a specified value in `thresholds`; `grid.pred` prediction locations. Each of the three components `logit`, `prevalence` and `odds` is also a list with the following components:

`predictions`: a vector of the predictive mean for the associated quantity (logit, odds or prevalence).

`standard.errors`: a vector of prediction standard errors (if `standard.errors=TRUE`).

`quantiles`: a matrix of quantiles of the resulting predictions with each column corresponding to a quantile specified through the argument `quantiles`.

### Author(s)

Emanuele Giorgi <[e.giorgi@lancaster.ac.uk](mailto:e.giorgi@lancaster.ac.uk)>

Peter J. Diggle <[p.diggle@lancaster.ac.uk](mailto:p.diggle@lancaster.ac.uk)>

---

spatial.pred.linear.MLE

*Spatial predictions for the geostatistical Linear Gaussian model using  
plug-in of ML estimates*

---

### Description

This function performs spatial prediction, fixing the model parameters at the maximum likelihood estimates of a linear geostatistical model.

**Usage**

```

spatial.pred.linear.MLE(
  object,
  grid.pred,
  predictors = NULL,
  predictors.samples = NULL,
  type = "marginal",
  scale.predictions = c("logit", "prevalence", "odds"),
  quantiles = c(0.025, 0.975),
  n.sim.prev = 0,
  standard.errors = FALSE,
  thresholds = NULL,
  scale.thresholds = NULL,
  messages = TRUE,
  include.nugget = FALSE
)

```

**Arguments**

object	an object of class "PrevMap" obtained as result of a call to <a href="#">linear.model.MLE</a> .
grid.pred	a matrix of prediction locations.
predictors	a data frame of the values of the explanatory variables at each of the locations in <code>grid.pred</code> ; each column correspond to a variable and each row to a location. <b>Warning:</b> the names of the columns in the data frame must match those in the data used to fit the model. Default is <code>predictors=NULL</code> for models with only an intercept.
predictors.samples	a list of data frame objects. This argument is used to average over repeated simulations of the predictor variables in order to obtain an "average" map over the distribution of the explanatory variables in the model. Each component of the list is a simulation. The number of simulations passed through <code>predictors.samples</code> must be the same as <code>n.sim.prev</code> . NOTE: This argument can currently only be used only for a linear regression model that does not use any approximation of the spatial Gaussian process.
type	a character indicating the type of spatial predictions: <code>type="marginal"</code> for marginal predictions or <code>type="joint"</code> for joint predictions. Default is <code>type="marginal"</code> . In the case of a low-rank approximation only marginal predictions are available.
scale.predictions	a character vector of maximum length 3, indicating the required scale on which spatial prediction is carried out: "logit", "prevalence" and "odds". Default is <code>scale.predictions=c("logit", "prevalence", "odds")</code> .
quantiles	a vector of quantiles used to summarise the spatial predictions.
n.sim.prev	number of simulation for non-linear predictive targets. Default is <code>n.sim.prev=0</code> .
standard.errors	logical; if <code>standard.errors=TRUE</code> , then standard errors for each <code>scale.predictions</code> are returned. Default is <code>standard.errors=FALSE</code> .

thresholds	a vector of exceedance thresholds; default is thresholds=NULL.
scale.thresholds	a character value indicating the scale on which exceedance thresholds are provided; "logit", "prevalence" or "odds". Default is scale.thresholds=NULL.
messages	logical; if messages=TRUE then status messages are printed on the screen (or output device) while the function is running. Default is messages=TRUE.
include.nugget	logical; if include.nugget=TRUE then the nugget effect is included in the predictions. This option is available only for fitted linear models with locations having multiple observations. Default is include.nugget=FALSE.

### Value

A "pred.PrevMap" object list with the following components: logit; prevalence; odds; exceedance.prob, corresponding to a matrix of the exceedance probabilities where each column corresponds to a specified value in thresholds; grid.pred prediction locations; samples, corresponding to the predictive samples of the linear predictor (only if any(scale.predictions=="prevalence")). Each of the three components logit, prevalence and odds is also a list with the following components:

- predictions: a vector of the predictive mean for the associated quantity (logit, odds or prevalence).
- standard.errors: a vector of prediction standard errors (if standard.errors=TRUE).
- quantiles: a matrix of quantiles of the resulting predictions with each column corresponding to a quantile specified through the argument quantiles.
- samples: If  $n.sim.prev > 0$ , the function returns  $n.sim.prev$  samples of the linear predictor at each of the prediction locations.

### Author(s)

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>  
 Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

spatial.pred.lm.ps      *Spatial predictions for the geostatistical Linear Gaussian model using plug-in of ML estimates*

---

### Description

This function performs spatial prediction, fixing the model parameters at the maximum likelihood estimates of a linear geostatistical model.

### Usage

```
spatial.pred.lm.ps(
  object,
  grid.pred = NULL,
  predictors = NULL,
  predictors.intensity = NULL,
```

```

control.mcmc = NULL,
target = 3,
type = "marginal",
quantiles = NULL,
standard.errors = FALSE,
messages = TRUE,
return.samples = FALSE
)

```

## Arguments

object	an object of class "PrevMap" obtained as result of a call to <a href="#">linear.model.MLE</a> .
grid.pred	a matrix of prediction locations. Default is grid.pred=NULL, in which case the grid used to approximate the intractable integral in the log-Gaussian Cox process model is used for prediction.
predictors	a data frame of the values of the explanatory variables at each of the locations in grid.pred, for the response variable model; each column correspond to a variable and each row to a location. <b>Warning:</b> the names of the columns in the data frame must match those in the data used to fit the model. Default is predictors=NULL for models with only an intercept.
predictors.intensity	a data frame of the values of the explanatory variables at each of the locations in grid.pred, for the log-Gaussian Cox process model; each column correspond to a variable and each row to a location. <b>Warning:</b> the names of the columns in the data frame must match those in the data used to fit the model. Default is predictors=NULL for models with only an intercept.
control.mcmc	output from <a href="#">control.mcmc.MCML</a> which defined the control parameters of the Monte Carlo Markov chain algorithm.
target	an integer indicating the predictive target: target=1 if the predictive target is the linear predictor of the response; target=2 is the predictive target is the sampling intensity of the preferentially sampled data; target=3 if both of the above are the predictive targets. Default is target=3.
type	a character indicating the type of spatial predictions for target=1: type="marginal" for marginal predictions or type="joint" for joint predictions. Default is type="marginal". Note that predictions for the sampling intensity (target=2) are always joint.
quantiles	a vector of quantiles used to summarise the spatial predictions.
standard.errors	logical; if standard.errors=TRUE, then standard errors for each scale predictions are returned. Default is standard.errors=FALSE.
messages	logical; if messages=TRUE then status messages are printed on the screen (or output device) while the function is running. Default is messages=TRUE.
return.samples	logical; if return.samples=TRUE a matrix of the predictive samples for the prediction target (as specified in target) are returned in the output.

**Value**

A "pred.PrevMap.ps" object list with the following components: response (if target=1 or target=3) and intensity (if target=2 or target=3). grid.pred prediction locations. Each of the components intensity and response is a list with the following components:

predictions: a vector of the predictive mean for the corresponding target.

standard.errors: a vector of prediction standard errors (if standard.errors=TRUE).

quantiles: a matrix of quantiles of the resulting predictions with each column corresponding to a quantile specified through the argument quantiles.

samples: a matrix corresponding to the predictive samples of the predictive target (only if return.samples=TRUE), with each row corresponding to a samples and column to a prediction location. In the case of a model with a mix of preferential and non-preferential data, if target=1 or target=3, each of the above components will be a list with two components, namely preferential and non.preferential, associated with response.

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

---

spatial.pred.poisson.MCML

*Spatial predictions for the Poisson model with log link function, using plug-in of MCML estimates*

---

**Description**

This function performs spatial prediction, fixing the model parameters at the Monte Carlo maximum likelihood estimates of a geostatistical Poisson model with log link function.

**Usage**

```
spatial.pred.poisson.MCML(
  object,
  grid.pred,
  predictors = NULL,
  control.mcmc,
  type = "marginal",
  scale.predictions = c("log", "exponential"),
  quantiles = c(0.025, 0.975),
  standard.errors = FALSE,
  thresholds = NULL,
  scale.thresholds = NULL,
  plot.correlogram = FALSE,
  messages = TRUE
)
```

**Arguments**

object	an object of class "PrevMap" obtained as result of a call to <code>poisson.log.MCML</code> .
grid.pred	a matrix of prediction locations.
predictors	a data frame of the values of the explanatory variables at each of the locations in <code>grid.pred</code> ; each column correspond to a variable and each row to a location. <b>Warning:</b> the names of the columns in the data frame must match those in the data used to fit the model. Default is <code>predictors=NULL</code> for models with only an intercept.
control.mcmc	output from <code>control.mcmc.MCML</code> .
type	a character indicating the type of spatial predictions: <code>type="marginal"</code> for marginal predictions or <code>type="joint"</code> for joint predictions. Default is <code>type="marginal"</code> . In the case of a low-rank approximation only joint predictions are available.
scale.predictions	a character vector of maximum length 2, indicating the required scale on which spatial prediction is carried out: "log" and "exponential". Default is <code>scale.predictions=c("log", "exp"</code>
quantiles	a vector of quantiles used to summarise the spatial predictions.
standard.errors	logical; if <code>standard.errors=TRUE</code> , then standard errors for each <code>scale.predictions</code> are returned. Default is <code>standard.errors=FALSE</code> .
thresholds	a vector of exceedance thresholds; default is <code>thresholds=NULL</code> .
scale.thresholds	a character value indicating the scale on which exceedance thresholds are provided; "log" or "exponential". Default is <code>scale.thresholds=NULL</code> .
plot.correlogram	logical; if <code>plot.correlogram=TRUE</code> the autocorrelation plot of the conditional simulations is displayed.
messages	logical; if <code>messages=TRUE</code> then status messages are printed on the screen (or output device) while the function is running. Default is <code>messages=TRUE</code> .

**Value**

A "pred.PrevMap" object list with the following components: `log`; `exponential`; `exceedance.prob`, corresponding to a matrix of the exceedance probabilities where each column corresponds to a specified value in `thresholds`; `samples`, corresponding to a matrix of the predictive samples at each prediction locations for the linear predictor of the Poisson model (if `scale.predictions="log"` this component is `NULL`); `grid.pred` prediction locations. Each of the three components `log` and `exponential` is also a list with the following components:

`predictions`: a vector of the predictive mean for the associated quantity (log or exponential).

`standard.errors`: a vector of prediction standard errors (if `standard.errors=TRUE`).

`quantiles`: a matrix of quantiles of the resulting predictions with each column corresponding to a quantile specified through the argument `quantiles`.

**Author(s)**

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 Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

summary.Bayes.PrevMap *Summarizing Bayesian model fits*

---

**Description**

summary method for the class "Bayes.PrevMap" that computes the posterior mean, median, mode and high posterior density intervals using samples from Bayesian fits.

**Usage**

```
## S3 method for class 'Bayes.PrevMap'
summary(object, hpd.coverage = 0.95, ...)
```

**Arguments**

object            an object of class "Bayes.PrevMap" obtained as result of a call to [binomial.logistic.Bayes](#) or [linear.model.Bayes](#).

hpd.coverage    value of the coverage of the high posterior density intervals; default is 0.95.

...              further arguments passed to or from other methods.

**Value**

A list with the following values

linear: logical value that is TRUE if a linear model was fitted and FALSE otherwise.

binary: logical value that is TRUE if a binary model was fitted and FALSE otherwise.

probit: logical value that is TRUE if a binary model with probit link function was fitted and FALSE if with logistic link function.

ck: logical value that is TRUE if a low-rank approximation was fitted and FALSE otherwise.

beta: matrix of the posterior summaries for the regression coefficients.

sigma2: vector of the posterior summaries for sigma2.

phi: vector of the posterior summaries for phi.

tau2: vector of the posterior summaries for tau2.

call: matched call.

kappa: fixed value of the shape parameter of the Matern covariance function.

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>  
 Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

summary.PrevMap      *Summarizing likelihood-based model fits*

---

### Description

summary method for the class "PrevMap" that computes the standard errors and p-values of likelihood-based model fits.

### Usage

```
## S3 method for class 'PrevMap'
summary(object, log.cov.pars = TRUE, ...)
```

### Arguments

object	an object of class "PrevMap" obtained as result of a call to <code>binomial.logistic.MCML</code> or <code>linear.model.MLE</code> .
log.cov.pars	logical; if <code>log.cov.pars=TRUE</code> the estimates of the covariance parameters are given on the log-scale. Note that standard errors are also adjusted accordingly. Default is <code>log.cov.pars=TRUE</code> .
...	further arguments passed to or from other methods.

### Value

A list with the following components

`linear`: logical value; `linear=TRUE` if a linear model was fitted and `linear=FALSE` otherwise.

`poisson`: logical value; `poisson=TRUE` if a Poisson model was fitted and `poisson=FALSE` otherwise.

`ck`: logical value; `ck=TRUE` if a low-rank approximation was used and `ck=FALSE` otherwise.

`spde`: logical value; `spde=TRUE` if the SPDE approximation was used and `spde=FALSE` otherwise.

`coefficients`: matrix of the estimates, standard errors and p-values of the estimates of the regression coefficients.

`cov.pars`: matrix of the estimates and standard errors of the covariance parameters.

`log.lik`: value of likelihood function at the maximum likelihood estimates.

`kappa`: fixed value of the shape parameter of the Matern covariance function.

`kappa.t`: fixed value of the shape parameter of the Matern covariance function for the temporal covariance matrix, if a spatio-temporal model has been fitted.

`fixed.rel.nugget`: fixed value for the relative variance of the nugget effect.

`call`: matched call.

### Author(s)

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

summary.PrevMap.ps	<i>Summarizing fits of geostatistical linear models with preferentially sampled locations</i>
--------------------	---

---

**Description**

summary method for the class "PrevMap" that computes the standard errors and p-values of likelihood-based model fits.

**Usage**

```
## S3 method for class 'PrevMap.ps'
summary(object, log.cov.pars = TRUE, ...)
```

**Arguments**

object	an object of class "PrevMap.ps" obtained as result of a call to <a href="#">lm.ps.MCML</a> .
log.cov.pars	logical; if log.cov.pars=TRUE the estimates of the covariance parameters are given on the log-scale. Note that standard errors are also adjusted accordingly. Default is log.cov.pars=TRUE.
...	further arguments passed to or from other methods.

**Value**

A list with the following components

coefficients.response: matrix of the estimates, standard errors and p-values of the estimates of the regression coefficients for the response variable.

coefficients.intensity: matrix of the estimates, standard errors and p-values of the estimates of the regression coefficients for the sampling intensity of the log-Gaussian process.

cov.pars.response: matrix of the estimates and standard errors of the covariance parameters for the Gaussian process associated with the response.

cov.pars.intensity: matrix of the estimates and standard errors of the covariance parameters for the Gaussian process associated with the log-Gaussian process.

log.lik: value of likelihood function at the maximum likelihood estimates.

kappa.response: fixed value of the shape parameter of the Matern covariance function.

call: matched call.

**Author(s)**

Emanuele Giorgi <[e.giorgi@lancaster.ac.uk](mailto:e.giorgi@lancaster.ac.uk)>

---

trace.plot	<i>Trace-plots for posterior samples</i>
------------	--

---

**Description**

Displays the trace-plots for the posterior samples of the model parameters and spatial random effects.

**Usage**

```
trace.plot(object, param, component.beta = NULL, component.S = NULL)
```

**Arguments**

object	an object of class 'Bayes.PrevMap'.
param	a character indicating for which component of the model the density plot is required: param="beta" for the regression coefficients; param="sigma2" for the variance of the spatial random effect; param="phi" for the scale parameter of the Matern correlation function; param="tau2" for the variance of the nugget effect; param="S" for the spatial random effect.
component.beta	if param="beta", component.beta is a numeric value indicating the component of the regression coefficients; default is NULL.
component.S	if param="S", component.S can be a numeric value indicating the component of the spatial random effect. Default is NULL.

**Author(s)**

Emanuele Giorgi <e.giorgi@lancaster.ac.uk>

Peter J. Diggle <p.diggle@lancaster.ac.uk>

---

trace.plot.MCML	<i>Trace-plots of the importance sampling distribution samples from the MCML method</i>
-----------------	---

---

**Description**

Trace-plots of the MCMC samples from the importance sampling distribution used in [binomial.logistic.MCML](#).

**Usage**

```
trace.plot.MCML(object, component = NULL, ...)
```

**Arguments**

object	an object of class "PrevMap" obtained as result of a call to <a href="#">binomial.logistic.MCML</a> .
component	a positive integer indicating the number of the random effect component for which a trace-plot is required. If component=NULL, then a component is selected at random. Default is component=NULL.
...	further arguments passed to <a href="#">plot</a> .

**Author(s)**

Emanuele Giorgi <[e.giorgi@lancaster.ac.uk](mailto:e.giorgi@lancaster.ac.uk)>

Peter J. Diggle <[p.diggle@lancaster.ac.uk](mailto:p.diggle@lancaster.ac.uk)>

---

trend.plot	<i>Plot of trends</i>
------------	-----------------------

---

**Description**

This function produces a plot of the variable of interest against each of the two geographical coordinates.

**Usage**

```
trend.plot(data, var.name, coords, ...)
```

**Arguments**

data	an object of class "data.frame" containing the data.
var.name	a <a href="#">formula</a> object indicating the variable to display.
coords	a <a href="#">formula</a> object indicating the geographical coordinates.
...	additional arguments to be passed to <a href="#">plot</a> .

---

variog.diagnostic.glm	<i>Variogram-based validation for generalized linear geostatistical model fits (Binomial and Poisson)</i>
-----------------------	---

---

**Description**

This function performs model validation for generalized linear geostatistical models (Binomial and Poisson) using Monte Carlo methods based on the variogram.

**Usage**

```
variog.diagnostic.glgm(
  object,
  n.sim = 200,
  uvec = NULL,
  plot.results = TRUE,
  which.test = "both"
)
```

**Arguments**

object	an object of class "PrevMap" obtained as an output from <code>binomial.logistic.MCML</code> and <code>poisson.log.MCML</code> .
n.sim	integer indicating the number of simulations used for the variogram-based diagnostics. Default is <code>n.sim=1000</code> .
uvec	a vector with values used to define the variogram binning. If <code>uvec=NULL</code> , then <code>uvec</code> is then set to <code>seq(MIN_DIST, (MAX_DIST-MIN_DIST)/2, length=15)</code>
plot.results	if <code>plot.results=TRUE</code> , a plot is returned showing the results for the selected test(s) for spatial correlation. By default <code>plot.results=TRUE</code> . defined as the distance at which the fitted spatial correlation is no less than 0.05. Default is <code>range.fact=1</code>
which.test	a character specifying which test for residual spatial correlation is to be performed: "variogram", "test statistic" or "both". The default is <code>which.test="both"</code> . See 'Details.'

**Details**

The function takes as an input through the argument `object` a fitted generalized linear geostatistical model for an outcome  $Y_i$ , with linear predictor

$$\eta_i = d_i' \beta + S(x_i) + Z_i$$

where  $d_i$  is a vector of covariates which are specified through formula,  $S(x_i)$  is a spatial Gaussian process and the  $Z_i$  are assumed to be zero-mean Gaussian. The model validation is performed on the adopted stationary and isotropic Matern covariance function used for  $S(x_i)$ . More specifically, the function allows the users to select either of the following validation procedures.

**Variogram-based graphical validation**

This graphical diagnostic is performed by setting `which.test="both"` or `which.test="variogram"`. The output are 95 (see below `lower.lim` and `upper.lim`) that are generated under the assumption that the fitted model did generate the analysed data-set. This validation procedure proceed through the following steps.

1. Obtain the mean, say  $\hat{Z}_i$ , of the  $Z_i$  conditioned on the data  $Y_i$  and by setting  $S(x_i) = 0$  in the equation above.
2. Compute the empirical variogram using  $\hat{Z}_i$
3. Simulate `n.sim` data-sets under the fitted geostatistical model.

4. For each of the simulated data-sets and obtain  $\hat{Z}_i$  as in Step 1. Finally, compute the empirical variogram based on the resulting  $\hat{Z}_i$ .

5. From the `n.sim` variograms obtained in the previous step, compute the 95

If the observed variogram (`obs.variogram` below), based on the  $\hat{Z}_i$  from Step 2, falls within the 95 evidence against the fitted spatial correlation model; if, instead, that partly falls outside the 95 correlation in the data.

### Test for suitability of the adopted correlation function

This diagnostic test is performed if `which.test="both"` or `which.test="test statistic"`. Let  $v_E(B)$  and  $v_T(B)$  denote the empirical and theoretical variograms based on  $\hat{Z}_i$  for the distance bin  $B$ . The test statistic used for testing residual spatial correlation is

$$T = \sum_B N(B) \{v_E(B) - v_T(B)\}$$

where  $N(B)$  is the number of pairs of data-points falling within the distance bin  $B$  (`n.bins` below).

To obtain the distribution of the test statistic  $T$  under the null hypothesis that the fitted model did generate the analysed data-set, we use the simulated empirical variograms as obtained in step 5 of the iterative procedure described in "Variogram-based graphical validation." The p-value for the test of suitability of the fitted spatial correlation function is then computed by taking the proportion of simulated values for  $T$  that are larger than the value of  $T$  based on the original  $\hat{Z}_i$  in Step 1.

### Value

An object of class "PrevMap.diagnostic" which is a list containing the following components:

`obs.variogram`: a vector of length `length(uvec)-1` containing the values of the variogram for each of the distance bins defined through `uvec`.

`distance.bins`: a vector of length `length(uvec)-1` containing the average distance within each of the distance bins defined through `uvec`.

`n.bins`: a vector of length `length(uvec)-1` containing the number of pairs of data-points falling within each distance bin.

`lower.lim`: (available only if `which.test="both"` or `which.test="variogram"`) a vector of length `length(uvec)-1` containing the lower limits of the 95 generated under the assumption of absence of suitability of the fitted model at each of the distance bins defined through `uvec`.

`upper.lim`: (available only if `which.test="both"` or `which.test="variogram"`) a vector of length `length(uvec)-1` containing the upper limits of the 95 generated under the assumption of absence of suitability of the fitted model at each of the distance bins defined through `uvec`.

`mode.rand.effects`: the predictive mode of the random effects from the fitted non-spatial generalized linear mixed model.

`p.value`: (available only if `which.test="both"` or `which.test="test statistic"`) p-value of the test for residual spatial correlation.

`lse.variogram`: (available only if `lse.variogram=TRUE`) a vector of length `length(uvec)-1` containing the values of the estimated Matern variogram via a weighted least square fit.

---

variog.diagnostic.lm *Variogram-based validation for linear geostatistical model fits*

---

### Description

This function performs model validation for linear geostatistical model using Monte Carlo methods based on the variogram.

### Usage

```
variog.diagnostic.lm(
  object,
  n.sim = 1000,
  uvec = NULL,
  plot.results = TRUE,
  range.fact = 1,
  which.test = "both",
  param.uncertainty = FALSE
)
```

### Arguments

object	an object of class "PrevMap" obtained as an output from <a href="#">linear.model.MLE</a> .
n.sim	integer indicating the number of simulations used for the variogram-based diagnostics. Default is n.sim=1000.
uvec	a vector with values used to define the variogram binning. If uvec=NULL, then uvec is then set to seq(MIN_DIST, (MAX_DIST-MIN_DIST)/2, length=15)
plot.results	if plot.results=TRUE, a plot is returned showing the results for the selected test(s) for spatial correlation. By default plot.results=TRUE.
range.fact	a value between 0 and 1 used to disregard all distance bins provided through uvec that are larger than the (pr)xrange.fact, where pr is the practical range, defined as the distance at which the fitted spatial correlation is no less than 0.05. Default is range.fact=1
which.test	a character specifying which test for residual spatial correlation is to be performed: "variogram", "test statistic" or "both". The default is which.test="both". See 'Details.'
param.uncertainty	a logical indicating whether uncertainty in the model parameters should be incorporated in the selected diagnostic tests. Default is param.uncertainty=FALSE. See 'Details.'

### Details

The function takes as an input through the argument object a fitted linear geostaistical model for an outcome  $Y_i$ , which is expressed as

$$Y_i = d_i' \beta + S(x_i) + Z_i$$

where  $d_i$  is a vector of covariates which are specified through formula,  $S(x_i)$  is a spatial Gaussian process and the  $Z_i$  are assumed to be zero-mean Gaussian. The model validation is performed on the adopted stationary and isotropic Matern covariance function used for  $S(x_i)$ . More specifically, the function allows the users to select either of the following validation procedures.

### Variogram-based graphical validation

This graphical diagnostic is performed by setting `which.test="both"` or `which.test="variogram"`. The output are 95 (see below `lower.lim` and `upper.lim`) that are generated under the assumption that the fitted model did generate the analysed data-set. This validation procedure proceed through the following steps.

1. Obtain the mean, say  $\hat{Z}_i$ , of the  $Z_i$  conditioned on the data  $Y_i$ .
2. Compute the empirical variogram using  $\hat{Z}_i$
3. Simulate `n.sim` data-sets under the fitted geostatistical model.
4. For each of the simulated data-sets and obtain  $\hat{Z}_i$  as in Step 1. Finally, compute the empirical variogram based on the resulting  $\hat{Z}_i$ .
5. From the `n.sim` variograms obtained in the previous step, compute the 95

If the observed variogram (`obs.variogram` below), based on the  $\hat{Z}_i$  from Step 2, falls within the 95 evidence against the fitted spatial correlation model; if, instead, that partly falls outside the 95 correlation in the data.

### Test for suitability of the adopted correlation function

This diagnostic test is performed if `which.test="both"` or `which.test="test statistic"`. Let  $v_E(B)$  and  $v_T(B)$  denote the empirical and theoretical variograms based on  $\hat{Z}_i$  for the distance bin  $B$ . The test statistic used for testing residual spatial correlation is

$$T = \sum_B N(B) \{v_E(B) - v_T(B)\}$$

where  $N(B)$  is the number of pairs of data-points falling within the distance bin  $B$  (`n.bins` below).

To obtain the distribution of the test statistic  $T$  under the null hypothesis that the fitted model did generate the analysed data-set, we use the simulated empirical variograms as obtained in step 5 of the iterative procedure described in "Variogram-based graphical validation." The p-value for the test of suitability of the fitted spatial correlation function is then computed by taking the proportion of simulated values for  $T$  that are larger than the value of  $T$  based on the original  $\hat{Z}_i$  in Step 1.

### Value

An object of class "PrevMap.diagnostic" which is a list containing the following components:

`obs.variogram`: a vector of length `length(uvec)-1` containing the values of the variogram for each of the distance bins defined through `uvec`.

`distance.bins`: a vector of length `length(uvec)-1` containing the average distance within each of the distance bins defined through `uvec`.

`n.bins`: a vector of length `length(uvec)-1` containing the number of pairs of data-points falling within each distance bin.

`lower.lim`: (available only if `which.test="both"` or `which.test="variogram"`) a vector of length `length(uvec)-1` containing the lower limits of the 95 generated under the assumption of absence of suitability of the fitted model at each of the distance bins defined through `uvec`.

`upper.lim`: (available only if `which.test="both"` or `which.test="variogram"`) a vector of length `length(uvec)-1` containing the upper limits of the 95 generated under the assumption of absence of suitability of the fitted model at each of the distance bins defined through `uvec`.

`mode.rand.effects`: the predictive mode of the random effects from the fitted non-spatial generalized linear mixed model.

`p.value`: (available only if `which.test="both"` or `which.test="test statistic"`) p-value of the test for residual spatial correlation.

`lse.variogram`: (available only if `lse.variogram=TRUE`) a vector of length `length(uvec)-1` containing the values of the estimated Matern variogram via a weighted least square fit.

---

variogram

*The empirical variogram*

---

### Description

This function computes sample (empirical) variograms with options for the classical or robust estimators. Output can be returned as a binned variogram, a variogram cloud or a smoothed variogram. Data transformation (Box-Cox) is allowed. "Trends" can be specified and are fitted by ordinary least squares in which case the variograms are computed using the residuals.

### Usage

```
variogram(data, var.name, coords, ...)
```

### Arguments

<code>data</code>	an object of class "data.frame" containing the data.
<code>var.name</code>	a <a href="#">formula</a> object indicating the variable to display.
<code>coords</code>	a <a href="#">formula</a> object indicating the geographical coordinates.
<code>...</code>	additional arguments to be passed to <code>variog</code> .

### Value

An object of the class "variogram" which is list containing components as detailed in `variog`.

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